



**WorkKeys
Applied Math
Technical Manual**

Table of Contents

List of Tables	vi
List of Figures	viii
Chapter 1	
Applied Math Assessment—Overview	1.1
1.1 WorkKeys and the Applied Math Assessment	1.1
1.2 The Workplace Skills Gap and the WorkKeys Solution	1.1
1.3 Mathematics in the Classroom and the Workplace	1.3
1.3.1 Workplace Math	1.3
1.4 WorkKeys Applied Math—Assessment Claims	1.5
1.5 Test Users and Stakeholders	1.5
1.6 Alignment to ACT’s Holistic Framework	1.7
Chapter 2	
Test Development.	2.1
2.1 Applied Math—Overview	2.1
2.2 Applied Math Domain	2.1
2.3 Revisions to Applied Math Domain as a Result of Review	2.2
2.4 Applied Math—Item Stem Characteristics	2.2
2.5 WorkKeys Applied Math—Skill Definitions	2.4
2.6 WorkKeys Applied Math—Performance Level Descriptors	2.8
Applied Math Level 3	2.8
Applied Math Level 4	2.9
Applied Math Level 5	2.9
Applied Math Level 6	2.10
Applied Math Level 7	2.10
2.7 Designing Items to Elicit Evidence of Applied Math	2.11
2.7.1 Item Writing	2.11
2.7.2 Item Review	2.11
2.7.3 Item Pretesting	2.12

Chapter 3

Test Specifications	3.1
3.1 WorkKeys Applied Math Specifications—Overview.	3.1
3.2 Content Relevance and Representativeness	3.2
3.3 Applied Math—Test Blueprint.	3.2

Chapter 4

Test Administration	4.1
4.1 Policies and Procedures	4.1
4.1.1 Standardized Procedures	4.1
4.1.2 Selecting Testing Staff	4.2
4.2 Test Administration Personnel and their Responsibilities	4.3
4.2.1 Test Coordinator	4.3
4.2.2 Back-up Test Coordinator.	4.4
4.2.3 Test Accommodations Coordinator.	4.5
4.2.4 Room Supervisor	4.5
4.2.5 Proctor	4.6
4.3 Training Testing Staff	4.6
4.3.1 Training Session.	4.7
4.3.2 <i>Administration Manual</i>	4.7
4.4 Test Administration Room Requirements.	4.7

Chapter 5

Accessibility.	5.1
5.1 ACT WorkKeys Applied Math Assessment Support System	5.1
5.2 Test Administration and Accessibility Levels of Support	5.3
Support Level 1: Default Embedded System Tools.	5.4
Support Level 2: Open Access Tools	5.5
Support Level 3: Accommodations	5.6
Support Level 4: Modifications	5.7
5.3 Allowable Embedded Tools, Open Access, and Accommodations	5.7
5.4 Valid Test Scores and Equal Benefit for All Examinees	5.8

Chapter 6

Test and Information Security	6.1
6.1 Test Security	6.1
6.2 Information Security.	6.2

Chapter 7	
Reporting	7.1
7.1 Applied Math Reports	7.1
Chapter 8	
Scores and Score Scales	8.1
8.1 Overview	8.1
8.2 Selected-Response Item Scoring	8.2
8.3 Scale Score and Level Score Differences and Rationale	8.2
8.4 Procedures for Establishing the Score Scale	8.3
8.5 Procedures for Establishing the Level Scores.	8.7
Chapter 9	
Equating and Linking.	9.1
9.1 Equating Method and Procedures.	9.1
9.2 Mode Comparability	9.2
9.2.1 Mode Comparability: Study Design	9.3
9.2.2 Mode Comparability: Sample	9.3
9.2.3 Mode Comparability: Comparisons on Items, Tests, and Score Conversions.	9.4
9.2.4 Mode Comparability: Score Comparisons	9.7
9.3 Linking Applied Mathematics to Applied Math Score Scale	9.9
9.3.1 Study Design and Sample Representativeness	9.9
9.3.2 Comparison of Omit Rates and Testing Time Between Applied Mathematics and Applied Math.	9.10
9.3.3 Scale Score Distributions for Applied Mathematics and Applied Math	9.11
9.3.4 Concordance from Applied Mathematics to Applied Math	9.12
9.3.5 Evaluation of Applied Mathematics Forms After Linking	9.12
Chapter 10	
Reliability and Measurement Error	10.1
10.1 Overview	10.1
10.2 Reliability Coefficients and Standard Error of Measurement (SEM).	10.2
10.3 Generalizability Theory	10.3
10.4 Classification Consistency of Level Scores.	10.4

Chapter 11

Validity	11.1
11.1 Validation of Test Score Uses and Interpretations	11.1
11.2 Purpose of the Applied Math Assessment	11.2
11.3 Applied Math Assessment Claims	11.3
11.4 Applied Math—A Measure of Foundational Workforce Skills	11.5
11.4.1 Foundational Workplace Skills	11.5
11.4.2 Applied Math—A Foundational Workplace Skill	11.6
11.4.3 Applied Math—Construct Defined	11.7
11.4.4 Applied Math—Field Test Sampling	11.7
11.4.5 Measuring Applied Math	11.8
11.4.6 Applied Math—Evidence Based on Internal Structure	11.10
11.4.7 Standard Setting	11.12
11.4.8 Applied Math Measurement—Summary	11.12
11.5 Applied Math—Primary Claims and Relevant Findings	11.13
11.5.1 Applied Mathematics—Evidence Based on Test Content	11.14
11.5.2 Applied Mathematics—Evidence Based on Relationships to Work-related Variables	11.16
11.5.3 Applied Mathematics and Return on Investment	11.18
11.5.4 Applied Mathematics and Educational Outcomes	11.19
11.5.5 Applied Math at the State and Regional Level	11.19
11.6 Applied Math—Evaluation of Claims	11.19
11.7 Applied Math—Evidence Based on the Consequences of Testing	11.21
11.7.1 Intended Outcomes	11.21
11.7.2 Adverse Impact	11.21
11.8 Applied Math—Ongoing Validation	11.22

Chapter 12

Assessment Fairness	12.1
12.1 Test Fairness—Overview	12.1
12.2 Fairness and Test Administration	12.2
12.3 Fairness in Access to the Construct Measured	12.2
12.4 Fairness as Lack of Measurement Bias	12.3
12.4.1 DIF Analysis Results from Applied Math Field Testing	12.5
12.5 Fairness as Validity of Individual Score Interpretations	12.7

Chapter 13

Defining Readiness for Work and Careers 13.1

 13.1 Work and Career Readiness Standards and Benchmarks 13.2

 13.2 Using WorkKeys Assessments for Career and Work Readiness 13.3

 13.2.1 Personnel Selection and Development 13.4

 13.2.2 Workforce and Economic Development. 13.4

 13.2.3 Accountability 13.4

References R.1

List of Tables

Table 2.1: Item Stem Characteristics by Level	2.4
Table 2.2: Skill 1.0—Basic Operations with Numbers Including Decimals	2.5
Table 2.3: Skill 2.0—Fractions	2.5
Table 2.4: Skill 3.0—Percentages/Ratios/Proportions	2.6
Table 2.5: Skill 4.0—Unit Conversions	2.6
Table 2.6: Skill 5.0—Geometric Measurement	2.7
Table 2.7: Skill 6.0—Applied Math Reasoning	2.7
Table 2.8: Applied Mathematics—External Subject Matter Experts	2.13
Table 3.1: Applied Math Skills Item Distribution by Level	3.3
Table 3.2: Basic Operations—Subskill Item Distribution	3.4
Table 3.3: Fractions—Subskill Item Distribution	3.4
Table 3.4: Percentages/Ratios/Proportions—Subskill Item Distribution	3.5
Table 3.5: Unit Conversions—Subskill Item Distribution	3.6
Table 3.6: Geometric Measurement—Subskill Item Distribution	3.7
Table 3.7: Applied Mathematical Reasoning—Subskill Item Distribution	3.8
Table 3.8: Number of Items per Level for Applied Math Applications	3.9
Table 4.1: Responsibilities of the Test Coordinator	4.4
Table 5.1: NCRC Accessibility Supports Permissible by Assessment—Paper and Online Testing	5.8
Paper Testing 2017	5.8
Computer Testing June 2017	5.10
Table 7.1: Applied Math Reports and Their Function	7.3
Table 8.1: Summary of Unrounded and Rounded Scale Score	8.6
Table 8.2: Median Cut Scores for Applied Math Assessment	8.8
Table 9.1: Sample Demographic Information for the Two Delivery Modes	9.4
Table 9.2: Test Summary Statistics for Applied Math	9.5
Table 9.3: Summary for Raw and Scale Scores for the Two Delivery Modes	9.7
Table 9.4: Summary for Total Testing Time (in minutes)—Applied Mathematics and Applied Math	9.10
Table 9.5: Test Summary Statistics for Applied Math and Applied Mathematics	9.11
Table 9.6: Scale Scores Summary Statistics for Applied Math and Applied Mathematics	9.11
Table 9.7: Summary Statistics of Scale Scores Before and After Concordance	9.13
Table 9.8: Summary for Level Scores Before and After Concordance	9.13

Table 10.1: Coefficient Alphas and SEMs for Applied Math Form M2C_S1	10.2
Table 10.2 Estimated Variance Components, Error Variances, and Generalizability Coefficients at Each Level for Applied Math Form M2C_S1	10.3
Table 10.3: Estimated Classification Consistency Indices for Level Scores for Form M2C_S1	10.4
Table 11.1: Comparison of WorkKeys Test Population and Field Test Samples by Student/Adult, Gender, and Ethnicity	11.8
Table 11.2: Summary of Eigenvalues and Factor Difference Ratio Index (FDRI)	11.11
Table 11.3: Correlations between Scores on the WorkKeys Applied Mathematics Assessment and Different Outcomes	11.17
Table 12.1: Differential Item Functioning Evaluations—Group Comparisons	12.4
Table 12.2: WorkKeys DIF Classification Rules	12.4
Table 12.3: Applied Math—Number and Percent of Field Test Participants by Demographic Group	12.6
Table 12.4: Identifications of C-Level DIF items on the two Applied Math Forms	12.6
Table 12.5: Comparing the Requirements of the <i>Uniform Guidelines</i> to the ACT WorkKeys Job Profiling Procedure	12.8

List of Figures

Figure 5.1: Accessibility Feature Mapping Process	5.2
Figure 5.2: Architectural Structure of Accessibility Supports	5.4
Figure 8.1: Raw Score Distribution for the AM Scaling Study Form (Form M2C_S1)	8.3
Figure 8.2: Item p-values and <i>b</i> -parameter estimates by Item Levels for Form M2C_S1	8.4
Figure 8.3: Test Characteristics Curve (left) and Test Information Function (right)	8.4
Figure 8.4: CSEM for Raw Scores (left) and Scale Scores (right)	8.6
Figure 8.5: Relative Frequency Distribution (left) and Cumulative Frequency Distribution (right)	8.6
Figure 9.1: Comparison of Item Omit Rates for the Two Delivery Modes	9.4
Figure 9.2: Scatterplots of Item p-values (left) and IRT <i>b</i> -parameter estimates (right) for the Two Delivery Modes	9.5
Figure 9.3: Comparisons of Test Characteristic Curves (left) and Test Information Functions (right) for the Two Delivery Modes	9.6
Figure 9.4: Comparisons of Unrounded (left) and Reported (right) Raw-to-Scale Score Conversions for the Two Delivery Modes	9.6
Figure 9.5: Comparisons of CSEMs for Raw Scores (left) and Scale Scores (right) for the Two Delivery Modes	9.7
Figure 9.6: Comparison of Raw Score Distributions for the Two Delivery Modes	9.8
Figure 9.7: Comparison of Scale Score Distributions for the Two Delivery Modes	9.8
Figure 9.8: Comparison of Item Omit Rates Between Applied Mathematics and Applied Math	9.10
Figure 9.9: Comparison of Relative (left) and Cumulative (right) Frequency Distribution for Applied Mathematics and Applied Math	9.12
Figure 11.1: Applied Math—Eigenvalue Scree Plot	11.11
Figure 11.2: Job Profile Process Designed to Align Job Tasks to Skill Levels	11.15
Figure 13.1: Summary of Work and Career Readiness	13.3

Chapter 1

Applied Math Assessment—Overview

1.1 WorkKeys and the Applied Math Assessment

ACT WorkKeys[®] is a job skills assessment system that helps employers select, hire, train, develop, and retain a high-performance workforce. It also assists workers in better understanding their foundational skill levels and may assist them in finding employment or training. The assessments measure foundational domains that are required for success in a wide variety of current jobs.

The WorkKeys cognitive assessments are criterion-referenced assessments. Unlike the more commonly used norm-referenced assessments, WorkKeys test scores are not determined by the relationship of an examinee's score to other examinees within a norm group. In WorkKeys, examinees are measured in terms of their ability to demonstrate competency in identified skill sets. As a result, an individual's scores indicate the skills an examinee demonstrates in a given area or areas.

WorkKeys Applied Math is a multiple-choice assessment designed to measure the extent to which individuals can use the mathematical skills needed in workplaces, where the ability to think problems through to find and evaluate solutions is important. The assessment measures skills that individuals use when they apply mathematical reasoning and problem-solving to work-related problems.

1.2 The Workplace Skills Gap and the WorkKeys Solution

Employers have long relied on America's schools to educate the workforce of the future. During the past few decades, traditional credentials such as a high school diploma or a four-year college degree no longer assure employers that a worker has the required skills to participate in the fast-paced, high-performing workplace. Increasingly, employers find that workers often have serious gaps in many of the personal and foundational skills needed for success. As business and industry processes and practices become progressively more complex, they perceive that workers' skill levels have improved little in both

behavioral skills (e.g., collaboration, conscientiousness, and timeliness) and foundational skills (e.g., reading, writing, mathematics, and critical thinking).

Over the past 25 years, requirements have changed for nearly all jobs in the developed economies, resulting in drastic changes in worker skill requirements. Work environments are technology-centered, problems are often poorly defined, people work in teams to deal with these problems, and employers seek innovative answers. These new ways of working require a different set of job skills from those found in the manufacturing/industrial economy. Autor, Levy, and Murnane (2003) analyzed job tasks, categorizing them as manual, routine, or abstract. From 1960 to 2002, they found that the percentage of abstract tasks performed in the workplace increased by approximately 25%, while the percentage of manual and routine tasks decreased by nearly 10%. Clearly, 21st-century workers must deal with a technology and information-rich work environment, where abstract thinking is a requirement, and fewer and fewer tasks require either manual labor or routine operations (Autor et al., 2003; Griffin, Care, & McGaw, 2012).

Economic and workforce leaders debate the significance of the skills gap and its influence on economic growth (Bessen, 2014; Cappelli, 2012; Krugman, 2014). The skills gap is a term used to describe a problem that employers and hiring managers frequently face. The skills gap occurs because many well-paying jobs exist; but, due to the shortage of qualified workers, employers are unable to find qualified workers to fill them. From the workers' perspective, the skills gap means that many willing workers are unable to find employment because they lack the required skills. From a business perspective, it means that jobs are not filled resulting in lost opportunities and unrealized economic gains. From an overall economic perspective, it means that unemployment is unacceptably high and that economic growth is stagnant or fails to reach its full potential.

ManpowerGroup[®] (2015) surveyed 41,700 global employers and found that 38% of employers state they experience problems finding qualified workers. Thirty-two percent of U.S. employers reported experiencing problems finding qualified workers. Goldin and Katz (2008) provide evidence demonstrating that, since 1970, educational achievement in the United States has increased only marginally while technological advances and job requirements have greatly increased. They analyze the race between education and technology, and conclude that many of the economic trends that have developed over the past 30 years are a result of educational advances not keeping up with the advances in technology and worker demands. As a result, a discrepancy exists between employer expectations and the skill sets many workers have (Autor, 2015; Goldin & Katz, 2008).

Such perceived gaps in job skills reflect a dynamic redrawing of America's demographic profile. The fastest growing demographic groups in the United States are the least educated (Kirsch, Braun, Yamamoto, & Sum, 2007). Changes in the nation's demographic profile will present challenges to both the educational system and employers seeking highly skilled workers. These challenges require new approaches to both schooling and hiring practices. Paradoxically, these challenges coincide with the growth of a knowledge-based economy in which most job growth will be in areas that require some postsecondary education or training (Carnevale & Desrochers, 2003).

ACT created the WorkKeys system to address the discrepancy between foundational skill levels and job requirements. Because of the discrepancy, the WorkKeys system provides a solution that is beneficial to both employers and workers. WorkKeys assessments provide both employers and test takers clear, evidence-based, objective information about job skills. WorkKeys job profiling services provide employers with clear information regarding the foundational skill demands required for success in specific jobs. The

ACT KeyTrain® online curriculum program provides workers with the opportunity to improve their skills and achieve the required levels to qualify for jobs. The WorkKeys system provides opportunities for employers to hire the right person for the job, and it provides workers with the opportunity to qualify and demonstrate that they possess the foundational skills required for success.

1.3 Mathematics in the Classroom and the Workplace

To help delineate the construct of Applied Math, ACT reviewed relevant literature on numeracy skills and their application to the workplace. Although classroom instruction in mathematics overlaps in important areas with workplace mathematical applications, it does not account for many workplace uses. A growing body of research has documented the differences between mathematical reasoning as it is taught in the classroom versus how it is applied in the workplace. As emphasized below, these studies and evaluations indicate that the successful application of mathematics in the workplace is situational, incorporates problem solving, and integrates various mathematical and quantitative reasoning skills (Australian Association of Mathematics Teachers Inc., 2014; Smith, 1999).

1.3.1 Workplace Math

Changes in workplace technology over the last half century, both large and unpredictable, have been rapidly absorbed and adopted. In the 1970s, the first desktop calculators cost hundreds of dollars and typically performed only the four basic arithmetic operations. Today, hand-held graphing calculators selling for under \$100 have more capabilities than early mainframe computers. Such developments imply necessary changes in the mathematics skills needed on the job. Where employees used to perform calculations by hand and check the results for accuracy and reasonableness, they now use calculators or spreadsheets from the outset. To be successful on the job, employees need

- problem-solving strategies to set up and run the calculations best suited to answer their needs, and
- sufficient estimation skills to be able to recognize when results are highly unlikely, or to determine that incorrect data may have been entered.

Unlike mathematical problems presented in classrooms, workplace problems are seldom clearly defined. In the classroom, mathematical problems are often structured by a textbook and are taught somewhat in isolation. Although classroom mathematical skills tend to progress and build on one another, the student normally is solving mathematical problems as defined by the specific unit.

In applying mathematical skills to workplace problems, employees must utilize their understanding of mathematics and quantitative reasoning to derive the process or procedure for solving the problem. An employee may have a boss or co-worker who will help him or her set up and solve the problem; but in many circumstances, the employee will be expected to set up and solve the problem without assistance. In other cases, besides setting up and solving the problem, the employee will need to determine what data is relevant and pertinent to solving the problem. Although the mathematical skills observed in the workplace may appear to be fundamental, it is the application of the skills to the workplace problem that is not straightforward.

To be successful with applying math in the workplace, workers need to be able to blend the following:

- Apply and integrate mathematical concepts, procedures, and skills
- Understand the types of practical tasks that require mathematical solutions
- Identify the strategic mathematical process required to solve the specified problems
- Identify pertinent or relevant information or data for use in solving the problem

Each step in solving a workplace Applied Math problem—from defining the problem through evaluating the results—requires a comprehensive understanding of mathematics.

Another critical difference between the classroom and the workplace is the motivation or purpose for using mathematics. In the classroom, the purpose is often to solve an isolated problem or set of problems. In the workplace, context provides the purpose for doing the work and a practical need to know the result exists. Finding the best solution in the workplace can be the difference between an effective and efficient operation or one filled with problems, mistakes, and lost opportunities. Mathematical problem solving is often intertwined with other issues, where the mathematical result is linked to business success.

Though people may believe they do not use math often, if at all, in their jobs, mathematics is often hidden in tasks as basic as recording hours on a timesheet, compiling an expense report, counting out change to a customer, or taking a patient’s pulse. Mathematics skills and concepts typically used at work include basic arithmetic operations, spatial reasoning, and converting between units of measurement (Nicol, 2002). In some cases, all that is needed is the ability to total a column of numbers; but, in other cases, the ability to analyze data, to move beyond computation to recursive thinking, multiplicative thinking, abstraction, and spatial visualization is essential (Nicol, 2002).

The modern office worker must use technology to solve problems. In this context, mathematics is both more concrete and more intuitive. The need for mathematical literacy and quantitative reasoning skills requires workers to be able to work through multiple-step problems and solve three-dimensional problems using two-dimensional data and elementary data analysis .

Frank Levy and Richard J. Murnane (2004), in their book *The New Division of Labor: How Computers are Creating the Next Job Market*, believe that the increasing use of computers:

. . . has made people into consumers of mathematics. A clothing manager uses a quantitative model to forecast dress demand. A truck dispatcher uses a mathematical algorithm to design delivery routes. A bakery worker monitors production using digital readouts rather than the smell of bread. Employees of all kinds are expected to use web-based tools to help manage their retirement plans. Each of these tasks involves some aspect of mathematical literacy. In most cases, a computerized tool does the actual calculation, but using the model without understanding the math leaves one vulnerable to potential serious misjudgments (p. 104).

While classroom mathematics may isolate skills and focus on one type of problem at a time, workplace problems may require the application of several different skills to develop a solution. For example, individuals in the workplace may need to know how to select relevant data from a large amount of available information or to recognize that the data are presented in a different metric than the solution requires.

In ACT’s National Curriculum Survey, the skills identified as important to postsecondary mathematics teachers are those stressed by the National Council of Teachers of Mathematics. These same skills are

also valued in the workplace. However, while students may learn what to do in school, they will need to be able to transfer that knowledge to workplace contexts. The educational efforts of the Council and others are striving to close gaps between the skills learned in school and the skills used at work. The WorkKeys Applied Math assessment provides a standardized method for measuring a person's ability to apply the skills they acquired in the classroom to workplace situations.

1.4 WorkKeys Applied Math— Assessment Claims

The three Applied Math claims align to workforce development issues including improving worker access to better jobs, improving worker productivity, and reducing employee turnover rates. The Applied Math assessment was designed to measure specific skills as one part of a suite of assessments that assess (a) work and career readiness for high school students as a part of state accountability programs, (b) work and career readiness indicators for adults seeking state unemployment services, and (c) job placement to assist businesses in identifying individuals who had the foundational skills needed to succeed.

ACT has defined the following three claims regarding Applied Math score interpretation and usage.

Claim #1: U.S. examinees of high school or workforce age who demonstrate scores that reach at least a given level on the Applied Math assessment are more likely to successfully perform in more and higher levels of U.S. jobs (in the ACT job taxonomy) than examinees whose scores do not reach that level.

Claim #2: U.S. companies who hire U.S. examinees of high school or workforce age who demonstrate scores that reach at least a given level on the Applied Math assessment are more likely to achieve greater gains in productivity (for example, measured as increased output per day) from new employees than if the company had hired examinees whose scores do not reach that level.

Claim #3: U.S. companies who hire U.S. examinees of high school or work force age who demonstrate Applied Math scores that reach at least a given level are more likely to reduce turnover (retain those examinees for at least 6 months) than if the companies had hired examinees whose scores do not reach that level.

Note. For further elaboration on the Applied Math assessment claims, including the assumptions associated with each claim, see Chapter 11—Validity.

1.5 Test Users and Stakeholders

The critical stakeholders and intended test users are business employers, regional workforce development offices, schools that use the assessment as a measure of workforce readiness, and states or regions committed to developing their workforce. They are the individuals and groups who are invested in finding the right people for the right jobs.

Examinees. Individuals who take the Applied Math assessment are students and workers interested in demonstrating their foundational skill level in order to qualify as career ready, receive specific skill-related training, or qualify for a specific job. The examinee group includes individuals from high school age through the adult working lifetime. High school students take the assessment to gain an understanding of their level of career readiness in applied math and/or as a part of state accountability programs. Community college students take the assessment to demonstrate that they possess foundational skills and are ready to move forward for advanced training. College graduates take the assessment to demonstrate their level of career readiness as a means of separating themselves from other graduates. Working adults take the assessment to either qualify for a job or to demonstrate that they have the foundational skills needed for promotion or advanced training. In short, the examinee group includes high school students and adults who are either seeking employment or looking to advance in their field.

Stakeholders. Stakeholder groups include high schools and local school districts, state departments of education, community colleges, state and local workforce development departments, and employers.

High schools and local school districts administer the WorkKeys assessments in order to evaluate whether their curricular programs are enabling students to become career ready. In doing this, they are also providing their students the opportunity to earn a career ready certificate. State departments of education use the WorkKeys assessments as an accountability measure for evaluating the effectiveness of high schools and school districts in assisting their students to become career ready.

More specifically, the WorkKeys Applied Math assessment provides high schools and school districts with student data regarding the extent to which students have mastered the K to 12 mathematics curriculum and also can apply these skills to actual workplace situations. The application of mathematics skills to workplace scenarios differentiates the Applied Math assessment from other standardized mathematics assessments. The assessment provides students the opportunity to demonstrate their mastery of applied mathematics along with the application of these skills to real-world problems.

Community colleges utilize the WorkKeys assessments in a variety of ways. Many community colleges use the WorkKeys program as part of the process for determining acceptance into Career and Technical Education programs. Other community colleges use the assessments for program evaluation. Additionally, community colleges may use the assessments as a means of assisting their graduates in obtaining employment.

The WorkKeys Applied Math assessment has the flexibility to assist community colleges to improve their programs in different ways. It can assist a program in identifying students who have the foundational applied math skills required to successfully complete a specific program of study. In this way, it assists a program in achieving higher completion rates. In other cases, it can be used as a means of program evaluation allowing teachers to evaluate the extent to which students have mastered foundational skills. Lastly, because it is recognized by thousands of employers, it can help graduating students obtain employment.

State and local workforce development offices utilize the assessments as a means of assisting unemployed or underemployed individuals in finding employment or better opportunities. The assessment provides a means for the workforce development office personnel to better understand the skill levels of individuals and to provide better guidance and assistance to them in finding employment.

Employers may use the assessments, when coupled with a job profile analysis, to assist them in screening job applicants and finding sufficiently-qualified employees. A WorkKeys Job Profile allows the employer to understand the level of skill needed by a newly hired employee to successfully meet job expectations. Following the profile process, the employer may have job applicants take the appropriate WorkKeys assessments and then use their test scores as an additional piece of information to determine which candidates to interview.

1.6 Alignment to ACT's Holistic Framework

Building on research conducted over the last 50 years, ACT has developed its Holistic Framework (Camara, O'Connor, Mattern, & Hanson, 2015), which provides a more complete description of college and career readiness. The framework is organized into four broad domains: core academic skills, cross-cutting capabilities, behavioral skills, and education and career navigation skills.

1. Core academic skills include the domain-specific knowledge and skills necessary to perform essential tasks in the core academic content areas of English language arts, mathematics, and science.
2. Cross-cutting capabilities include the general knowledge and skills necessary to perform essential tasks across academic content areas. This includes technology and information literacy, collaborative problem solving, thinking and metacognition, and studying and learning.
3. Behavioral skills include interpersonal, self-regulatory, and task-related behaviors important for adaptation to and successful performance in education and workplace settings.
4. Education and career navigation skills include the personal characteristics, processes, and knowledge that influence individuals as they navigate their educational and career paths (e.g., make informed, personally relevant decisions; develop actionable, achievable plans).

The WorkKeys Applied Math assessment draws on skills defined as part of the core academic skills and skills defined as a part of cross-cutting capabilities. The skills constituting the Applied Math assessment align broadly with the skills defined within the mathematics section of core academic skills. At the same time, because test takers are applying mathematical skills in various ways to make decisions, the assessment construct overlaps with cross-cutting capabilities.

The cross-cutting capabilities that align to the WorkKeys Applied Math skills include troubleshooting (finding and/or correcting errors), and finding an optimal solution from among two or more options (including identifying the correct equation). These skills align to the Thinking and Metacognition capabilities within the Holistic Framework including critical thinking, problem-solving, decision making, computational thinking, and metacognition. Based on several workplace competency models, these skills are all identified as critical for work readiness skills (Institute for the Future, 2011; National Network of Business and Industry Associations [NNBIA], 2014).

Chapter 2

Test Development

2.1 Applied Math—Overview

WorkKeys[®] Applied Math is designed to assess the extent to which individuals can use mathematical skills needed in workplaces. The ability to think problems through to find and evaluate solutions is critical for workplace success (Australian Association of Mathematics Teachers Inc., 2014; Smith, 1999). The Applied Math assessment measures skills that individuals use when they apply mathematical reasoning and problem-solving to work-related problems.

To ensure that the Applied Math assessment would measure useful and relevant skills, a team composed of individuals from within ACT including Test Development Content, Measurement and Research, Industrial/Organizational Psychology, and Assessment Design was established to design the specifications for the Applied Math assessment. The team pooled resources to define the Applied Math construct, test specifications, and develop item prototypes. The design team's work was reviewed by external Subject Matter Experts (SMEs) who also provided feedback and recommendations, which were incorporated by the team.¹

Through a review of the pertinent empirical and professional literature and thorough deliberations among team members, the team determined that the applied math construct was defined through a combination of the test item characteristics and the mathematics skill elicited by the item. (This conclusion was a modification of the current Applied Math definition that defined the construct as an interaction of mathematics skills, applications, and level of complexity.) For example, a Level 5 item must meet the content criteria (identified in Table 2.1) and assess a mathematics skill identified as a Level 5 skill (see Tables 2.2 through 2.7). Both the item/stem characteristics and the mathematics skills were aligned to a level of difficulty for the assessment.

2.2 Applied Math Domain

The design team carefully reviewed information and research assessing the uses of workplace applied mathematical skills. Through multiple discussions and reviews the team decided that six general applied

mathematics skills constituted the domain. Each of the six skills was further defined into a set of subskills within the skill domain.

The six general applied mathematics skills are:

- Basic Operations Including Decimals
- Fractions
- Percentages/Ratios/Proportions
- Unit Conversions
- Geometric Measurement
- Applied Math Reasoning

More information regarding these dimensions is provided throughout Chapter 2. Tables 2.2 through 2.7 provide the subskills defined within each skill.

2.3 Revisions to Applied Math Domain as a Result of Review

Consultation with SMEs revealed technology (particularly spreadsheets, calculators, and scanning devices) removed many of the computational demands from the workplace. Despite these advanced tools, employees still needed mathematical and quantitative reasoning skills. For example, employees utilize spreadsheets to do calculations, but they must be capable of troubleshooting and finding errors in cells that are automatically calculated. Furthermore, in production situations, employees need to be able to understand and interpret measures of central tendency, spread, and tolerances, particularly as they relate to quality control. Given the evaluation and feedback, the following skills were included in the revised Applied Math assessment.

- Troubleshooting was expanded to include identifying whether an error occurred. In these cases, examinees must identify where values are incorrect.
- Basic statistical concepts were expanded beyond calculating means and medians to include interpreting measures of central tendency and dispersion (variability). Examinees might be asked to interpret or make a decision based on statistical values, but they are not required to calculate the values. Interpreting these values are considered within the construct of the Applied Math assessment; calculating measures of dispersion are considered outside of the construct.
- Identify the correct equation was added to assess examinees' skill in creating and comprehending equations used to produce automated calculations.

2.4 Applied Math—Item Stem Characteristics

The Applied Math assessment team found that the successful application of mathematics in a workplace situation incorporates problem solving and integrates mathematical and quantitative reasoning skills

(Australian Association of Mathematics Teachers Inc., 2014; Smith, 1999). While the proliferation of spreadsheets and calculators in the workplace has reduced the need for computational skills, employees still need to be able to apply quantitative reasoning skills to solve complex problems. Item levels are determined by the situational and problem solving complexity along with the mathematical skill and reasoning required.

Because the Applied Math assessment presents realistic workplace problems, each item is defined, in part, by its context. To assist in creating realistic workplace problems, each test item is presented in the context of money, time, measurement, or quantity.

Additionally, WorkKeys defines Applied Math items as having varying degrees of complexity. The complexity of each item is determined by the following dimensions:

- Presentation of quantitative information (Is the quantitative information presented in the order required to set up the problem?)
- Amount of language that must be understood to translate it into a mathematics problem
- Whether extraneous information is included
- Whether the item contains a graph
- Whether solving the problem requires multiple steps

The design team developed Table 2.1 to provide guidelines on how item complexity influences item level.

Table 2.1: Item Stem Characteristics by Level

Item Stem Characteristics	Level 3	Level 4	Level 5	Level 6	Level 7
Presentation of Quantitative Information	Presented in logical order	May not be in logical order	May not be in logical order	May not be in logical order	May have incomplete information or require an assumption
Amount of Language to Translate to Math Expression	Minimal	Some	Some	Considerable translation	May have unusual format
Extraneous Information	None	May have some extraneous information	May have some extraneous information	May have some extraneous information	May have some extraneous information
Contains Simple Graph	No	May be included	May be included	May be included	May be included
Set up/ Planning	Minimum set-up	Some set-up required	May require complicated set-up	May require complicated set-up	May require complicated set-up
Calculations	One operation	One or two operations	May have several operations	May have several operations	May have several operations
Solving for Unknowns	Solve for one unknown	Solve for one or two unknowns	May solve for one unknown and then use to solve the problem to answer the question	May solve for one unknown and then use to solve the problem to answer the question	May solve for one unknown and then use to solve the problem to answer the question

Using this table: The table is intended as a guide describing the general characteristics of the item/stem for each given Level.

2.5 WorkKeys Applied Math—Skill Definitions

The Applied Math assessment strives to measure the most relevant and consequential foundational mathematical skills that are widely used in the workplace. To determine these skills, the design team drew upon information from the ACT JobPro® Database, professional literature, and feedback from external SMEs.

The Applied Math domain was defined through six critical skills. Each of the six skills was divided into subskills. The skill and subskill definitions collectively constitute the workplace applied math construct. Tables 2.2 through 2.7 provide the subskills that constitute each Applied Math skill.

Table 2.2: Skill 1.0—Basic Operations with Numbers Including Decimals

1.0	Basic Operations with Numbers Including Decimals
	Subskills:
1.1	Add positive numbers
1.2	Add with negative number(s)
1.2.1	Add more than four numbers, some of which may be negative
1.2.2	Add two negative numbers
1.3	Subtract positive numbers
1.3.1	Subtract positive numbers where the result is positive
1.3.2	Subtract positive numbers where the result is negative
1.4	Subtract with negative number(s)
1.4.1	Positive minus negative
1.4.2	Negative minus positive
1.4.3	Negative minus negative
1.5	Multiply positive numbers
1.6	Divide positive numbers (result could be a fraction)
1.7	Two or more basic operations

Table 2.3: Skill 2.0—Fractions

2.0	Fractions
	Subskills:
2.1	Add/Subtract fractions
2.1.1	Add/Subtract fractions (limited to halves and fourths). No more than two fractions
2.1.2	Add/Subtract fractions that share a common denominator (such as $1/8 + 3/8 + 7/8$)
2.1.3	Add/Subtract fractions with unlike denominators
2.2	Multiply fractions
2.2.1	Multiply fractions (none are mixed numbers)
2.2.2	Multiply a mixed number (such as $12 \frac{1}{8}$) by a whole number or a decimal
2.2.3	Multiply more than 1 mixed number
2.3	Divide fractions
2.4	Change between fractions and decimals

Table 2.4: Skill 3.0—Percentages/Ratios/Proportions

3.0	Percentages/Ratios/Proportions
	Subskills:
3.1	Convert between decimals and percentages
3.2	Calculate a given percentage of a given number; (e.g., what is 4% of 10? Tax, commission, discount, markup, raise)
3.3	Calculate the percentage one number is of another. (e.g., 6 is what percentage of 15?)
3.4	Calculate percent change
3.5	Calculate reverse percent (e.g., you have discounted a coat by 15% and now the sales price is \$30; what was the original price?)
3.6	Set up and/or manipulate Simple Ratio/Proportions/Rates
3.6.1	Figure out simple ratios
3.6.2	Figure out simple proportions
3.6.3	Figure out simple rates (such as 10 mph)
3.7	Set up and/or manipulate ratios, rates, or proportions (at least one of the quantities related is a fraction)
3.8	Rates, production rates, rate x time (e.g., 15 cups over 40 mins = x cups per minute; at 59 units per hour, how many made in 8 hours?)

Table 2.5: Skill 4.0—Unit Conversions

4.0	Unit Conversions
	Subskills:
4.1	Convert between familiar units (between: hours and minutes, dollars and cents)
4.2	Convert where the conversion factor is given in the problem
4.3	Convert where you must select the conversion factor (e.g., from the formula sheet)
4.4	Two or more step conversions (e.g., inches to feet to yards, kilometers to meters to feet)
4.5	Two or more separate conversions (e.g., problem that has minutes to hours and pounds to ounces)
4.6	Operations with mixed units (e.g., add 6 feet 4 inches and 3 feet 8 inches, 3.5 hours + 4 hours 30 minutes, etc.)
4.7	Convert the unit of measurement using fractions, mixed numbers, decimals, or percentages

Table 2.6: Skill 5.0—Geometric Measurement

5.0	Geometric Measurement
	Subskills:
5.1	Calculate perimeter or circumference
5.2	Calculate area
5.2.1	Find the area of one rectangle with dimensions given
5.2.2	Find the area of other polygons with dimensions given
5.2.3	Find the area of a circle given radius or diameter
5.2.4	Find the area of multiple shapes
5.2.5	Find the area of a composite shape
5.2.6	Find the area when it may be necessary to rearrange the formula, convert units of measurement in the calculations, or use the result in further calculations
5.3	Calculate volume
5.3.1	Calculate volume of a rectangular solid
5.3.2	Calculate volume of spheres, cylinders, and cones
5.3.3	Find the volume when it may be necessary to rearrange the formula, convert units of measurement in the calculations, or use the result in further calculations

Table 2.7: Skill 6.0—Applied Math Reasoning

6.0	Applied Math Reasoning
	Subskills:
6.1	Troubleshooting
6.1.1	Identify where a mistake occurred (e.g., in the spreadsheet, identify the row where the problem occurred)
6.1.2	Identify the reason for the mistake
6.2	Best Deal
6.2.1	Find the best deal using one- or two-step calculation that meets the stated conditions
6.2.2	Find the best deal from a group and then do something with the answer
6.2.3	Determine the better economic value of several alternatives by using graphics, or determining the percentage difference, or by determining unit cost
6.3	Basic Statistical Concepts
6.3.1	Calculate the average (mean)
6.3.2	Calculate the weighted average
6.3.3	Interpret measures of central tendency
6.3.4	Interpret measures of spread and tolerances
6.4	Identify the Correct Equation

2.6 WorkKeys Applied Math—Performance Level Descriptors

Individuals taking the assessment earn a scale score and a level score. Scale scores range from 65 to 90. The scale scores are transformed to level scores ranging from Level 3 to Level 7. Most examinees focus on their level scores because they have interpretability related to job skills. Consistent with the other WorkKeys NCRC assessments, Level 3 is defined as the lowest level at which an employer would be willing to hire and pay an employee to perform those skills in a job requiring applied mathematics. (An individual may perform poorly and receive a Level score of less than 3; in this case, the individual has not achieved a WorkKeys level.) Level 7 is defined as the highest skill level that an employee could be expected to hold without specialized formal training.

Applied Mathematics score levels are interpreted as a progression in that a test taker who holds skills at a specific level will be able to do the skills defined for each lower level. For example, a test taker who scores at Level 5 not only possesses the skills defined as Level 5 skills, but he or she also possesses the skills defined at Levels 3 and 4.

The following section identifies performance level descriptors for examinees who earn scores at each level.

Applied Math Level 3

Level 3 problems can easily be translated from a word problem to a math equation requiring a single type of math operation. All the needed information is presented in logical order and there is no extra information given. When test takers use Level 3 Applied Math skills, they are able to:

- Solve problems that require one type of mathematical operation. They add or subtract either positive or negative numbers (such as 10 or -2). They multiply or divide using only positive numbers (such as 10).
- Convert a familiar fraction (such as $\frac{1}{2}$ or $\frac{1}{4}$ to a decimal) and convert from a decimal to a common fraction; OR convert between decimals to percentages (such as 0.75 to 75%).
- Convert between familiar units of money and time (such as one hour equals 60 minutes or $\frac{1}{2}$ of a dollar equals \$0.50).
- Add the prices of several products together to find the total, and calculate the correct change for a customer.

Applied Math Level 4

In Level 4 problems, tasks may present information out of order and may include extra, unnecessary information. One or two operations may be needed to solve the problem. A chart, diagram, or graph may be included. When test takers use Level 4 Applied Math skills, they use the skills described at Level 3, and they also are able to:

- Solve problems that require one or two mathematical operations. They can add, subtract, or multiply using positive or negative numbers (such as 10 or -2), and they can divide positive numbers (such as 10).
- Calculate the average or mean of a set of numbers (such as $\frac{10+11+12}{3}$). For this, they may use whole numbers and decimals.
- Figure out simple ratios (such as $\frac{3}{4}$), simple proportions (such as 10/100 cases), or rates (such as 10 mph).
- Add commonly known fractions, decimals, or percentages (such as $\frac{1}{2}$, 0.75, or 25%).
- Add or subtract fractions with a common denominator (such as $\frac{1}{4} + \frac{3}{4} + \frac{1}{4}$).
- Multiply a mixed number (such as 12 $\frac{1}{8}$) by a whole number or a decimal.
- Put the information in the right order before they perform calculations.

Applied Math Level 5

In Level 5 problems, the information may not be presented in logical order; the item may contain extraneous information; it may contain a graph or diagram; and the mathematical set-up may be complicated. In solving, the test taker may need to perform multiple operations. (For example, at this level, examinees may complete an order form by totaling an order and then calculating sales tax.) When test takers use Level 5 Applied Math skills, they use the skills described at Levels 3 and 4, and they also are able to:

- Decide what information, calculations, or unit conversions to use to find the answer to a problem.
- Add and subtract fractions with unlike denominators (such as $\frac{1}{2} - \frac{1}{4}$).
- Convert units within or between systems of measurement (e.g., time, measurement, and quantity) where the conversion factor is given either in the problem or in the formula sheet.
- Solve problems that require mathematical operations using mixed units (such as adding 6 feet and 4 inches to 3 feet and 10 inches, or subtracting 4 hours and 30 minutes from 3.5 hours).
- Identify the best deal using one- or two-step calculations that meet the stated conditions.
- Calculate the perimeter or circumference of a basic shape or calculate the area of a basic shape
- Calculate a given percentage of a given number and then use that percentage to find the solution to a problem (e.g., find the percentage and then use it to find the discount, markup, or tax).
- Identify where a mistake occurred in a calculation (such as identifying the row in a spreadsheet where a problem occurred).

Applied Math Level 6

Level 6 problems may require considerable translation from verbal form to mathematical expression. They generally require considerable setup and involve multiple-step calculations. When test takers use Level 6 Applied Mathematics skills, they use the skills described at Levels 3, 4, and 5, and they also are able to:

- Use fractions with unlike denominators and calculate reverse percentages.
- Convert units within or between systems of measurement (e.g., time, measurement, and quantity) where multiple-step conversions are required and the formulas are provided such as converting from kilometers to meters to feet.
- Identify why a mistake occurred in a solution.
- Find the best deal from a group of solutions and then use the result for another calculation.
- Find the area of basic shapes when it may be necessary to rearrange a formula, convert units of measurement in the calculations, or use the result in further calculations.
- Calculate the volume of rectangular solids (e.g., cubes)
- Calculate rates, productions rates, rate by time (such as, production rate is 59 cups produced per hour, how many will be produced in an 8 hour shift).
- Identify the correct equation for solving a problem.

Applied Math Level 7

Level 7 problems may be presented in an unusual format and information presented may be incomplete or require the test taker to make an assumption. Problems often involve multiple steps of logic and calculation. When test takers use Level 7 Applied Math skills, they use the skills described at Levels 3, 4, 5, and 6, and they also are able to:

- Solve problems that include ratios, rates, or proportions where at least one of the quantities is a fraction.
- Identify the reason for a mistake.
- Convert between units of measurement using fractions, mixed numbers, decimals, and percentages.
- Calculate volumes of spheres, cylinders, or cones.
- Calculate the volume when it may be necessary to rearrange the formula, convert units of measurement in calculations, or use the result in further calculations.
- Set up and manipulate ratios, rates, or proportions where at least one of the quantities is a fraction.
- Determine the better economic value of several alternatives by using graphics, or determining the percentage difference, or by determining unit cost.
- Apply basic statistical concepts. For example, calculate the weighted mean, interpret measures of central tendency, or interpret measure of spread and tolerance.

2.7 Designing Items to Elicit Evidence of Applied Math

Applied Math uses multiple-choice items to measure examinees' proficiency in various mathematical skills necessary for workplace success. The domain of mathematical skills measured by the assessment was defined by the design team and confirmed by external SMEs with backgrounds in business, industry, and education (see Table 2.8). To properly elicit evidence of the skills in the Applied Mathematics domain, ACT follows an item-design model aligned with both evidence-centered assessment design (Mislevy, Steinberg, & Almond, 1999) and the *Standards for Educational and Psychological Testing* (American Educational Research Association [AERA], American Psychological Association [APA], & National Council for Measurement in Education [NCME], 2014).

2.7.1 Item Writing

Item writers qualify to write for the Applied Math assessment by completing item-writing training modules. The modules cover numerous aspects of developing quality multiple-choice items including creating text that elicits evidence of the skill the item measures, writing effective distractors, employing realistic workplace contexts, and avoiding common item-writing errors. Once an item writer has successfully completed all required training modules, he or she is given an item-writing assignment that details the number of items to be developed at specific levels. The assignment may also include other item specifications such as Career Cluster alignment, the required level of stem complexity, the presence or absence of particular data displays, or other item-defining characteristics. What follow are other requirements that are universal to all Applied Math items:

- The context must be work-related and realistic, and the mathematics should be authentic to the work presented in the item.
- Prices, rates, and procedures in the item should be authentic and realistic for the next few years. Moreover, the source of the information regarding the prices, rates, and procedures should be documented.
- Avoid overlap with the Graphic Literacy assessment. That is to say, while graphics are allowed in an item, the mathematical skill must be the emphasis of the item rather than reading and interpreting the graphic.

2.7.2 Item Review

After items have been developed, edited, and tentatively finalized by the Content Assessment team, they are submitted to external consultants with backgrounds in workplace math assessment for review. They review the item in terms of

- the content, including concerns about whether the item is appropriately aligned to the construct;
- whether the context and the solution method are workplace relevant; and
- whether there is one, and only one, correct response.

The reviewer is also required to evaluate the item on the basis of fairness and cultural bias. The reviewer is asked to evaluate the item in terms of how members of different demographic groups would respond to the item. (ACT asks the item reviewer to evaluate the item from the perspective of men and women examinees, and from the perspective of African-American, Hispanic-American, and Asian-American examinees.) The reviewer is asked to comment on whether there is anything within the item that any group might find offensive. Also, the reviewer is to evaluate if each demographic group has equal access to, and opportunity to learn, the information and skills assessed.

For both the content and fairness reviews, item reviewers complete a questionnaire either approving the item as written or identifying specific concerns. The content team gathers the information from the reviewers and determines how to appropriately address any concerns. Items are not classified as ready for pretesting until after content specialists conclude that all relevant issues are resolved.

2.7.3 Item Pretesting

All Applied Math items are pretested before they become operational. Newly developed or recently revised items are embedded in current forms of the Applied Math assessment. As a result, examinees respond to the pretest items as a part of their responses to the operational assessment.

ACT conducts statistical analyses to determine if each pretest item meets required statistical criteria. ACT analyzes the items using both classical and item response theory (IRT) statistics to evaluate the psychometric properties. Items must meet criteria based on overall difficulty and discrimination. If the pretest item meets the statistical criteria, it has passed pretesting. If it fails to meet the criteria, the Applied Math content team reviews it and considers whether it should be edited, modified, or removed from the pool. When items are edited, the item receives a new item identifier and is pretested a second time.

To ensure item fairness, ACT compares item difficulty values based on group membership (item analysis is conducted comparing difficulty levels by gender and ethnic status) and performs Differential Item Functioning (DIF) evaluations. Items that are flagged through the DIF evaluations are sent to the Applied Math content team for review. The content team determines whether the flagged item should remain as it currently is, be revised and returned to pretesting, or be removed from the pool. (For detailed information on the evaluation of items for fairness, please refer to Chapter 12.)

Note

¹ Eleven external SMEs reviewed the Applied Mathematics test development documentation and provided feedback. The SMEs were provided notebooks that included information on the definition of workforce applied mathematics, description of the difference between mathematics in the classroom and mathematics in the workforce, cognitive skill domains and subdomains, sample items, and related questions. The SMEs reviewed the notebooks and then participated in small group two-hour interviews (between three and four SMEs participated in each interview). Following the interviews, the SMEs were asked to make comments and notes in their notebooks and return them to ACT. Based on this feedback, the design team made modifications to all related materials. The individuals who served as external SMEs are provided in the table below along with their affiliations.

Table 2.8: Applied Mathematics—External Subject Matter Experts

Name	Institution	Qualifications
Beverly Deal	S.B. Phillips	Workforce Readiness Director
Ana Gilbertson	Kirkwood Community College	Advanced Manufacturing Department Coordinator
Julia Holdridge	Sedgwick Industries	Director, Colleague Resources
Randy Lane	Eastman Chemical	ACT Job Profiler; Industrial Engineer
Chris Manheim	Manheim Solutions (Independent Consultant)	President and ACT Job Profiler
Scott Oppler	Society for Human Resource Management (SHRM) – VP of Psychometric and Test Development	Psychometrician; developed multiple assessments for certification and licensing programs
Wayne Rollins	Mid-East Commission of North Carolina	ACT Job Profiler; community college vocational-technical advisor
Priti Shah	University of Michigan	Professor of Cognition and Cognitive Neuroscience and Educational Psychology
Andrew Stull	University of California Santa Barbara	Scientist studying the cognitive and perceptual effects of concrete and virtual reality manipulatives
Charles Wayne	State of Pennsylvania Department of Education	State Assessment Programs; former middle school and high school math instructor
Eric Vincent	VIO Consulting (Independent Consultant)	Former ACT employee in I/O Psychology; currently working as independent consultant to business and industry in the Phoenix area

Chapter 3

Test Specifications

3.1 WorkKeys Applied Math Specifications—Overview

The purpose of the WorkKeys[®] assessment program is to assist workers, students, employers, and workforce development leaders by providing a system to measure and improve individuals' skills. Chapter 1 of the Technical Manual provided evidence demonstrating that the ability to solve applied mathematical problems was a foundational skill required for success in the modern economy.

In this chapter, the Applied Math test specifications are provided. An assessment's test specifications are developed by first developing the assessment's claims and score interpretations, followed by articulating the set of behaviors that need to be elicited through the test content to provide evidence in support of the claims. In articulating the set of behaviors, the team evaluated the degree to which examinee responses to the item content provided support for the assessment's claims and score interpretations. Item and test content must elicit examinee behaviors that are aligned to the Applied Math construct and that provide evidence supporting score interpretations (Kane, 2013; Messick, 1989).

The Applied Math team utilized a variety of reputable source materials to identify relevant content that should constitute a measure of workplace applied mathematics. Over the past 25 years, through its job profiling services, ACT has gathered information related to workplace quantitative problems and skill requirements from the manufacturing, health care, construction, transportation, financial, and sales sectors. The Applied Math team reviewed these findings and used the information to determine what types of applied math problems should be included and which skills were most frequently required. To further support content-related decisions, the team reviewed professional literature around workplace applied math (Australian Association of Mathematics Teachers Inc., 2014; Binkley et al., 2012; Smith, 1999) and workplace competency models (NNBIA, 2014). Lastly, the team consulted with a group of external Subject Matter Experts (SMEs) to obtain their perspective on workplace applied mathematics problems and skills. (See list of participating SMEs in the Chapter 2 Note.)

Based on the findings from the review of these resources, ACT formulated the Applied Math test specifications. Using the findings in conjunction with the assessment's purpose, claims, and score interpretations, the team defined the critical content facets and weighted the skills based on their importance and frequency.

3.2 Content Relevance and Representativeness

Test specifications must be carefully defined to ensure that the assessment tasks are construct relevant and representative of the domain purported to be measured (Messick, 1989; Mislevy et al., 1999).

In the context of Applied Math, construct relevance requires not only that the examinee demonstrate the ability to solve mathematical problems, but that he or she also demonstrates the ability to use the tools commonly found in the workplace for solving quantitative problems. Because WorkKeys assessments are designed to measure skills that are widely applicable to a large number of jobs, construct representativeness refers to a range of problems and the various mathematical skills needed in the workplace. To illustrate, the context of the mathematical problems must be applicable to the full range of job sectors, from manufacturing to construction to office work and beyond. The problems must also represent appropriate ranges of difficulty, from basic operations, to more complicated multi-step problems, to the use of quantitative reasoning.

A second purpose of the test specifications involves the development of alternate forms. The size of the WorkKeys test population combined with the need for security and fairness necessitates the construction of alternate forms of the Applied Math assessment. In developing alternate forms, ACT believes that all forms must meet Lord's (1980) equity property. Lord's equity property states, from the test taker's perspective, it must be a matter of score indifference whether he or she is administered Form A or Form B of an assessment. To achieve alternate forms that meet the equity property, the content representativeness of each form must be identical (Kolen & Brennan, 2014).

As a result, by carefully defining the test specifications, ACT accomplishes two critical assessment goals:

1. Content is construct relevant and representative.
2. Content representation is identical across alternate forms.

3.3 Applied Math—Test Blueprint

ACT developed detailed blueprints defining the content attributes of each test item. The content specifications were developed by clearly specifying the attributes of types of problems that workers need to solve. Using this information, the team identified six primary applied mathematical skills. Analyzing the data further, the team defined the subskills that existed within each of the primary skills. The team using the job profiling data weighted the criticality and frequency of use of each subskill (Allen & Yen, 2002). Doing this resulted in some subskills being removed. The weightings were then reviewed by the external SMEs, and based on the feedback, the team made final adjustments to the blueprint. Lastly, the team evaluated the problem context and set up a table recommending the problem context distribution.

The workplace Applied Math construct was based on three critical facets:

- Applied Mathematical Complexity Level
- Applied Mathematical Skills and Subskills
- Applied Mathematical Problem Context

The Applied Mathematical Complexity Level was divided into five levels and defined by the presentation of quantitative information, amount of language used to translate to math expression, amount of extraneous information, whether it contains a graphic, the planning and mathematical set-up, and the number of unknowns (see Table 2.1).

Applied mathematical skills were divided into six primary skills: basic operations with numbers including decimals, fractions, percentages/ratios/proportions, unit conversions, geometric measurement, and applied mathematics reasoning. Through analyzing the professional literature on applied mathematics and data from ACT’s job profiling, ACT learned that workplace applied mathematics is conducted using tools (e.g., calculators and spreadsheets). Ensuring that workers can effectively use these tools to apply their mathematical skills and find the correct solution thus becomes a critical component of the assessment.

Four critical contexts were identified as relevant to workplace applied mathematics: quantity, money, time, and measurement. The overwhelming majority of foundational applied mathematics workplace tasks involved one of these four contexts.

Tables 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, and 3.8 present the Applied Math test specifications. The test specifications provide a blueprint for form development and also represent the relative importance of the applied mathematics skills and subskills in the workplace.

Table 3.1: Applied Math Skills Item Distribution by Level

Domain	Number per Level					Total
	Level 3	Level 4	Level 5	Level 6	Level 7	
1.0 Basic Operations with Numbers Including Decimals	4	2	0	0	0	6
2.0 Fractions	1	2	1	0	0	4
3.0 Percentages/Ratios/Proportions	0	1	1	2	1	5
4.0 Unit Conversions	1	0	2	1	1	5
5.0 Geometric Measurement	0	0	1	1	1	3
6.0 Applied Mathematics Reasoning	0	1	2	2	3	8
Total Item Count	6	6	7	6	6	31

Table 3.2: Basic Operations—Subskill Item Distribution

1.0 Basic Operations with Numbers Including Decimals	Level 3	Level 4	Level 5	Level 6	Level 7	Total
1.1 Add positive numbers	1	0	0	0	0	1
OR						
1.2 Add negative numbers (includes 1.2.1 and 1.2.2)						
Subtract positive numbers (includes 1.3.1 and 1.3.2)	1	0	0	0	0	1
OR						
1.4 Subtract negative numbers (includes 1.4.1, 1.4.2, and 1.4.3)						
1.5 Multiply positive numbers	1	0	0	0	0	1
1.6 Divide positive numbers	1	0	0	0	0	1
1.7 Two or more basic operations	0	2	0	0	0	2
Total	4	2	0	0	0	6

Table 3.3: Fractions—Subskill Item Distribution

2.0 Fractions	Level 3	Level 4	Level 5	Level 6	Level 7	Total
2.1 Add/subtract fractions with a common denominator (includes 2.1.1 and 2.1.2)	0	1	0	0	0	1
2.1.3 Add/subtract fractions with unlike denominators	0	0	1	0	0	1
2.2.2 Multiply a mixed number (such as $12 \frac{1}{8}$) by a whole number	0	1	0	0	0	1
2.4 Change between fractions and decimals	1	0	0	0	0	1
OR						
3.1 Convert between decimals and percentages						
Total	1	2	1	0	0	4

Table 3.4: Percentages/Ratios/Proportions—Subskill Item Distribution

3.0 Percentages/Ratios/Proportions	Level 3	Level 4	Level 5	Level 6	Level 7	Total
3.2 Calculate a given percentage of a given number (e.g., what is 4% of 10? Tax, commission, discount, mark-up, raise) OR 3.3 Calculate the percentage one number is of another number	0	0	1	0	0	1
3.4 Calculate percent change OR 3.5 Calculate reverse percent	0	0	0	1	0	1
3.6 Set up and/or manipulate simple ratio/proportions/rates (includes 3.6.1, 3.6.2, and 3.6.3)	0	1	0	0	0	1
3.7 Set up and/or manipulate ratios, rates, or proportions (at least one of the quantities related to a fraction)	0	0	0	0	1	1
3.8 Rates, production rates, rate x time (e.g., 15 cups over 40 minutes = x cups per minute; at 59 units per hour, how many made in 8 hours?)	0	0	0	1	0	1
Total	0	1	1	2	1	5

Table 3.5: Unit Conversions—Subskill Item Distribution

4.0 Unit Conversions	Level 3	Level 4	Level 5	Level 6	Level 7	Total
4.1 Convert between familiar units (between: hours and minutes, dollars and cents)	1	0	0	0	0	1
4.2 Convert where the conversion factor is given in the problem OR	0	0	1	0	0	1
4.3 Convert where you must select the conversion factor (from the formula sheet)						
4.4 Two or more step conversions (e.g., feet to yards, kilometers to meters to feet) OR	0	0	0	1	0	1
4.5 Two or more separate conversions						
4.6 Operations with mixed units (e.g., add 6 feet and 4 inches to 3 feet and 8 inches, 3.5 hours + 4 hours and 30 minutes)	0	0	1	0	0	1
4.7 Convert the unit of measurement using fractions, mixed numbers, decimals, or percentages	0	0	0	0	1	1
Total	1	0	2	1	1	5

Table 3.6: Geometric Measurement—Subskill Item Distribution

5.0 Geometric Measurement	Level 3	Level 4	Level 5	Level 6	Level 7	Total
5.1 Calculate perimeter or circumference OR 5.2 Calculate area (includes 5.2.1, 5.2.2, or 5.2.3)	0	0	1	0	0	1
5.2 Find the area of basic shapes when it may be necessary to rearrange the formula, convert units of measurement in the calculations, or use the result in further calculations (5.2.6) OR 5.3 Calculate volume (5.3.1)	0	0	0	1	0	1
5.2.4 Find the area of multiple shapes OR 5.2.5 Find the area of a composite shape OR 5.3.2 Calculate volume of spheres, cylinders, and cones OR 5.3.3 Find the volume when it may be necessary to rearrange the formula, convert units of measurement in the calculations, or use the result in further calculations	0	0	0	0	1	1
Total	0	0	1	1	1	3

Table 3.7: Applied Mathematical Reasoning—Subskill Item Distribution

6.0 Applied Mathematical Reasoning	Level 3	Level 4	Level 5	Level 6	Level 7	Total
6.1.1 Identifying where a mistake occurred (e.g., identify the row in a spreadsheet where the problem occurred)	0	0	1	0	0	1
6.1.2 Identifying the reason for the mistake	0	0	0	1*	1*	1
6.2.1. Find the best deal using a one- or two-step calculation that meets the stated conditions	0	0	1	0	0	1
6.2.2. Find the best deal from a group and then do something with the answer	0	0	0	1*	0	1*
6.2.3. Determine the better economic value of several alternatives by using graphics, or determining the percentage difference, or by determining unit cost	0	0	0	0	1*	1*
6.3 Basic Statistical Concepts	0	0	0	0	1	1
6.3.2 Calculate the weighted mean OR						
6.3.3 Interpret measures of central tendency OR						
6.3.4 Interpret measures of spread and tolerances						
6.3.1 Calculate the average (mean)	0	1	0	0	0	1
6.4 Identify the correct equation	0	0	0	1	1	2
Total	0	1	2	2	3	8

* For 6.1 Troubleshooting and 6.2 Best Deal: if a form contains a Troubleshooting item at Level 6, then it must not have a Best Deal item at Level 6, but should include a Best Deal item at Level 7; if form contains a Best Deal item at Level 6, then it must not have a Troubleshooting item at Level 6, but should include a Troubleshooting item at Level 7.

Table 3.8: Number of Items per Level for Applied Math Applications

Application	Number per Level					Total
	Level 3	Level 4	Level 5	Level 6	Level 7	
Quantity (QUA)	0–4	0–4	0–4	0–4	0–4	4–9
Money (MON)	0–4	0–4	0–4	0–4	0–4	4–9
Time (TIM)	0–4	0–4	0–4	0–4	0–4	4–9
Measurement (MEA)	0–4	0–4	0–4	0–4	0–4	4–9
Total	6	6	7	6	6	31

Each form of the Applied Math assessment is built to conform to test specifications defined in Tables 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, and 3.8. ACT’s test development and psychometric staff members thoroughly review each form to ensure that it meets the specifications, and that each form is parallel in terms of content to all other Applied Math forms.

Chapter 4

Test Administration

The *ACT WorkKeys[®] Administration Manual—Paper Testing* and *ACT WorkKeys[®] Administration Manual—Online Testing* manuals contain the instructions for administering the ACT WorkKeys assessments. Staff members associated with approved sites are responsible for the secure administration of the WorkKeys assessments.

In addition to the testing manuals, ACT WorkKeys has additional resources available online.¹ (The online resources are available through the ACT website. See the Note at the end of the chapter for the link to the online resources.)

4.1 Policies and Procedures

The *ACT WorkKeys Administration Manual—Paper Testing* and *ACT WorkKeys Administration Manual—Online Testing* provide direction in the administration of the WorkKeys assessments including timing instructions. It is important that all staff involved in the administration of WorkKeys assessments follow the instructions as provided by ACT to appropriately measure the skills and abilities of the individuals completing the assessments.

4.1.1 Standardized Procedures

Included in the two manuals are detailed directions for securing materials and administering the assessments in a standardized manner. The following actions violate ACT policies and procedures for delivering WorkKeys assessments:

- accessing or obtaining a test booklet or test questions prior to the test for any reason (An exception is provided for American Sign Language and Signing Exact English interpreters assisting examinees)
- photocopying, making an electronic copy, or keeping a personal copy of the test or of any test items

- taking notes about test questions or any paraphrase of test questions to aid in preparing examinees for testing
- aiding or assisting an examinee with a response or answer to a secure test item, including providing formulas
- rephrasing test questions for examinees
- creating an answer key or “crib sheet” of answers to test questions
- editing or changing examinee answers after completion of the test, with or without the examinee’s permission
- allowing examinees to test in an unsupervised setting
- leaving test materials in an unsecured place or unattended
- failing to properly report and document incidents of prohibited behavior involving examinees, staff, or others
- allowing examinees to test longer than the permitted time
- failing to return and account for all testing materials after the testing session has ended

4.1.2 Selecting Testing Staff

Test Coordinators are responsible for selecting their testing staff. The Test Coordinator provides the continuity and administrative uniformity necessary to ensure that all examinees are tested under the same conditions, and to ensure the security of the test. Relatives and guardians of individuals taking the WorkKeys assessments are not allowed to participate in the delivery of WorkKeys assessments.

The school or organization should strive to ensure that all individuals administering the assessment are of sound ethical standing. Room supervisors and proctors may be current or retired faculty members, school administrative or clerical employees, substitute teachers, student teachers, or paraprofessionals.

The following individuals may *not* act as testing staff:

- High school examinees, volunteers, and lower-division undergraduates
- Anyone who intends to take ACT WorkKeys tests within the next 12 months
- Anyone involved in ACT WorkKeys test preparation activities at any time during the current testing year (September 1 through August 31), due to potential conflict of interest. (**Note:** ACT recognizes that the normal duties of a counselor or teacher may involve some responsibilities for test preparation. These activities are not a conflict of interest, provided they are part of job responsibilities specifically defined by one’s employer and the employer is not a commercial enterprise.)

In addition, if any relative or ward will test at your site or any school in the state during the testing window:

- You *may not* serve as Test Coordinator for the administration of any of the tests. You must delegate all supervisory responsibilities—including the receipt and return of test materials—to a qualified colleague.
- You *may not* have access to the secure test materials prior to test day.

- You *may* serve as a room supervisor or proctor, provided that the examinee is not assigned to test in a room where you are working. You must not have access to the examinee's answer document or test materials.
- Relatives and wards include children, stepchildren, grandchildren, nieces, nephews, siblings, in-laws, spouses, and persons under your guardianship.

Scores for an examinee will be cancelled if any of these policies are violated

4.2 Test Administration Personnel and their Responsibilities

4.2.1 Test Coordinator

The Test Coordinator ensures that examinees test under the same conditions as examinees at every other site. The Test Coordinator can serve at only one test site.

Table 4.1: Responsibilities of the Test Coordinator

Category	Responsibility
Facilities and Staffing	<ul style="list-style-type: none"> • Selecting and reserving test rooms and preparing them for test day according to ACT guidelines • Selecting and training qualified testing staff
Before Testing	<ul style="list-style-type: none"> • Reading the testing manuals and ensuring compliance with its policies and procedures • Viewing and participating in training provided by ACT • Ordering standard time materials for the initial test date • Ordering alternate testing formats for examinees needing accommodations • Receiving, checking-in, and securely storing test materials • Arranging for the application of barcode labels on the answer documents by testing staff if required • Arranging for examinees to complete the non-test portions of their answer documents • Preparing rosters and organizing test materials • Notifying examinees of the test date(s), location, and materials needed
On Test Day	<ul style="list-style-type: none"> • Conducting a briefing session for testing staff • Counting and distributing test materials to staff • Ensuring that testing begins at the same time in all rooms • Supervising and assisting staff during testing • Arranging for transfer of test responses to answer documents for examinees approved by ACT for alternate response modes, or approved locally to mark answers in the test booklet • Serving as room supervisor as needed

4.2.2 Back-up Test Coordinator

The Test Coordinator should have a qualified Back-up Test Coordinator available if the Test Coordinator becomes ill or is otherwise unable to be present on test day. The Back-up Test Coordinator is encouraged to assist the Test Coordinator prior to, during, and after testing.

He or she is also expected to participate in training conducted by ACT (if previously untrained by ACT) prior to the test date. The Back-up Test Coordinator can serve at only one test site.

If the Test Coordinator is not able to supervise the administration, the Back-up Test Coordinator must complete and submit a profile change form online by going to the web address listed on your *Checklist of Dates*.

4.2.3 Test Accommodations Coordinator

The Test Coordinator must name a qualified Test Accommodations Coordinator. The Test Accommodations Coordinator is responsible for the following:

- Assisting the Test Coordinator in his or her responsibilities as needed
- Reading the testing manuals and complying with its policies and procedures
- Evaluating and approving requests for ACT WorkKeys accommodations
- Notifying the Test Coordinator of any examinees needing alternate format test materials from ACT
- Viewing and participating in accommodations training provided by ACT
- If the Test Accommodations Coordinator is no longer able to serve in his or her role, the Test Coordinator must contact ACT at 800.553.6244, ext. 1788, to designate a replacement

4.2.4 Room Supervisor

Each room is required to have a Room Supervisor who must serve for the entire session. The Test Coordinator or Test Accommodations Coordinator may serve as room supervisor if only one room is used.

Specific responsibilities include:

- Reading the testing manuals and complying with the policies and procedures it describes
- Attending both the training and briefing sessions conducted locally by the Test Coordinator
- Being responsible for the test room and providing an environment conducive to testing
- Checking ID or personally recognizing and admitting examinees
- Marking attendance/ID on the roster
- Directing examinees to seats
- Counting test booklets upon receipt from the Test Coordinator
- Distributing test materials and keeping test booklets in sequential serial number order
- Reading verbal instructions to examinees exactly as they are written
- Properly timing tests and recording the start, 5-minutes-remaining, and stop times in the manual using two timepieces
- Completing all information on the Seating Diagram and Test Booklet Count Form as found in the *Administration Manual for Paper and Pencil Testing*.
- Being attentive to examinees and materials at all times (Proctor may assist with this activity)

- Walking around the test room during testing to be sure examinees are working on the correct sections of the test booklet and answer document (Proctor may assist with this activity)
- Paying strict attention to monitoring examinees during the entire test session to detect and discourage prohibited behavior (Proctor may assist with this activity)
- Collecting and accounting for all answer documents and test booklets before dismissing examinees (Proctor may assist with this activity)
- Completing detailed documentation of any irregularities and, as required, voiding examinees' tests
- Returning all test materials and forms to the Test Coordinator immediately after testing

4.2.5 Proctor

A Proctor may be used to assist a Room Supervisor or the Test Coordinator if fewer than 10 examinees are testing. A Proctor *is required* (in addition to the Room Supervisor) for every 10 examinees (or portion thereof) after the first 10 in the room. For example, if there are 30 examinees, three proctors are required.

The Proctor's responsibilities include:

- Reading the testing manuals and complying with the policies and procedures it describes
- Attending both the training and briefing sessions conducted locally by the Test Coordinator
- Helping admit examinees and marking attendance/ID on the roster
- Directing examinees to seats
- Helping distribute test materials and keeping test booklets in sequential serial number order
- Verifying the timing of the tests using a different timepiece than the room supervisor
- Being attentive to examinees and materials at all times
- Walking around the room during testing to replace defective materials, to be sure all examinees are working on the correct test, and to observe examinee behavior
- Reporting any irregularities to the room supervisor immediately
- Accompanying examinees to the restroom if more than one is allowed to leave during the timed tests
- Paying strict attention to monitoring examinees during the entire test session to discourage and detect prohibited behavior
- Helping collect and account for all answer documents and test booklets

4.3 Training Testing Staff

For testing to occur successfully, staff members must understand their responsibilities. It is critical that the standardized test administration procedures are followed by every test center.

4.3.1 Training Session

Test Coordinators are required to hold a training session **before** test day to prepare staff for test day activities and to stimulate discussion. In addition, on each test day morning, Test Coordinators are required to hold a briefing session to discuss any last-minute issues that may arise as well as concerns staff members may have.

4.3.2 Administration Manual

ACT provides the *Administration Manual*, which every staff member is expected to read and communicate its expectations. The manual is proprietary information and is copyrighted by ACT. It is to be used only for the purpose of administering the ACT WorkKeys assessments and is not to be copied or shared for any other purpose.

Each testing staff member is to be provided with a complete copy of this manual before the training session. It is especially important that Room Supervisors read and understand the policies, procedures, and directions.

4.4 Test Administration Room Requirements

Test administration rooms must be set up according to the requirements defined below. If these requirements are not met, scores may be cancelled.

- **All examinees in the test room must face the same direction**, regardless of the number of examinees in the room or the distance between them.
- There must be **at least three feet of space between examinees** (side-to-side measured shoulder-to-shoulder, and front-to-back measured head-to-head).
- In a room with multiple-level seating, examinees must be **at least five feet apart** front-to-back.
- There must be sufficient aisle space for staff to get to every seat during testing without disturbing examinees.
- Seat examinees in straight rows and columns, directly in line with each other.
- If a clock is in the room, seat examinees facing the clock whenever possible so they can see it without looking around.
- The room supervisor must be stationed in the room facing the examinees. Staff must be able to see every examinee clearly. Seating with dividers or partitions, such as study carrels, partitioned tables, or booths, is not acceptable because it obstructs staff's view of examinees.

Note

¹ ACT WorkKeys provides test administrators multiple support materials. The support materials can be found at <http://www.act.org/content/act/en/products-and-services/workforce-solutions/act-workkeys/administer.html#techspecs>.

Chapter 5

Accessibility

The ACT WorkKeys[®] Applied Math assessment uses a variety of levels of accessibility supports including default embedded tools, open access tools, and full accommodations to allow all examinees, including those with disabilities, to participate in testing.

5.1 ACT WorkKeys Applied Math Assessment Support System

ACT has established for the Applied Math assessment a continuum of supports for effective communication that spans from the most simple, common accessibility tools used by everyone, to the most intensive accessibility supports that require the user to have specific qualifications and expertise. To build an assessment system that meets the needs of all populations tested and provides a fair communication and performance pathway for all learners, more than one level of support is needed.

“Accessibility is the degree to which the items or tasks on a test enable as many test takers as possible to demonstrate their standing on the target construct without being impeded by characteristics of the item that are irrelevant to the construct being measured” (AERA et al., 2014, p. 215). The Applied Math assessment support continuum is an inclusive concept that recognizes that the need for personalized communication supports is not restricted to any one group of examinees. It describes needs all test takers have, regardless of whether or not they have an official diagnostic label. It encompasses the needs of the entire testing population, including those with disabilities, those who are English Learners, as well as all the rest who have no diagnostic label at all. All of these individuals have a shared need to be able to fairly and effectively communicate what they know and can do when they take a test.

To provide a fair performance pathway for all learners, including populations with diverse needs, the development of the Applied Math assessment followed a theory of action known as Access by Design (Fedorchak, 2013) which incorporates elements of Universal Design for Learning (UDL) described by the Center for Applied Special Technologies (CAST, 2011), and Evidence-Centered Design (Mislevy, Almond, & Lukas, 2004; Mislevy & Haertel, 2006) into its conceptual structure.

In September 2015, in anticipation of the development of this assessment, a week-long accessibility test development workshop was held with leadership and content developers of ACT WorkKeys National Career Readiness Certificate (NCRC®) Assessments. The topic of this workshop focused on methods of mapping the characteristics and accessibility needs of learner populations to the content models intended to be measured by the ACT WorkKeys NCRC Assessments. During this training, accessibility consultants provided feedback with respect to accessible definitions of constructs to be tested and a plan was established for ongoing accessibility consultation and advisement during test development.

The mapping process presented in Figure 5.1 provides an evidence-based structure to determine accessible communication and performance pathways as well as accessibility support options to be allowed for the ACT WorkKeys NCRC assessments.

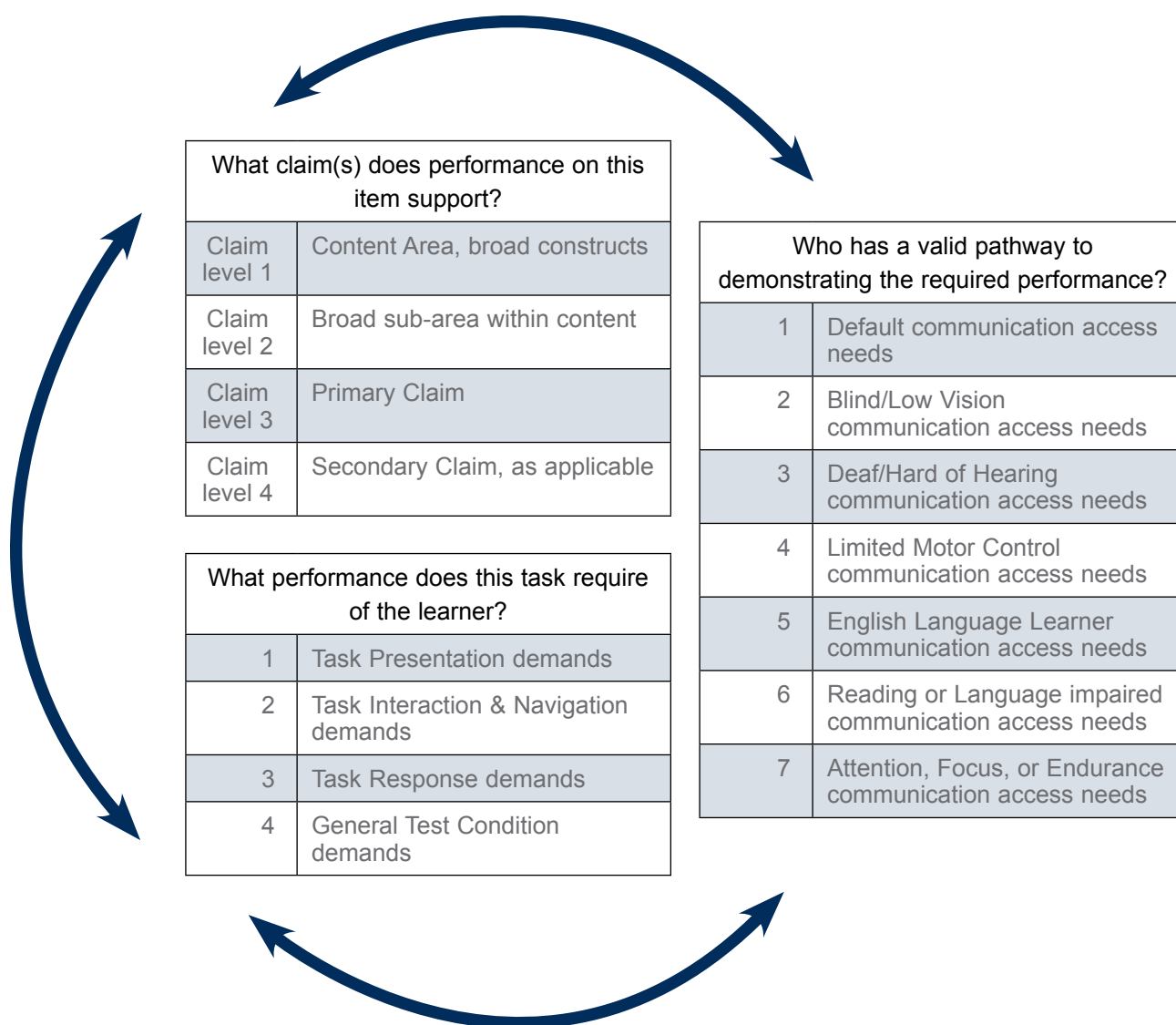


Figure 5.1: Accessibility Feature Mapping Process

The Applied Math assessment accessibility supports are structured along a continuum of increasingly intensive supports designed to meet the needs of all participating learner populations. Three levels of accessibility supports are offered: 1) Embedded Tools, 2) Open Access Tools, and 3) Accommodations. Embedded tools are commonly used by many people, available to all examinees, and do not need to be requested in advance. Open Access Tools are used by fewer people, are also available to anyone, but their use must be identified and planned for locally in advance. Accommodation-level supports and tools are the most intensive levels of support. Accommodations are available to those who are qualified to use them. Currently, certain supports are only available with the paper form of the test. These are outlined later in this chapter. Beginning in 2018, several new accessibility supports will be added to the Applied Math assessment for both paper and online forms. These additions will fill out the planned continuum of accessibility supports and will provide many options for unique personalization of experience for each examinee.

5.2 Test Administration and Accessibility Levels of Support

Educational researchers and practitioners have learned over the last decade that all examinees have tools they need and use every day to engage in the classroom and to communicate effectively what they have learned and can do. There are different levels of support that examinees may need in order to demonstrate what they know and can do on academic tests. The Applied Math assessment makes several possible levels of support available. All these levels of support taken together are called accessibility supports. These accessibility supports:

- allow all examinees to gain access to effective means of communication that in turn allow them to demonstrate what they know without providing an advantage over any other examinee;
- enable effective and appropriate engagement, interaction, and communication of examinee knowledge and skills;
- honor and measure academic content as the test developers originally intended;
- remove unnecessary barriers to examinees demonstrating the content, knowledge, and skills being measured on the Applied Math assessment.

In short, accessibility supports do nothing for the examinee academically that he or she should be doing independently; they just make interaction and communication possible and fair for each examinee.

The Applied Math assessment accessibility system defines four levels of support that range from minor support (default embedded system tools) to extreme support (modifications). Figure 5.2 shows the architectural structure of ACT WorkKeys assessments accessibility supports.

The Applied Math assessment permits the use of only those accessibility supports that validly preserve the skills and knowledge that the assessment claims to measure, while removing needless, construct-irrelevant barriers to examinee performance. The four levels of support in the Applied Math assessment accessibility system represent a continuum of supports, from least intensive to most intensive, and assumes all users have communication needs that fall somewhere on this continuum. The continuum of supports permitted in the Applied Math assessment results in every examinee having a personalized performance opportunity.

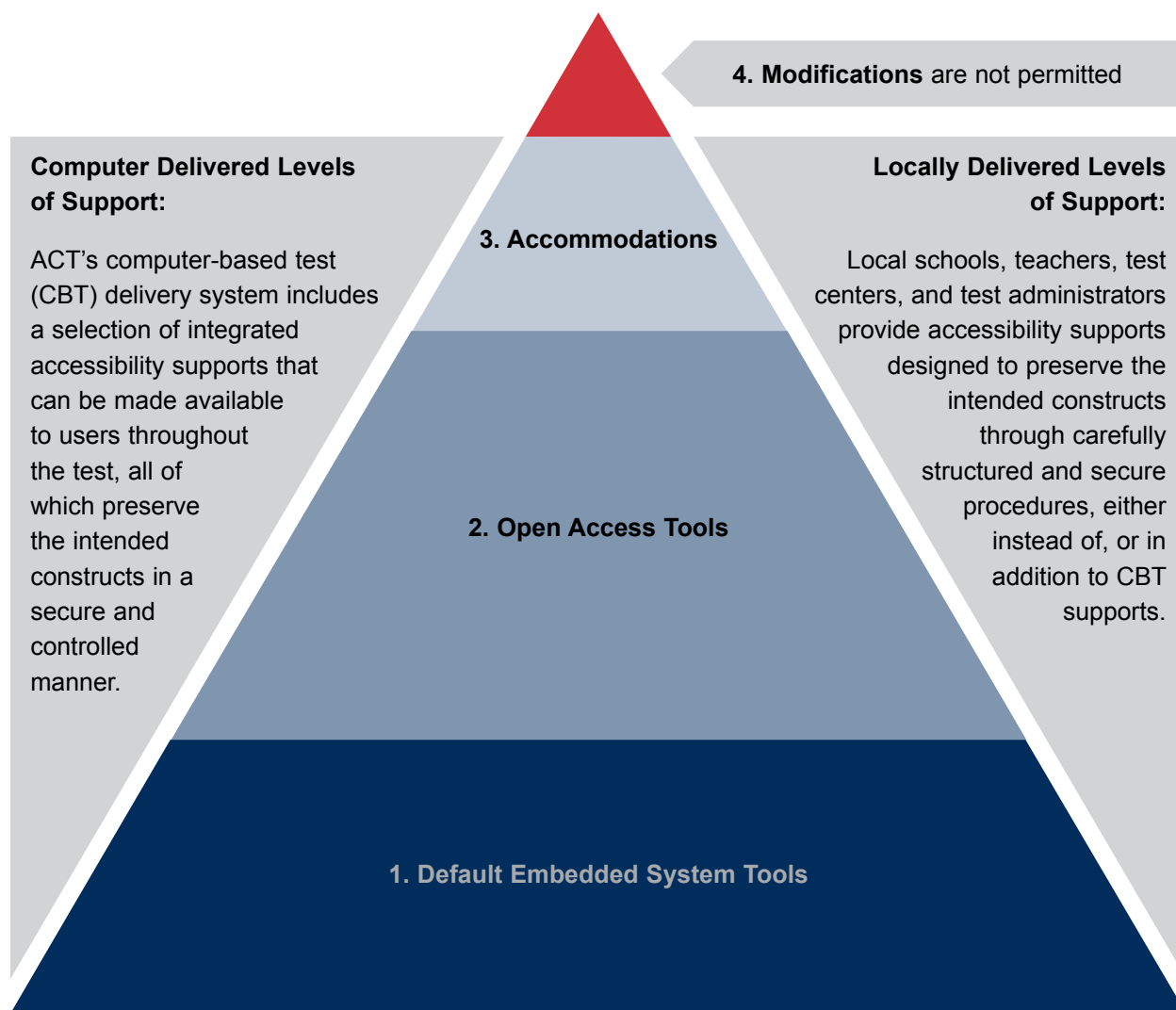


Figure 5.2: Architectural Structure of Accessibility Supports

Note. Width of the triangle above shows the proportion of examinees who use that set of assessment tools.

Support Level 1: Default Embedded System Tools

The first level of supports is called the Default Embedded System Tools. (See the first level of the pyramid in Figure 5.2.) They are automatically available to a default user whose accessibility needs are sufficiently met through the basic test administration experience.

Default embedded system tools meet the common, routine accessibility needs of the most typical test takers. All examinees are provided these tools as appropriate, even examinees who have no documented support plan. Default embedded system tools include, but are not limited to, the following examples in online and paper tests:

- Magnifier Tool (online and paper)
- Browser Zoom Magnification (online)
- Answer Eliminator (online and paper)
- Test Directions Available on Demand (online and paper)
- Highlighter (online and paper)
- Keyboard Navigation (online)
- Scratch Paper (online and paper)
- Mark Item for Review (online and paper)

Default embedded system tools are common supports made available to all users upon launch or start of the test; they are the accessibility tools that nearly everyone uses routinely and assumes will be made available although they are seldom thought of in this way. These tools are either embedded in the basic computer test delivery platform, or they may be locally provided as needed. No advance request is needed for these supports.

Support Level 2: Open Access Tools

Open Access tools (See the second level of the pyramid in Figure 5.2.) are available to all users, but must be identified in advance, planned for, and then selected from the menu inside the test to be activated (online), or else provided locally.

Many examinees' unique sensory and communication accessibility needs are predictable and can be met through a set of accessibility features designed into the underlying structure and delivery format of test items. Rather than overwhelm the user with all the possible tools, Open Access tools provide just the tools needed by individual users, allowing true personalization of the test experience.

Open Access tools are slightly more intensive than default embedded system tools but can be delivered in a fully standardized manner that is valid, appropriate, and personalized to the specific access needs identified for an individual examinee. Some of these require the use of tool-specific administration procedures. In the Applied Math assessments, Open Access tools include, but are not limited to the following examples:

- Color Contrast (online and paper)
- Line Reader (online and paper)
- Translated Verbal: Directions Only (online and paper) locally provided
- Signed Exact English (SEE) for Directions Only – locally provided (paper)
- Answer Masking (online and paper)
- Dictate Responses (online and paper)

- Respond in Test Booklet or on separate paper (online and paper)
- Audio Indicator of Time Remaining (online and paper)
- Individual Administration (online and paper)
- Special Seating/Grouping (online and paper)

Open Access tools should be chosen carefully and specifically to prevent the examinee from becoming overwhelmed or distracted during testing. Room supervisors must follow required procedures. Prior to the testing experience, examinees need to have an opportunity to practice and become familiar and comfortable using these types of tools as well as using them in combination with other tools.

Support Level 3: Accommodations

Accommodations are high-level accessibility tools needed by relatively few examinees. (See the third level of the pyramid in Figure 5.2.) The Applied Math assessment system requires accommodation-level supports to be requested by educational personnel on behalf of an examinee. The accommodations must be identified in advance, planned, and selected from the menu inside the test to activate them (online), or else provided locally. Accommodations use often requires advance ordering of specialized paper materials from ACT. The advance planning process allows any needed resources to be assigned appropriately and documented for the examinee.

Typically, examinees who receive this high level of support have a formally documented need and have therefore been identified as qualifying for resources or specialized supports that require expertise, special training, and/or extensive monitoring to select, administer, and even to use the support effectively and securely. These can include but are not limited to the following examples:

- Braille EBAE, contracted, includes tactile graphics (paper)
- Braille UEB with Nemeth contracted, includes tactile graphics (paper)
- Cued Speech (online and paper)
- Word-to-Word Bilingual Dictionary, ACT approved (online and paper)
- English Audio DVD (designed for user with blindness (paper)
- English Audio Reader Script (designed for user with blindness (paper)
- Signed Exact English (SEE): Test Items
- Abacus
- Extra Time

Decisions about accommodation-level supports are typically made by an educational team on behalf of, and including the examinee. Accommodation decisions are normally based on a formal, documented evaluation of specialized need and require the examinee to have personal familiarization and successful prior experience with the tools so they may be used fluidly and effectively during the test experience. Accommodation supports require substantial additional local resources or highly specialized, expert knowledge to deliver successfully and securely.

Accommodations are available to users who have been qualified by the local governing school or employment authority to use them, (e.g., a school district, a work training agency, an employer, or a

branch of military or other government service). Official determination of qualification for accommodation-level support by a governing school or workforce authority is usually documented in writing in the form of an accommodation plan, or such qualification may have been routinely recognized and permitted for this examinee by that governing authority. ACT WorkKeys NCRC Assessments require that examinees who use accommodation-level supports have a formally documented need, as well as relevant knowledge and familiarity with these tools. Accommodations must be requested through the local test site according to ACT WorkKeys NCRC Assessments procedures, as defined in the administration manual. Appropriate documentation of accommodation need, as specified in the manual, must be provided prior to testing by the examinee, or by a local governing educational authority on behalf of the examinee.

Support Level 4: Modifications

Modifications are supports that are sometimes used during instruction, but when used in a testing situation, they alter the construct that the test is designed to measure. While they may provide an individual with the experience of taking ‘a test,’ modifications provide so much support that they actually prevent the examinee from having meaningful access to performance of the construct being tested. (See the top level of the pyramid in Figure 5.2.) Because modifications violate the construct being tested, they invalidate performance results and communicate low expectations of examinee achievement. Modifications are not permitted during Applied Math testing, and if used, invalidate the resulting test score.

5.3 Allowable Embedded Tools, Open Access, and Accommodations

In our commitment to provide a fair testing experience for all examinees, ACT WorkKeys NCRC Assessments provide an integrated system of accessibility supports that include accommodations as well as other forms (less intensive levels) of accessibility support. There are times when supports provided for those who test using the online format are combined with other types of locally provided or paper-format supports. The reverse is also true, as examinees using the paper format sometimes also take advantage of certain online options. Regardless of test format, all examinees who use Accommodation-Level accessibility features must have this use documented by appropriate school (or test site) personnel. For this reason, we have provided the general description of ACT WorkKeys NCRC Assessments Accessibility Supports here in one section. Full procedural requirements and instructions for using permitted supports during test administration are provided in the ACT WorkKeys NCRC Assessments Administration Manual.

5.4 Valid Test Scores and Equal Benefit for All Examinees

ACT aims to ensure that all examinees may benefit equally from the WorkKeys Applied Math assessment. Accommodations and other accessibility supports administered under these standardized conditions result in a valid and fully reportable NCRC score. Use of any accessibility supports that are not specified by ACT or not properly administered violate what the test is designed to measure and result in a score that is invalid and non-comparable for the stated purposes of the assessment.

Table 5.1: NCRC Accessibility Supports Permissible by Assessment—Paper and Online Testing Paper Testing 2017

Presentation Supports	Support Level	Applied Math
Test Directions Available on Demand (Printed)	Embedded	Yes
Magnifier Tool	Embedded	Yes
Full Page Magnification	Embedded	Yes
Line Reader	Open Access	Yes
Color Contrast (Color Overlays)	Open Access	Yes
Large Print Test Booklet, Printed	Open Access	Yes
Translated Verbal: Directions only (locally provided)	Open Access	Yes
American Sign Language (ASL) Directions Only	Open Access	Yes
Signed Exact English (SEE): Directions Only	Open Access	Yes
Signed Exact English (SEE): Test Items	Accommodation	Yes
Cued Speech	Accommodation	Yes
English Audio DVD (designed for user with blindness)	Accommodation	Yes
English Audio Reader Script (designed for user with blindness)	Accommodation	Yes
Word-to-Word Bilingual Dictionary, ACT approved	Accommodation	Yes
Braille EBAE, contracted, includes tactile graphics	Accommodation	Yes
Braille UEB with Nemeth, contracted, includes tactile graphics	Accommodation	Yes

Paper Testing 2017 (continued)

Interaction & Navigation Supports	Support Level	Applied Math
Answer Eliminator	Embedded	Yes
Highlighter	Embedded	Yes
Scratch Paper	Embedded	Yes
Calculator	Embedded	Yes
Answer Masking	Open Access	Yes
Custom Masking	Open Access	Yes
Abacus	Accommodation	Yes

Response Supports	Support Level	Applied Math
Mark Item for Later Review (requires examinee mark to be erased thoroughly)	Embedded	Yes
Dictate Responses	Open Access	Yes
Respond in Test Booklet or on separate paper	Open Access	Yes
Electronic Spell Checker	Accommodation	Yes
Accessible Keyboard or AAC Device, with local print-out	Accommodation	Yes

General Test Conditions	Support Level	Applied Math
Proctor ability to add Extra Time (in event of test administration incident)	Embedded	Yes
Audio Indicator of Time Remaining	Open Access	Yes
Audio Indicator: 5-minute Warning	Open Access	Yes
Break: Supervised within each day (stop the clock)	Open Access	Yes
Individual Administration (not home)	Open Access	Yes
Location for Movement	Open Access	Yes
Other Setting (not home)	Open Access	Yes
Physical/Motor Equipment	Open Access	Yes
Special Seating/Grouping	Open Access	Yes
Visual Environment	Open Access	Yes
Audio – Acoustic Environment	Open Access	Yes
Extra Time	Accommodation	Yes
Break: Securely extend session over multiple days	Accommodation	Yes

Computer Testing June 2017

Presentation Support	Support Level	Applied Math
Test Directions Available on Demand (on screen)	Embedded	Yes
Magnifier Tool	Embedded	Yes
Browser Zoom Magnification (full page)	Embedded	Yes
American Sign Language (ASL) Directions Only	Open Access	Yes
Line Reader	Open Access	Yes
Color Contrast (High/Low Contrast Colors)	Open Access	Yes
Translated Audio: Directions Only	Open Access	Yes
Signed Exact English (SEE): Directions Only	Open Access	Yes
Cued Speech	Accommodation	Yes
Word-to-Word Bilingual Dictionary, ACT Approved	Accommodation	Yes

Interaction & Navigation Support	Support Level	Applied Math
Answer Eliminator	Embedded	Yes
Highlighter	Embedded	Yes
Keyboard Navigation	Embedded	Yes
Scratch Paper	Embedded	Yes
Calculator	Embedded	Yes
Answer Masking	Open Access	Yes
Custom Masking	Open Access	Yes
Abacus	Accommodation	Yes

Response Support	Support Level	Applied Math
Mark Item for Review	Embedded	Yes
Dictate Responses	Open Access	Yes
Respond on Separate Paper	Open Access	Yes
Electronic Spell Checker	Accommodation	Yes
Accessible Keyboard or AAC device, with local print-out	Accommodation	Yes

Computer Testing June 2017 (continued)

General Test Conditions	Support Level	Applied Math
Proctor ability to add Extra Time (in event of test administration incident)	Embedded	Yes
Audio Indicator of Time Remaining	Open Access	Yes
Audio Indicator: 5-minute Warning	Open Access	Yes
Break: Supervised within each day (stop the clock)	Open Access	Yes
Individual Administration (not home)	Open Access	Yes
Location for Movement	Open Access	Yes
Other Setting (not home)	Open Access	Yes
Physical/Motor Equipment	Open Access	Yes
Special Seating/Grouping	Open Access	Yes
Audio—Acoustic Environment	Open Access	Yes
Visual Environment	Open Access	Yes
Extra Time	Accommodation	Yes

Chapter 6

Test and Information Security

6.1 Test Security

In order to ensure the validity of the ACT WorkKeys[®] Applied Math test scores, test takers, individuals that have a role in administering the tests, and those who are otherwise involved in facilitating the testing process, must strictly observe ACT's standardized testing policies, including the Test Security Principles and test security requirements. Those requirements are set forth in the *ACT WorkKeys Administration Manual—Paper Testing* and the *ACT WorkKeys Administration Manual—Online Testing* and may be supplemented by ACT from time to time with additional communications to test takers and testing staff.

ACT's test security requirements are designed to ensure that examinees have an equal opportunity to demonstrate their academic achievement and skills, that examinees who do their own work are not unfairly disadvantaged by examinees who do not, and that scores reported for each examinee are valid. Strict observation of the test security requirements is required to safeguard the validity of the results.

Testing staff must protect the confidentiality of the ACT WorkKeys test items and responses. Testing staff should be competent and aware of their roles, including understanding ACT's test administration policies and procedures and acknowledging and avoiding conflicts of interest in their roles as test administrators for ACT WorkKeys.

Testing staff must be alert to activities that can compromise the fairness of the test and the validity of the scores. Such activities include, but are not limited to, cheating and questionable test taking behavior (such as copying answers or using prohibited electronic devices during testing); accessing questions prior to the test; taking photos or making copies of test questions or test materials; posting test questions on the internet; or test proctor or test administrator misconduct (such as providing answers or questions to test takers or permitting test takers to engage in prohibited conduct during testing).

In addition to these security-related administration protocols, ACT engages in additional test security practices designed to protect the WorkKeys assessment and the validity of its scores. These practices include: (1) use of a reporting hotline through which individuals with information about misconduct on an ACT WorkKeys test can anonymously report such information to ACT; (2) data forensics in support

of ACT WorkKeys related investigations; and (3) web monitoring to detect testing misconduct, possible unauthorized disclosure of secure ACT WorkKeys test content, and other activity that might compromise the security of the ACT WorkKeys test or the validity of its scores.

6.2 Information Security

ACT's Information Security program framework is based on the widely recognized ISO/IEC 27000 standard (International Organization for Standardization, 2017). This framework was selected because it covers a range of information security categories that comprehensively matches the broad perspective that ACT takes in safeguarding information assets. The categories covered by the framework and brief statements of their importance to ACT are:

1. **Information Security Program Management:** This is overseen by the Information Security Officer at ACT. The Information Security Officer has responsibility for providing guidance and direction to the organization to ensure compliance with all relevant security-related regulations and requirements. The program itself is designed to cover all security domains identified in the ISO 27001 standards and provides comprehensive oversight for Information Security at ACT.
2. **Information Security Risk Management:** The cornerstone of the ACT Information Security program is a risk assessment that conforms to the ISO 27005 standard. The identification, management, and mitigation of information security risks are managed using the ISMS (Information Security Management System) guidelines defined in the 27005 standard. ACT also makes use of the SP NIST 800-37 Risk Assessment which complies with FISMA security requirements for risk management (National Institute of Standards and Technology, 2017).
3. **Information Security Policies and Standards:** ACT established an Information Security policy to set direction and emphasize the importance of safeguarding information and data assets. Additional supporting policies, standards, and procedures have been developed to communicate requirements.

ACT's Information Security Policy and the Assessment Data Sharing procedures govern the handling of examinee data that is classified as confidential restricted. The policy states that confidential restricted information must meet the following guidelines:

- Electronic information assets must only be stored on ACT-approved systems/media with appropriate access controls.
- Only limited authorized users may have access to this information.
- Physical records must be locked in drawers or cabinets while not being used.
 - ACT also has Access Management, Business Continuity Standard, Clear Desk/ Clear Screen, End User Storage, External Authentication, Information Security Incident Management, Malware Protection, Mobile Device, Network Security Management, Payment Card Security, Secure Application Development, Secure System Configuration, Security Event Logging and Monitoring Standard, System Vulnerability and Patch Management and Web Content Standard to form a system of control to protect examinee data.

4. **Information and Technology Compliance:** The systems that store, maintain, and process information are designed to protect data security through all lifecycle stages. The security considerations surrounding ACT's systems include measures such as encryption, system security requirements, and logging and monitoring to verify systems are operating within expected parameters.
5. **Business Continuity and Disaster Recovery:** ACT maintains a Business Continuity program designed to provide assurance that critical business operations will be maintained in the event of a disruption. An essential part of the program includes a cycle of planning, testing, and updating. Disaster Recovery activities are prioritized by the criticality of systems and recovery times established by the business owners.
6. **Security Training and Awareness:** At ACT, Information Security is everyone's responsibility. All employees take part in annual Information Security awareness training on topics covered in the Information Security policy. Additionally, ACT has individuals within the organization who are responsible for the management, coordination, and implementation of specific Information Security objectives and who receive additional Information Security Training.
7. **Identity and Access Management:** ACT addresses data integrity and confidentiality by implementing policies and procedures that limit access to individuals who have a business need to know the information and that verify the individual's identity. Access to ACT systems and data requires authorization from the appropriate system owner. Active Directory, file permissions, and VPN (Virtual Private Network) remote access is administered by an Identity and Access management team who are part of the Information Security organization.
8. **Information Security Monitoring:** The foundation of ACT's Information Security Program is reflected in the Information Security Policy which is presented and reinforced with training to all ACT employees. ACT is held accountable to following the Information Security Program through internal assessments of the security control environment. Additionally, ACT works with independent third-parties to provide assessment feedback.
9. **Vulnerability and Threat Management:** ACT has several mechanisms in place to identify vulnerabilities on networks, servers, and desktops. Monthly vulnerability scanning is performed by a qualified ASV (Approved Scanning Vendor). ACT has always maintained a "compliant" status in accordance with PCI-DSS (Payment Card Industry Data Security Standards) requirements. In addition to the scans performed for PCI compliance, ACT has a suite of vulnerability scanning tools which are coordinated with a log management and event monitoring tool to provide reporting and alerting.
10. **Boundary Defense:** ACT utilizes multiple intrusion protection and detection strategies, tools, processes, and devices to look for unusual attack mechanisms and detect any kind of compromise of these systems. Network-based IDS sensors are deployed on Internet and extranet DMZ systems and networks which provide alerting and procedures for review and response. Procedures include security review and approval of changes to configurations and semi-annual firewall rule review and restrictions to deny communications with, or limit data flow to known malicious IP addresses.
11. **Endpoint Defenses:** A variety of tools are utilized to ensure that a secure environment is maintained at the end-user device level. This includes segmentation within the ACT network,

anti-virus programs, and data-loss prevention programs. VPN is required for all remote access to the ACT network. Wireless access on the ACT campus requires authentication credentials and continuous scanning for rogue access points is performed.

12. **Physical Security:** Maintaining security on the premises where information assets reside is often considered the first line of defense in Information Security. ACT has implemented several security measures to ensure physical locations and equipment used to house data are protected, including card-key access to all facilities and camera monitoring at all entry points.
13. **Security Incident Response and Forensics:** Planning for how to handle information security incidents is a critical component of ACT's Information Security program. Formal policy guidance outlines response procedures, notification protocols, and escalation procedures. Forensic investigations are performed at the direction of the Information Security Officer. ACT maintains a subscription service with a third-party specializing in computer forensics in the event of a declared incident.

ACT's Information Security Incident Response Plan (ISIRP) brings needed resources together in an organized manner to deal with an incident, classified as an adverse event, related to the safety and security of ACT networks, computer systems, and data resources.

The adverse event could come in a variety of forms: technical attacks (e.g., denial of service attack, malicious code attack, exploitation of a vulnerability), unauthorized behavior (e.g., unauthorized access to ACT systems, inappropriate usage of data, loss of physical assets containing Confidential or Confidential Restricted data), or a combination of activities. The purpose of the plan is to outline specific steps to take in the event of any information security incident.

This Information Security Incident Response Plan charters an ACT Security Incident Response Team (ISIRT) with providing an around-the-clock (i.e., 24/7) coordinated security incident response throughout ACT. Information Security management has the responsibility and authority to manage the Information Security Incident Response Team and implement necessary ISIRP actions and decisions during an incident.

Chapter 7

Reporting

7.1 Applied Math Reports

ACT WorkKeys[®] Applied Math reports are designed to provide detailed information to examinees, test administration officials, employers, workforce development officials, and educators. With the updated assessments and systems, the WorkKeys Online Reports Portal (WKRP) has been designed to provide real-time electronic information to test users. This information is available through the portal whether an examinee takes an assessment online or on paper.

The objectives of the Applied Math reports are:

- To clearly communicate to examinees, employers, educators, and workforce development officials the skills demonstrated by examinees
- To provide examinees with insights on their current skill levels and how they might improve
- To provide employers and educators actionable information to assist in decision making
- To provide workforce development officials and educators insights needed to improve examinee performance
- To provide information that connects skill levels to worker success
- To leverage technology to make the reporting user experience faster and more effective through the use of the WKRP

The Applied Math assessment is a criterion-referenced test. A criterion-referenced test differs from a norm-referenced test in that scores are interpreted based on skills demonstrated through testing. The Applied Math Performance Level Descriptors (PLDs) provide a detailed summary of the skills demonstrated by the examinee at each score level. (See Chapter 2 for the complete Applied Math PLDs.)

For the person who takes the assessment, performance is summarized through the Individual Examinee Score Report. For each WorkKeys assessment that a person takes, a separate Individual Examinee Score Report is generated. It provides the following information:

- ACT WorkKeys Realm Name
- Test Date
- Report Date
- Examinee's name
- Examinee's ID
- Assessment Title
- Scale Score (including possible scale score range)
- Level Score (including possible level score range)
- What your score means – a section that includes the PLD for the specified Level Score
- How you can use your scores – a statement that directs the examinee to a WorkKeys URL where additional score interpretation information is found

In addition to the Individual Examinee Score Report, ACT provides other reports that are available to either examinees or institutions. Table 7.1 presents the list of available Applied Math reports.

Table 7.1: Applied Math Reports and Their Function

Report	Function
Individual Examinee Score Report	This report provides information to the examinee about his or her score and what it means to be at a specified skill level.
Individual Summary Score Report	This report provides information to the examinee about his or her scores and skill levels for all tests taken online.
Roster Score Report	This report is a list of all examinees, the tests taken, and the scores examinees received.
Data Export Report	This report exports data from the Validus system into an Excel file format. It provides all of the information about the examinee including demographics, date tested, test titles, and scores.
Individual Score Reports (by Group)	This report provides information to the examinee about their score and what it means to be at that skill level. This report is run for all examinees in the selected group.
Individual Score vs. Profile Report	This report is used to show a comparison of a required skill level with the skill level the examinee achieved. For example, a company may want this report if they are hiring for a job that has been job profiled and they know the level required for a specific skill area. This report will print with the skill level required and the skill level of the applicant.
Group vs. Profile Report	This report displays the scores that a group of examinees achieved compared to a score that is required for a job. For example, a company may want this report if they are hiring for a job that has been job profiled and they know the level required for a specific skill area. This report will print with the skill level required and the skill level of all applicants in the group.
Registered to Test Report	This report provides a list of examinees registered for tests who have not yet tested. Proctors of a realm who are not administrators of that realm will be able to run the Registered to Test Report.
Test Usage Report	This report provides a count of the tests launched at the site for a given test date range.

Chapters 8–11 of the Technical Manual describe in detail Applied Math assessment scores, metrics, and interpretations.

Chapter 8

Scores and Score Scales

8.1 Overview

This chapter describes the rationales, procedures, and outcomes for scoring the WorkKeys[®] Applied Math items, establishing scale scores, and defining level scores for the assessment.

Raw and scale scores are two types of scores used to facilitate score interpretation and use. *The Standards for Educational and Psychological Testing* (referred to as *the Standards* below) defines a raw score as “a score on a test that is calculated by counting the number of correct answers, or more generally, a sum or other combination of item scores” (AERA et al., 2014, p. 222). Raw scores are frequently transformed to scale scores to facilitate and standardize score interpretations. To produce scale scores for a new assessment, a scaling analysis is required; that is, “the process of creating a scale or a scale score to enhance test score interpretation by placing scores from different tests or test forms on a common scale or by producing scale scores designed to support score interpretations” (AERA et al., 2014, p. 223). For the Applied Math assessment, an Item Response Theory (IRT) approach with arcsine transformation was applied to produce a scale with nearly equal conditional standard error of measurement for most score points.

Any WorkKeys foundational skill assessment, including the Applied Math assessment, classifies an examinee into score levels that are aligned to the Performance Level Descriptors (PLDs). Combining the score level with the associated PLD provides the examinee and the test user with a description of the Applied Math skills demonstrated by the examinee. To achieve this alignment, cut scores are established on the reported score scale to support level score interpretations. A cut score is defined as “a specified point on a score scale, such that scores at or above that point are reported, interpreted, or acted upon differently from scores below that point” (AERA, et al., 2014, p. 218). For the Applied Math assessment, cut scores are established through a standard setting process drawing upon a panel of Subject Matter Experts (SMEs) to ensure the alignment of the level scores to the PLDs (AERA et al., 2014).

8.2 Selected-Response Item Scoring

All items on the Applied Math assessment are selected-response items (e.g., multiple choice items). Selected-response items require examinees to select a correct answer from a set of alternative choices. For the Applied Math assessment, each selected-response item has five choices or options. Each item that an examinee answers correctly provides the examinee with a score value of one raw point. An incorrect response, a missing response (items that an examinee did not answer), or multiple responses yield a value of zero raw point. The examinee's raw score is calculated by summing the correct responses.

ACT strives to write each Applied Math item so that there is only one correct response. To ensure that there is only one correct response, ACT follows the process outlined in Chapter 2 that includes item writing, editing, review, and pretesting. Following these steps, an item may be selected for inclusion on an Applied Math form. ACT psychometricians and content specialists regularly conduct preliminary item analysis and review the results for key validation for all the items on a form when initial form administration reaches acceptable sample size.

8.3 Scale Score and Level Score Differences and Rationale

Each item on the assessment is written to assess a specified skill level defined by the Applied Math assessment construct. Applied Math skills associated with each of the five levels (Levels 3 to 7) were defined through the design process described in Chapter 2. Each Applied Math form is composed of the items to assess the skills defined by the level, and it is built to the test specifications described in Chapter 3. When examinees complete the Applied Math assessment, they receive a report that includes the scale and level scores. The scale and level scores serve two distinct purposes in facilitating score interpretations and uses.

Scale scores provide finer grain score distinctions than level scores and they are designed to assist in analyzing growth or improvement over time, evaluating group comparisons on outcome measures, and providing evidence of benefit from educational or training programs. The scale scores, ranging from 65 to 90, are constructed such that the Standard Error of Measurement (SEM) is approximately equal at each score point (Kolen, 1988). When the SEM is the same for all scores across the distribution, ACT is able to report all test scores with the same level of precision. Doing so increases the fairness of score interpretation, and it removes the need for ACT to report the SEM at the different score points.

Level scores provide examinees with information as to whether they were able to master the defined skills associated with a specified level. The levels are defined through the PLDs. (See Chapter 2 for the PLDs associated with each level.) ACT implemented a standard setting process by which data was gathered from SMEs to enable the establishment of cut scores to identify the scale score performance required to achieve a specified level score.

8.4 Procedures for Establishing the Score Scale

A scaling study was conducted in spring 2017 as part of a series of field studies to establish the score scale for the updated WorkKeys assessments. ACT recruited examinees to participate in the field studies from various regions in the United States. The sampling plan was designed to achieve a representative sample corresponding to the WorkKeys test taking population in terms of geographic region, gender, and ethnic groups. Following data cleaning, the scaling study included a sample of 1,185 examinees.

Forty sites participated in the scaling study. It included 13 high schools and 27 adult testing centers across 22 states. For the scaling study, female examinees outnumbered male examinees by 51% to 46%. In terms of ethnicity, White examinees comprised approximately 60% of the examinees, while African-American examinees comprised 17%, and Hispanic examinees comprised 7%. ACT concluded that the sample was representative of the current WorkKeys test taking population.

The examinees took the Applied Math assessment—Form M2C_S1 – in the scaling study. ACT analyzed examinee data from the scaling study applying a three-parameter logistic (3-PL) IRT model to calibrate item parameters. Figure 8.1 presents the raw score distribution from the sample. The distribution appears to be slightly left skewed, which is consistent with distributions observed from previous administrations of the Applied Mathematics assessment.

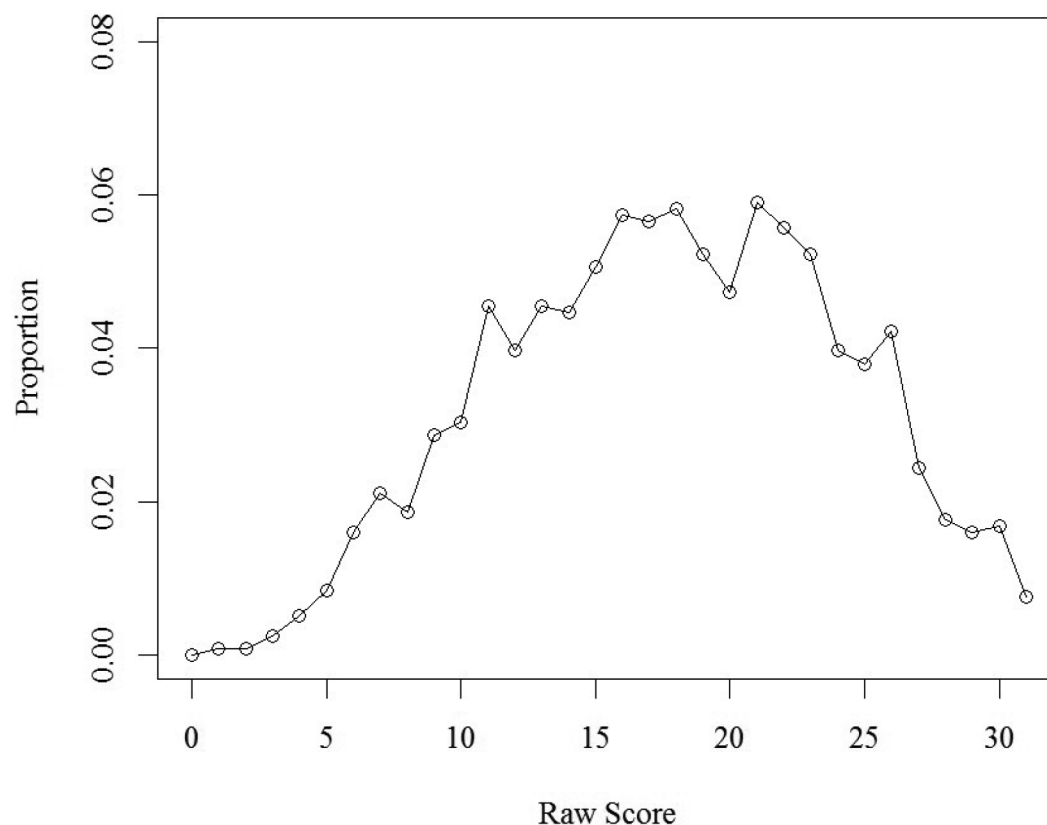


Figure 8.1: Raw Score Distribution for the AM Scaling Study Form (Form M2C_S1)

Note. Mean and standard deviation are 17.88 and 6.25 respectively.

Figure 8.2 illustrates the item p-values (ranging from 0.2 to 0.95) and b -parameter estimates by corresponding levels for this form, where the red dots represent the average item p-value or b -parameter estimate for that level. The item p-values tend to decrease as the item difficulty increases as expected. The plot on b -parameter estimates shows the similar trend (average b -parameter values increases as the level increases). Figure 8.3 shows the test characteristic curve (TCC) and test information function (TIF) for the Scaling Study form.

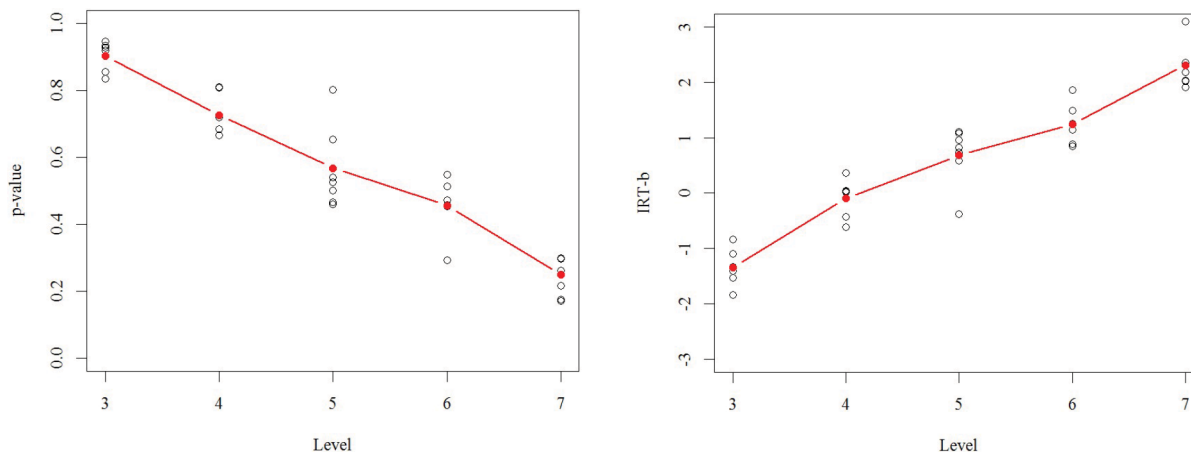


Figure 8.2: Item p-values and b -parameter estimates by Item Levels for Form M2C_S1

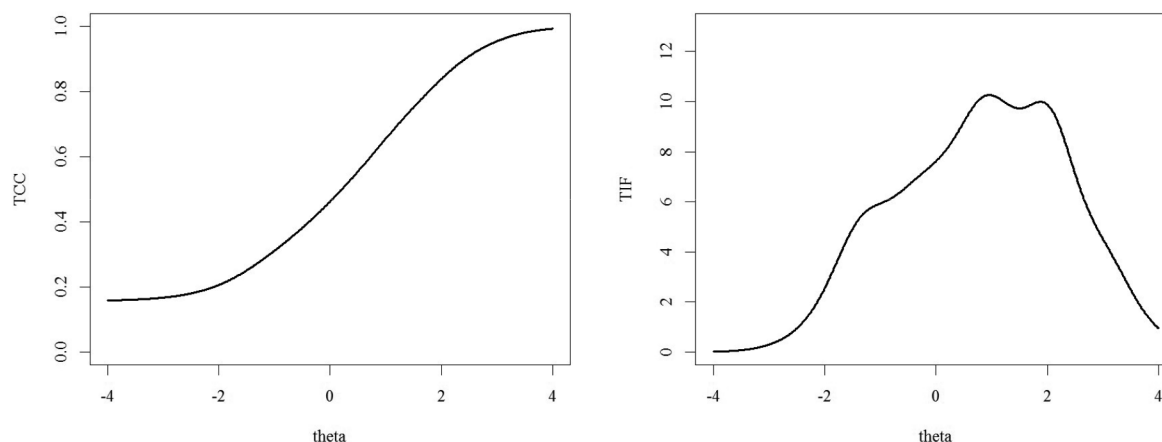


Figure 8.3: Test Characteristics Curve (left) and Test Information Function (right)

To be consistent with the Applied Mathematics assessment and the other NCRC assessments, the average scale score was set to be about 78 and the scale score Conditional Standard Error of Measurement (CSEM) was set to less than 2. In addition, the scale score range was defined as 65 to 90, which is identical to the range of NCRC 1.0 assessment scale score. The target scale score mean and target scale score SEM are required to conduct the scaling. IRT (Ban & Lee, 2007) was used to derive the raw-to-scale score conversion, and the arcsine transformation (Kolen, 1988; Kolen & Brennan, 2014)

was used to equalize the CSEM along the score scale. The following five steps were implemented for deriving the raw-to-scale score conversion:

1. Item parameters were calibrated based on the 3-PL IRT model.
2. Theta estimates (ability estimates) for each examinee were calculated based on the item scoring vector data and the item parameter estimates calibrated in step one.
3. The expected raw score distribution was estimated based on the item parameter estimates from step one and theta estimates from step two using the Lord-Wingersky recursive formula (Lord & Wingersky, 1984).
4. Arcsine transformation was used to transform the expected raw scores to g-scores.
5. The g-scores from step four were linearly transformed to the scale scores using the target scale score mean and target scale score SEM. The slope and intercept of the linear transformation are $A = \frac{\sigma(E_S)}{\sigma(E_g)}$ and $B = \mu(S) - \frac{\sigma(E_S)}{\sigma(E_g)} \times \mu[c(\chi)]$, respectively, where $\mu(S)$ and $\sigma(E_S)$ are the target mean and SEM of the scale scores, and $\mu[c(\chi)]$ and $\sigma(E_g)$ are the mean and SEM of the g-scores.

In applying the process to create the raw to scale score transformation, the following requirements were met:

- The reported score scale covered the full range from 65 to 90.
- No more than two raw score points corresponded to one scale score, except at the two ends.
- No gaps were allowed in the score scale except at the two ends.
- Rounding error was minimized. In other words, the number of scale scores with the first decimal place of 0.5 was small.
- CSEM was as similar as possible across the score scale.

The target scale score mean and target scale score SEM were specified to be 77.9 and 1.6. These values were obtained through several explorations using the data from the scaling study and the requirements defined above.

Along with achieving the same conversions as the NCRC 1.0 assessments (e.g., same scale score range and constant CSEM), the base form conversion for the Applied Math assessment included the following characteristics: (a) fewer truncated points at the lower end of the scale, (b) fewer and smaller score gaps at the higher end of the scale, and (c) defined target scale score average and CSEM.

The results indicated that the scaling procedures achieved the following goals:

- As shown in Figure 8.4, the scale score CSEMs is flat below 2.0 along the scale score except for two score ends. Note that the CSEMs of the raw scores tend to be larger in the middle and smaller at the two ends.
- The mean scale score (78) is very close to the target scale score mean (77.9) used as the input for the arcsine transformation. Table 8.1 presents the summary of the unrounded scale scores (USS) and rounded scale scores (RSS) for this form. Figure 8.5 illustrates the relative and cumulative frequency distributions of the scale scores.

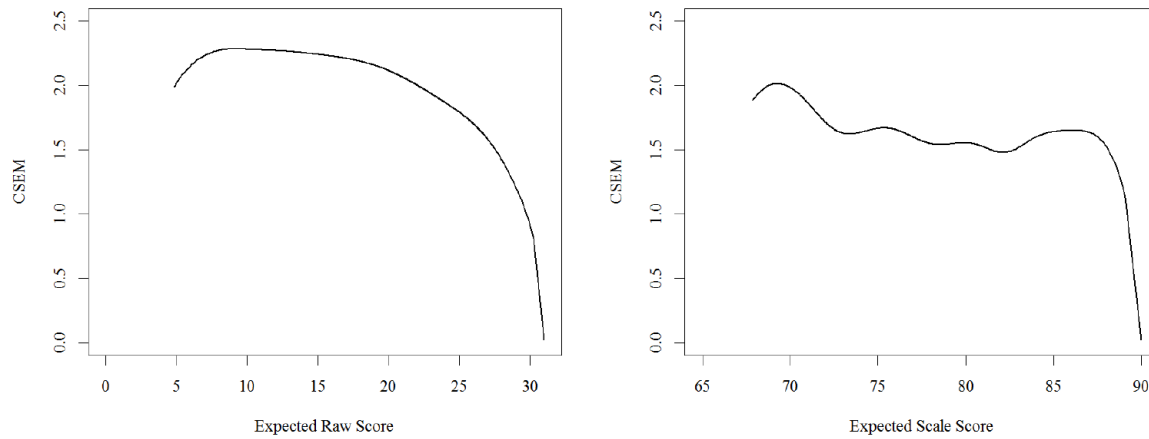


Figure 8.4: CSEM for Raw Scores (left) and Scale Scores (right)

Table 8.1: Summary of Unrounded and Rounded Scale Score

Form	Mean	SD	Min	10th	25th	50th	75th	90th	95th	Max
USS	78.03	4.77	63.65	71.60	74.47	77.93	81.57	84.08	86.08	91.53
RSS	78.02	4.75	65	72	74	78	82	84	86	90

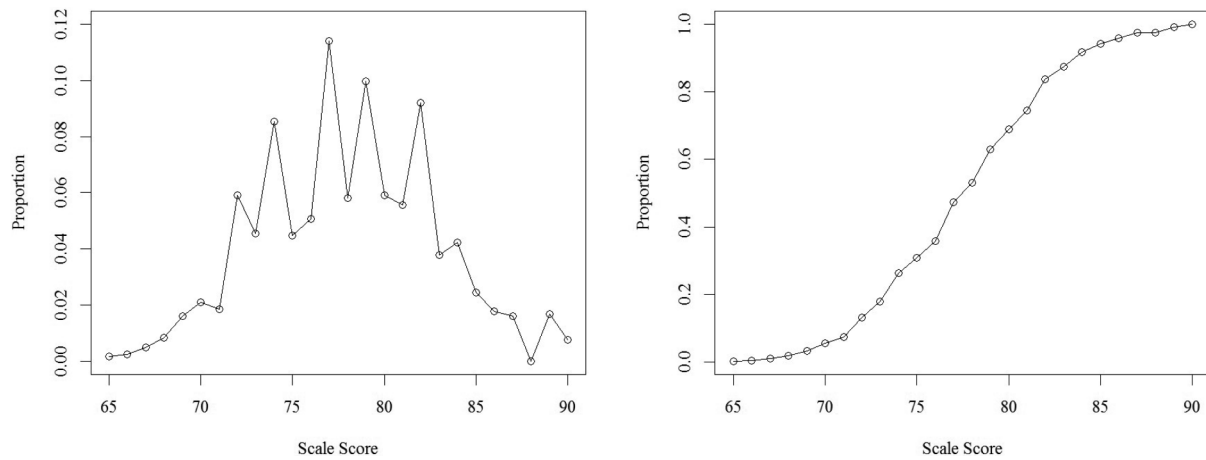


Figure 8.5: Relative Frequency Distribution (left) and Cumulative Frequency Distribution (right)

8.5 Procedures for Establishing the Level Scores

As identified above, when examinees complete the Applied Math assessment, they receive a score report that includes a scale score and a level score. Following the establishment of the score scale, ACT undertook a standard setting process to establish the minimum scale scores required to achieve each of the five Applied Math levels. To establish the minimum scale scores, ACT assembled a panel of SMEs consisting of educators and business people, some of whom are current WorkKeys customers. The Mapmark standard setting method (Schulz & Mitzel, 2005) with Whole Booklet Feedback was used to establish the cut scores for each of the Applied Math score levels.

Mapmark builds on the popular Bookmark procedure (Lewis, Mitzel, Mercado, & Schulz, 2012). The key difference between Mapmark and Bookmark methods is the Item Map contained within the Order Item Booklet (OIB). The OIB contains a sample of items from the Applied Math item pool ordered from easiest to hardest. The Mapmark process includes within the OIB the item map, which provides the difficulty of each item mapped to the actual scale value. The item map, therefore, shows “how much” more difficult one item is than another. In other words, the item map provides additional information on item difficulty.

A total of 77 items were selected to create the OIB. The IRT parameter estimates for all the items in the OIB were calibrated and scaled to the base form. All the items were ranked in order by the corresponding scale score (convert item difficulty to scale score) to form the OIB.

ACT conducted a standard setting study with a panel of SMEs (see Chapter 2 for the credentials of the panel), including appropriate training sessions. The purpose of the standard setting process was to gather data to assist ACT in establishing the standards for achieving a defined performance level on the Applied Math assessment. Because the Applied Math assessment is a criterion-referenced measure, reported scores on the assessment are aligned to the PLDs (see Chapter 2) that a test taker has demonstrated through responding to items on the assessment. Specifically, the purpose is to identify a cut point on the score scale per skill level where examinees who score at or above the point have demonstrated the ability to perform the skills corresponding to that skill level, and examinees who score below the point have not demonstrated the ability to perform the skills. In implementing the Mapmark procedure, ACT instructed the SMEs to define the level scores such that:

- an examinee is expected to correctly respond to at least 67% of the items that belong to his or her reported level.
- an examinee is expected to have demonstrated mastery for all levels below his or her reported level.
- an examinee is NOT expected to correctly respond to more than 67% of the items that belong to levels higher than his or her reported level.

The Mapmark standard setting included a three-round process, with Whole Booklet Feedback. For each of three rounds, the SMEs set cut scores for each level. In Round 1, the SMEs (a) took the Applied Math assessment, (b) reviewed the Applied Math PLDs, (c) reviewed test items and their associated scale scores, (d) linked test items to the PLDs, and (e) placed bookmarks in the OIB for each level. Specifically, the panelists were asked to divide the items for each skill level into two groups—those items that they felt were easy enough for a minimally qualified examinee in the skill level to have mastered,

and those items that were too difficult for a minimally qualified examinee to have mastered. In this context, mastery was defined as having a 2-in-3 chance of success (or a response probability of .67) on the item. This was done to establish the initial cut scores for the five levels (e.g., Levels 3–7).

In Round 2, the panelists received feedback regarding their bookmark placement relative to recommended scale scores on the item map scale and to the group’s median cut score. The group was then provided with Whole Booklet Feedback. Specifically, they were provided with data showing how 16 test takers (two test takers in each level and one test taker between each level) answered each of the items on Form M2C_S1. Data was provided for two examinees that scored at or near the Round 1 cut score for each skill level and data for a borderline examinee at each level. The purpose was to help the panelists understand what examinees at the Round 1 cut scores “can” do and consider whether this is what examinees “should” be able to do according to the PLD for each skill level. Using all of this information, panelists were asked to repeat the process of placing bookmarks in the OIB for each level.

In Round 3, the panelists received feedback regarding their bookmark placement in Round 2. The feedback included consequences or impact data showing the percentage of examinees performing at or above the cut scores set for each skill level. ACT emphasized to the panelists that the PLDs should take precedence since the assessment is criterion-referenced. With that, they set their bookmarks for the third round.

During the final meeting, the panelists reviewed the Item Map with lines representing the Round 3 median cut scores drawn on the map. Next, they received instructions for recording the Round 3 cut scores in their OIB, and reviewed a Cut Score Distribution Chart showing the distribution of panelists’ Round 3 cut scores across all the skill levels. Finally, the panelists discussed consequences data based on the final cut scores. Following these discussions, the panelists approved the final median cut score to define the five performance levels.

ACT reviewed the work of the Standard Setting panelists and evaluated whether the work of the panelists achieved the desired result of a criterion-referenced assessment with level scores aligned to the PLDs. After reviewing the panelists’ work and recommendations, the cut scores for the five levels were approved for the Applied Math assessment. The final median cut scores will be used to define each performance level on the Applied Math assessment, and the cut scores are presented in Table 8.2.

Table 8.2: Median Cut Scores for Applied Math Assessment

Final Scale Score Cut Points			
Levels	Median Cut	Range of Median Cut	
		Min	Max
Level 3	72	72	72
Level 4	76	74	78
Level 5	80	78	81
Level 6	83	83	84
Level 7	86	86	89

With the establishment of the scale scores and cut scores, new forms will be built to be parallel based on the test specifications (see Chapter 3) and will be equated to the base form to achieve score comparability. As a result, scale scores and level scores for different forms of the Applied Math assessment will be comparable (see Chapter 9).

Chapter 9

Equating and Linking

This chapter contains three sections. The first section describes the equating methods used for the ACT[®] WorkKeys[®] Applied Math assessment. Because multiple alternate forms of the Applied Math assessment are required, ACT applies equating methods to ensure that scores from different forms are interchangeable and comparable across forms. The second section reports the findings of the mode comparability study. ACT administers the ACT[®] WorkKeys[®] NCRC[®] assessments in both paper and online formats. The mode comparability study was conducted to learn if scores earned by an examinee using the paper mode are interchangeable and comparable to scores earned by an examinee using the online mode. The third section presents the findings of a linking study to provide concordance scale scores between the previous version of Applied Mathematics (AM 1.0) and current Applied Math (AM 2.0) assessments. WorkKeys test users want to understand the relationship between scores earned on the Applied Mathematics assessments and scores earned on the Applied Math assessments. Although scores earned on the Applied Math assessment are not interchangeable with scores earned on the Applied Mathematics assessment, the linking study will assist users in understanding the relationship of the current assessment to the previous assessment.

9.1 Equating Method and Procedures

New test forms for the WorkKeys Applied Math assessment are developed on a regular basis to ensure the fairness and security of the test scores. Though each form is constructed to meet the same content (see Chapter 3 for the detailed content blueprint) and statistical specifications, the forms may differ slightly in form difficulty. Equating is the process of making statistical adjustments to achieve score interchangeability across the forms so that the reported scale scores have the same meaning regardless of the forms administered (Kolen & Brennan, 2014). Using Item Response Theory (IRT) true-score equating, the Applied Math forms are either pre-equated or post-equated to produce scale scores and level scores. Pre-equating refers to the process by which conversions from raw to scale scores are established prior to test delivery. Pre-equating enables test takers to receive their score reports in a relatively short period of time following testing. To construct an Applied Math new test form, items are

selected from an item pool which meets the content classification specifications and the item statistical specifications. Test development content specialists and research psychometric specialists review the proposed form to ensure that it meets the complete test specifications. After item selection is approved and finalized, ACT applies pre-equating to derive the raw-to-scale score conversion table (see greater detail about skill level and scale scores in Chapter 8). However, if pre-equating cannot be applied due to a lack of calibrated item statistics, post-equating can be conducted following the test administrations, assuming a sufficient number of examinees have taken the assessment.

To be able to apply pre-equating to a newly developed form, all items in the form need IRT-calibrated parameter estimates that have been placed on the same scale. For the Applied Math assessment, ACT is continually developing new items. When newly developed items have been reviewed and approved, they are embedded as pretest items in operational form administrations (see Chapter 8). ACT routinely conducts item calibrations using a three-parameter logistic (3-PL) IRT model. The Stocking-Lord method (Stocking & Lord, 1983) is used to place the item parameter estimates, including those for pretest items, onto the same scale. After each form calibration, the item statistics are reviewed in terms of classical test theory (CTT) and IRT. For example, items with very low discrimination indices (e.g., point biserial correlation or IRT a -parameter estimate) or extreme difficulty indices (e.g., p -value or IRT b -parameter estimate) are either archived or revised for additional pretesting. Through the process of item development, pretesting, and calibrations, new items whose content and statistical properties are reviewed and found to be acceptable, are added to the WorkKeys item pool which is continually expanded and maintained.

In addition, ACT periodically reviews the item pool for the purpose of archiving outdated or overused items. ACT also monitors the stability of item parameters to ensure that all items contained in the pool are suitable for the assembly of new test forms.

9.2 Mode Comparability

ACT developed the Applied Math assessment to be administered using both paper and online formats. The *Standards for Educational and Psychological Testing* (AERA et al., 2014) state that evidence supporting score interpretations and uses should be provided when a testing program maintains test forms “administered under different test administration conditions are comparable for the same purpose” (see standard 5.17 of *the Standards*) (AERA et al., 2014, p. 106).

Mroch, Li, and Thompson (2015) proposed a framework of score comparability focusing on construct and score equivalence, while considering a variety of test conditions. For the Applied Math assessment, forms are built independently of test mode, using the same item pool and test specifications. ACT applies the same test equating methods for both paper and online forms to derive raw-to-scale score conversions. The mode comparability for the Applied Math assessment includes an evaluation of items, scores, and score conversions.

9.2.1 Mode Comparability: Study Design

ACT conducted a field study to evaluate the comparability of scores between paper and online administrations. In the field study, test centers were to randomly assign examinees to one of three proposed testing conditions. ACT directed the proctors to randomly assign test takers to take one of the three test forms: an Applied Math online Form (M2C_LM1), an Applied Math paper Form (M2P_LM2), or an Applied Mathematics online Form (M1C_LM3). Examinees responded to the items on Forms M2C_LM1 and M2P_LM2 were used to evaluate mode comparability, and examinees responded to items on Forms M2C_LM1 and M1C_LM3 were used for the Linking Study. ACT directed the centers to have each test taker take all three WorkKeys NCRC assessments on the same or different days, with the test order counterbalanced across the sites. The test takers also completed a survey regarding their testing experience either at the end of each online assessment or after finishing all three paper assessments.

9.2.2 Mode Comparability: Sample

Similar to the scaling study presented in Chapter 8, ACT recruited a sample of examinees representative of the WorkKeys test-taker population.

Although ACT had instructed test centers to randomly assign examinees to the three conditions, ACT discovered that in some cases these instructions were not followed. Consequently, ACT did extensive review and cleaning of the test data. ACT removed data from a few centers where examinee distribution in the three conditions was extremely unbalanced (ACT defined an unbalanced test center as a center with a difference of 10 or more examinees between the different test conditions). Following data cleaning, ACT conducted further reviews to ensure that the remaining data represented random equivalent groups. A total of 37 testing sites participated in this study including 10 high schools and 27 adult testing centers across 20 states from different regions. Because the data may contain additional sampling error, measurement precision may be affected. As a result, the interpretations of the results below should be made with caution.

Final examinee counts were 688 and 667 for online (Form M2C_LM1) and paper (Form M2P_LM2) testing conditions, respectively. Table 9.1 presents the demographic distribution information. In general, the recruited samples for the two mode conditions are acceptable to represent the current WorkKeys test population, and are quite similar except for Caucasian groups (64% vs. 57% for online and paper testing).

Table 9.1: Sample Demographic Information for the Two Delivery Modes

Mode	N	M (SD)	Gender		Sample		Ethnicity		
			F	M	HS	AD	W	B	H
Online	688	19.37 (7.07)	54%	45%	46%	54%	64%	15%	9%
Paper	667	19.38 (6.87)	52%	44%	46%	54%	57%	15%	9%

Note. None-respondent or multi-races not included; F = Female; M = Male; HS = High Schooler; AD = Adult; W = Caucasian; B = African American; H = Hispanic.

Across two mode conditions, the omit rates (no-answer) at each item are compared. As shown in Figure 9.1, the omit rates are generally below 10% for both conditions except for the last item. The omit rates tend to be slightly higher from the paper form than the online form.

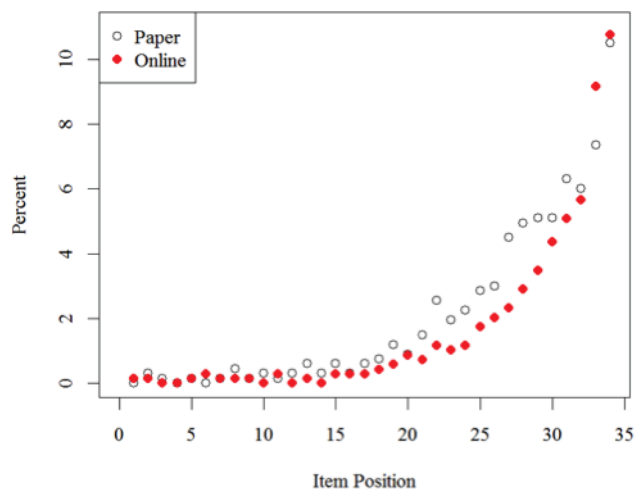


Figure 9.1: Comparison of Item Omit Rates for the Two Delivery Modes

9.2.3 Mode Comparability: Comparisons on Items, Tests, and Score Conversions

Item Level Comparison. Separate calibrations were conducted for the online and paper forms, and the item parameter estimates were transformed to the same pool scale. Table 9.2 shows the summary

statistics between the online and paper forms, and Figure 9.2 presents the scatterplots of item p-values and IRT *b*-parameter estimates. These results indicate that the items statistics were similar across the two mode conditions.

Table 9.2: Test Summary Statistics for Applied Math

Mode	P	PBIS	IRT-a	IRT-b	IRT-c
Online	0.625 (0.206)	0.521 (0.113)	1.152 (0.309)	0.428 (1.317)	0.155 (0.056)
Paper	0.625 (0.213)	0.512 (0.101)	1.102 (0.259)	0.448 (1.390)	0.151 (0.044)

Note. P = p-value; PBIS = point biserial correlation; standard deviations are in parentheses.

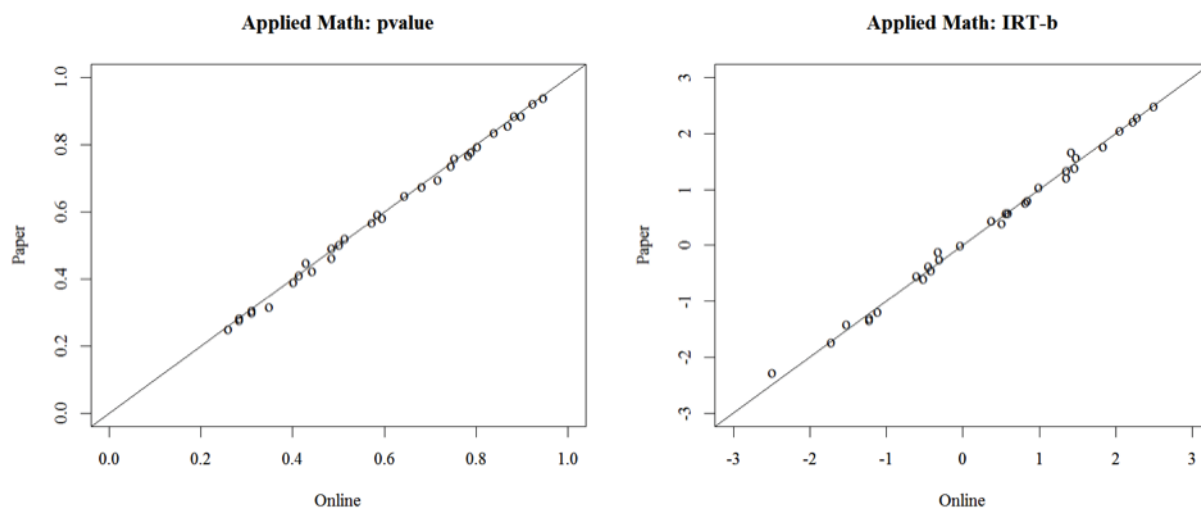


Figure 9.2: Scatterplots of Item p-values (left) and IRT *b*-parameter estimates (right) for the Two Delivery Modes

Differential item functioning (DIF) analysis was also conducted on the items between paper and online forms. Only one item is flagged as Category C (favoring paper testing) using the Mantel-Haenszel method.

Test Comparison. Figure 9.3 shows the comparisons of the Test Characteristics Curve (TCC) and Test Information Function (TIF). The TCCs are almost identical and the TIFs are very similar between modes, which indicate that the average mode effect is negligible.

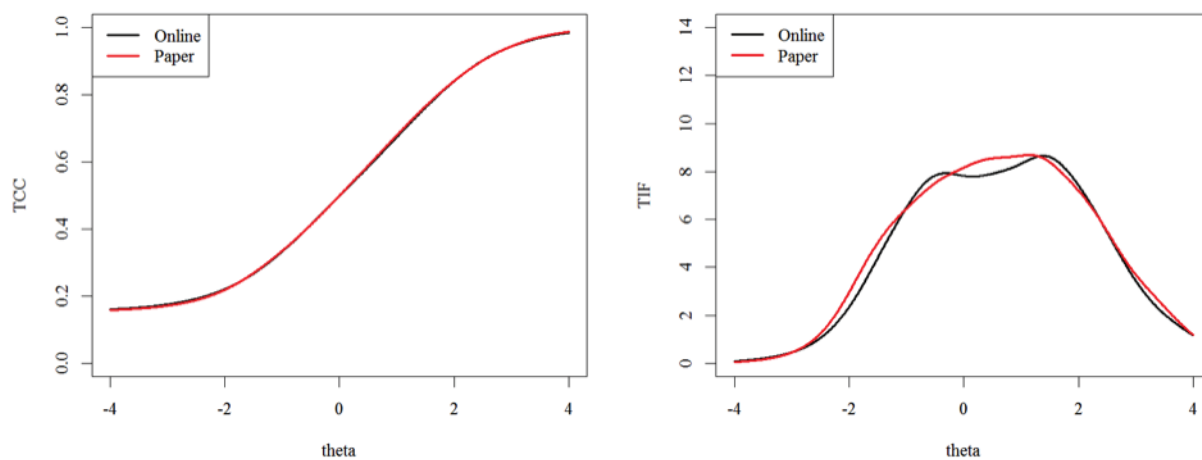


Figure 9.3: Comparisons of Test Characteristic Curves (left) and Test Information Functions (right) for the Two Delivery Modes

Score Conversion Comparison. Figure 9.4 compares the raw-to-scale score conversions. For mean unrounded scale score and level score cut for each level, the absolute differences are below 0.2 for the raw score points of 21 or below, and between 0.24 and 0.49 for the higher raw score points. Only four raw score points differ on reported scale scores between modes mainly due to rounding errors. As for the raw-to-level score conversions between modes, only one raw score discrepancy at the raw score of 21 (corresponding scale score is 79.64) or 22 (corresponding scale score is 80.24) for Level 5 due to rounding error.

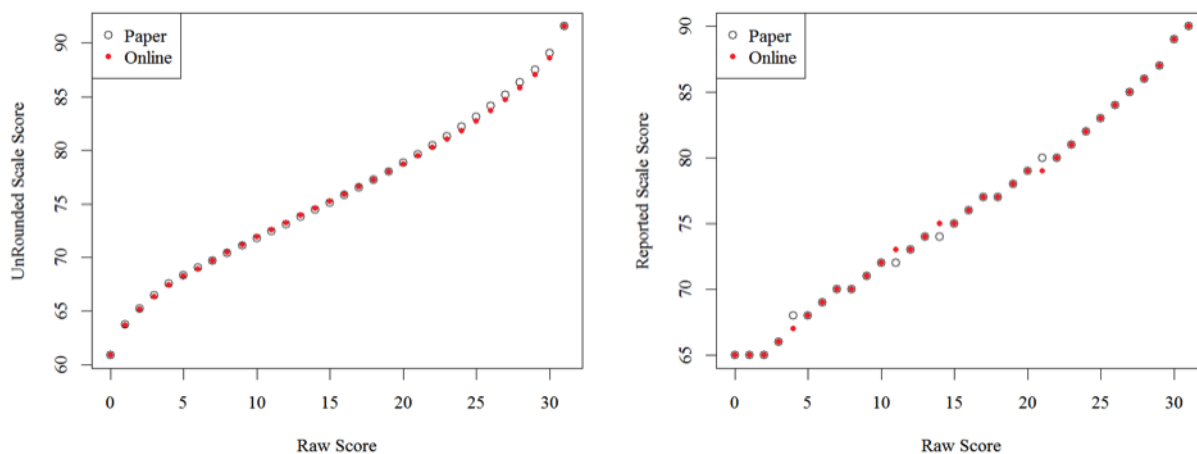


Figure 9.4: Comparisons of Unrounded (left) and Reported (right) Raw-to-Scale Score Conversions for the Two Delivery Modes

Figure 9.5 shows the Conditional Standard Error of Measurements (CSEMs). The raw score CSEMs tend to be larger in the middle and smaller at the two ends and the scale score CSEMs tend to be flat for most of the score points. The CSEMs for both scores appear to be similar between modes.

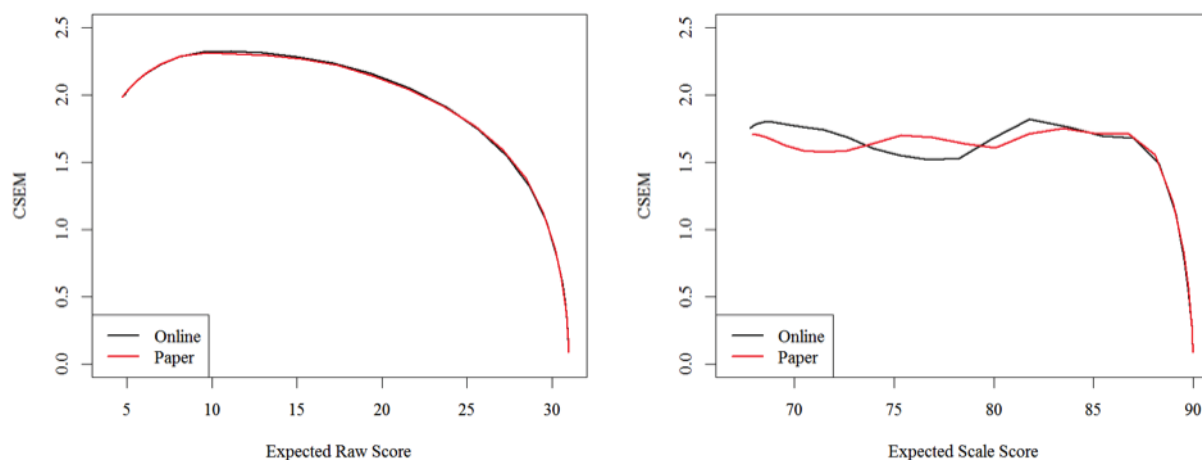


Figure 9.5: Comparisons of CSEMs for Raw Scores (left) and Scale Scores (right) for the Two Delivery Modes

9.2.4 Mode Comparability: Score Comparisons

Table 9.3 presents the summary statistics for the raw and scale scores by mode. Figure 9.6 presents the raw score distributions, and Figure 9.7 presents the scale score distribution. The results are very similar between the two modes. For both types of scores, mean differences are below 0.01 and the effect sizes are below 0.002, indicating nearly identical score distributions.

Table 9.3: Summary for Raw and Scale Scores for the Two Delivery Modes

Score	Mode	M	SD	P10	P25	P50	P75	P90	P95	M Diff.	ES	t-test prob
Raw Scores	Online	19.37	7.07	10	13	20	25	28	30	0.01	0.002	0.969
	Paper	19.38	6.87	10	15	20	25	29	30			
Scale Scores	Online	78.82	5.62	72	74	79	83	86	89	0.00	0.000	0.993
	Paper	78.82	5.52	72	75	79	83	87	89			

Note. M Diff. = mean difference; ES = effect size.

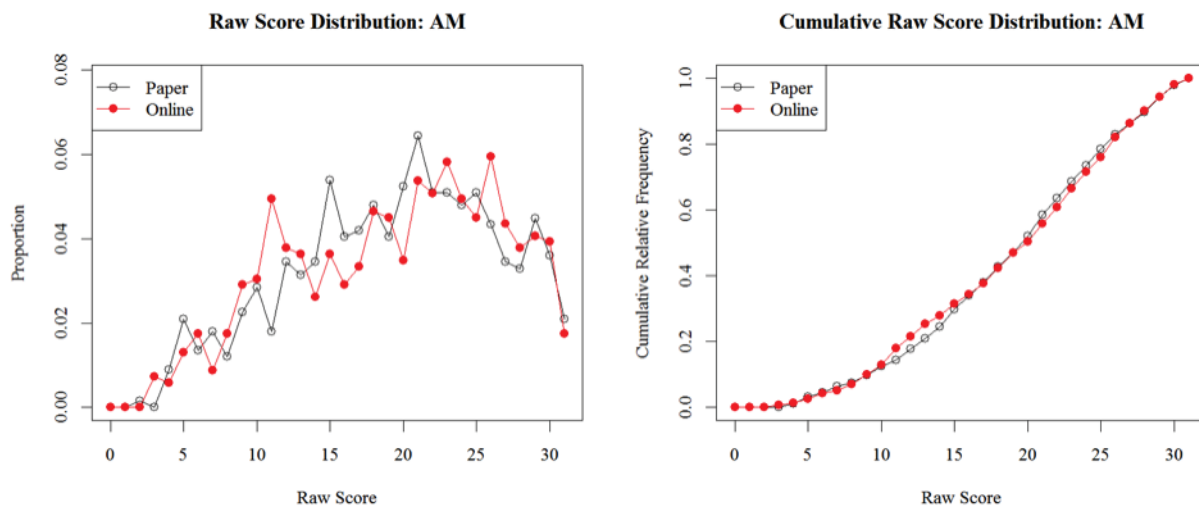


Figure 9.6: Comparison of Raw Score Distributions for the Two Delivery Modes

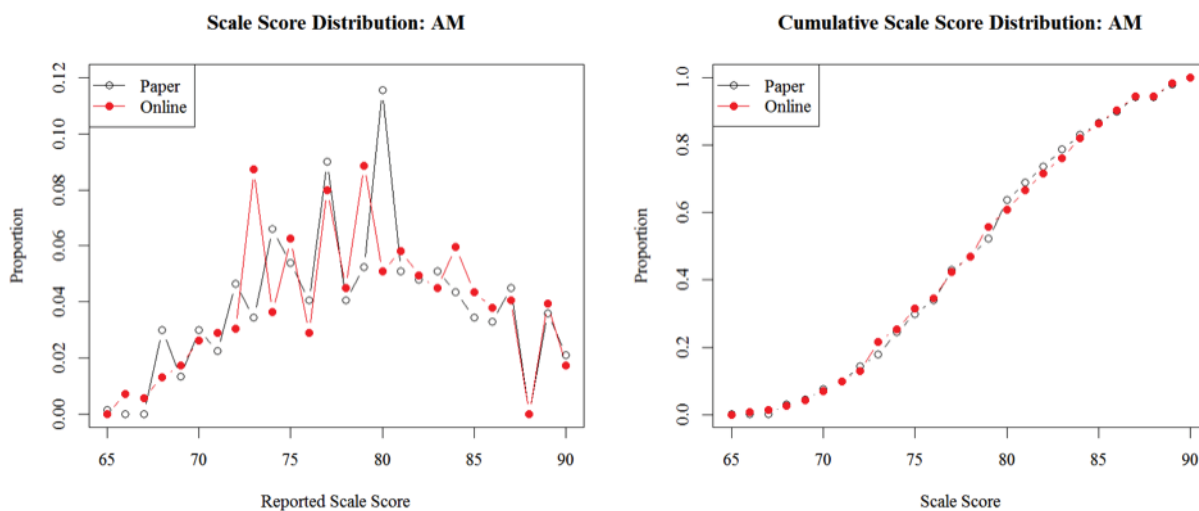


Figure 9.7: Comparison of Scale Score Distributions for the Two Delivery Modes

Based on the findings of the analysis, ACT concluded that no significant mode effect existed. Due to the limitations of the field test data, ACT will continue to monitor the potential mode effects on the Applied Math assessment to ensure the comparability of test scores for paper and online administrations.

9.3 Linking Applied Mathematics to Applied Math Score Scale

When a test publisher needs to modify the test construct, update test specifications, or refresh content to improve an existing assessment, test score users often need to understand the relationships between the old and new assessments. To facilitate a better understanding of the relationship between the different tests or different versions of a test, a statistical procedure is often used to make adjustments to link the scores from one test to another. There are generally four types of linking which are ordered in terms of the “strength” of the resulting relationship: equating, calibration, projection, and moderation (Linn, 1993; Mislevy, 1992). Concordance is a type of statistical moderation of “matching distributions” using percentile ranks to derive a table that links the scores between two tests. Holland (2007) points out that “Concordance represents scaling of tests that are very similar but that were not created with the idea that their scores would be used interchangeably” (p. 19). Different from the equating of two forms of a same test which produces comparable scores, scores from concordance of two tests are *not* interchangeable.

The Applied Math assessment was developed based on modified test specifications of the Applied Mathematics assessment (see Chapter 3 for the test specifications). To facilitate a smooth transition from Applied Mathematics to Applied Math assessments, ACT conducted a Linking Study in the spring of 2017. The focus of the Linking Study was to develop a concordance between Applied Mathematics and Applied Math assessments. Concordance between the two assessments is defined by identifying the scale scores on the Applied Mathematics assessment that have the same percentage of test takers at or below the given scale score points on the Applied Math assessment within the linking study sample. This document summarizes the findings from the Linking Study, as a means to better understand the relationships between the two assessments and ultimately to assist users in appropriately interpreting the scores or score trends derived from the two assessments.

9.3.1 Study Design and Sample Representativeness

A total of 43 testing sites were administered both Forms M2C_LM1 (Applied Math online) and M1C_LM3 (Applied Mathematics online) including 10 high schools and 33 adult testing centers across 20 states. More than 800 test takers took one of the two Linking forms and they were given 55 minutes to complete each test. The sample sizes were similar between the two forms. In general, the recruited sample is representative of the WorkKeys test population based on the demographic characteristics (see Table 9.1).

Although the Applied Math assessment was developed based on modified constructs or specifications from the Applied Mathematics assessment, resulting scores are not interchangeable, it is desirable to have similar difficulty and measurement precision to strengthen the concordances. A series of analyses were conducted to evaluate and compare psychometric properties of the two assessments in terms of omit rates, testing time, scale score summary statistics, reliability, and Standard Error of Measurement (SEM).

9.3.2 Comparison of Omit Rates and Testing Time Between Applied Mathematics and Applied Math

Figure 9.8 presents the omit rates for each item in both Applied Math and Applied Mathematics forms administered in the Linking Study. In general, the figure indicates that the omit rates are less than 10% for most items except for the last item in Applied Math Form M2C_LM1. In addition, as summarized in Table 9.4, test takers on average spent slightly more time on Form M2C_LM1 than on Form M1C_LM3. It should be noted that one more operational item was added to the Applied Math assessment.

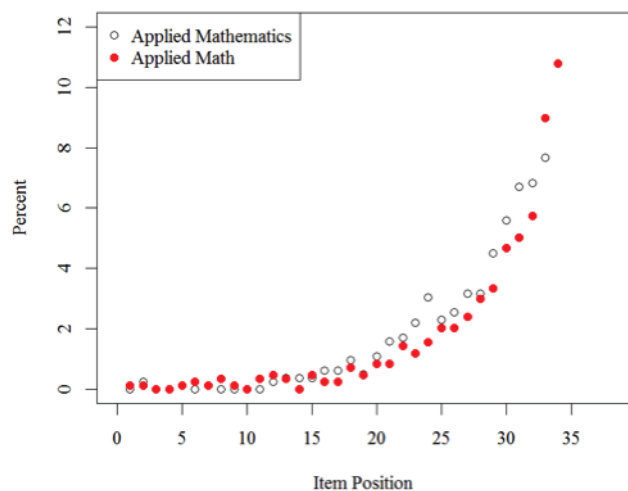


Figure 9.8: Comparison of Item Omit Rates Between Applied Mathematics and Applied Math

Table 9.4: Summary for Total Testing Time (in minutes)—Applied Mathematics and Applied Math

Form	N	Mean (SD)	Min	P5	P10	P25	P50	P75	P90	P95
M1C_LM3	821	37.28 (14.00)	5	11	17	27	39	50	54	55
M2C_LM1	835	37.85 (13.73)	6	11	16	28	40	51	54	54

9.3.3 Scale Score Distributions for Applied Mathematics and Applied Math

Because no significant mode effect was observed in the Mode Study, the item parameter estimates were then re-calibrated using the combined data from both paper and online administrations to derive the conversion for the Applied Math (M2_LM) Form. Tables 9.5 and 9.6 provide the summary statistics for the raw and the scale scores for the Linking Study. Based on average IRT-b statistics, the Applied Math Form, M2_LM, appears to be slightly easier than the Applied Mathematics Form, M1C_LM3.

Table 9.5: Test Summary Statistics for Applied Math and Applied Mathematics

Form	p	PBIS	IRT-a	IRT-b	IRT-c
M2_LM	0.620 (0.214)	0.510 (0.110)	1.120 (0.278)	0.431 (1.350)	0.152 (0.055)
M1C_LM3	0.633 (0.205)	0.492 (0.106)	1.111 (0.315)	0.467 (1.312)	0.171 (0.055)

Note. p = p-value; PBIS = point biserial correlation; standard deviations are in parentheses.

Table 9.6: Scale Scores Summary Statistics for Applied Math and Applied Mathematics

Form	N	Mean (SD)	P5	P10	P25	P50	P75	P90	P95
M2_LM	835	78.67 (5.46)	70	72	75	79	83	86	87
M1C_LM3	821	78.12 (5.87)	68	70	75	78	82	86	87

Figure 9.9 presents the relative frequency distributions (left) and cumulative relative frequency distributions (right) for the Applied Mathematics and Applied Math Forms. These plots suggest that the scale score distributions are similar for two assessments.

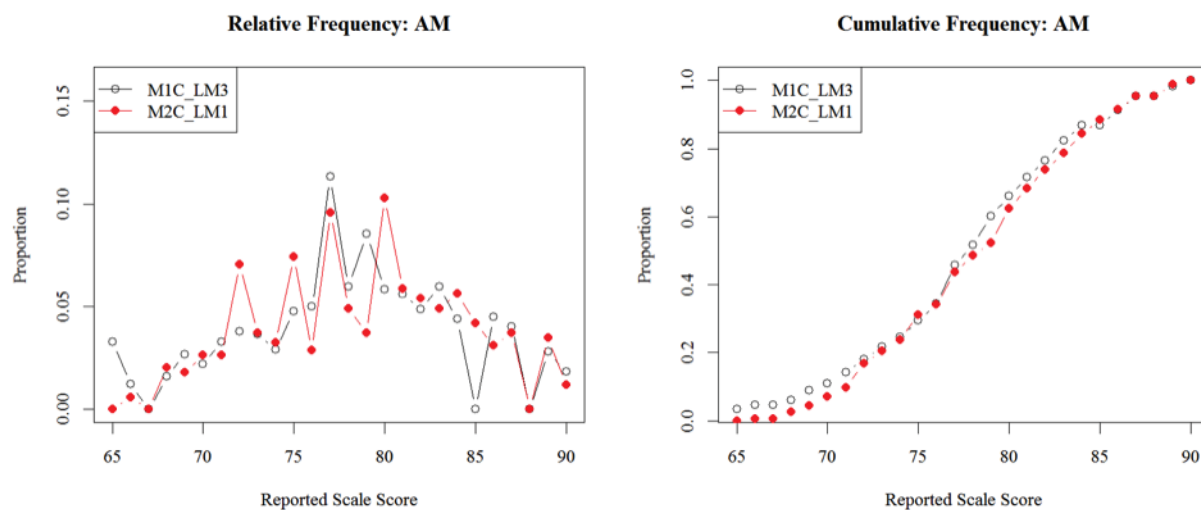


Figure 9.9: Comparison of Relative (left) and Cumulative (right) Frequency Distribution for Applied Mathematics and Applied Math

9.3.4 Concordance from Applied Mathematics to Applied Math

Given the changes in test specifications and the need to link the Applied Mathematics and Applied Math assessments, statistical moderations using an equating method were performed to link scores from Applied Mathematics (AM 1.0) to Applied Math (AM 2.0) assessments. The concordance was based on the equipercentile method with smoothing (S) of 0.05 for Applied Mathematics to Applied Math.

9.3.5 Evaluation of Applied Mathematics Forms After Linking

Table 9.7 provides the summary statistics of the scale scores for the original Applied Mathematics Form (M1C_LM3) before and after it was transformed to the Applied Math scale (M1C_LM3*), and the Applied Math Form (M2_LM). It can be observed that the means, standard deviations, and quantiles of the transformed scale score on the Applied Mathematics Form (M1C_LM3*) are very similar to the Applied Math Form (M2_LM).

Table 9.7: Summary Statistics of Scale Scores Before and After Concordance

Scale	Form	N	Mean (SD)	P10	P25	P50	P75	P90	P95
AM 1.0	M1C_LM3	821	78.12 (5.87)	70	75	78	82	86	87
AM 2.0	M1C_LM3*	821	78.60 (5.56)	71	76	79	82	86	87
AM 2.0	M2_LM	835	78.67 (5.46)	72	75	79	83	86	87

Note. M1C_LM3* = M1C_LM3 implemented AM 2.0 scale score concordance table.

Table 9.8 provides summary statistics of the Level Scores for the previous version of the Applied Mathematics Form (M1C_LM3) before and after it was transformed to the Applied Math scale (M1C_LM3*), and the Applied Math Form (M2_LM). The means and standard deviations are very similar between M1C_LM3* and M2_LM, except for the P10, P25, and P75 quantiles. The Level cuts for the Applied Math assessment were developed based on a standard setting study using a Mapmark method (see Chapter 8 for greater detail on the Standard Setting process).

Table 9.8: Summary for Level Scores Before and After Concordance

Scale	Form	N	Mean (SD)	P10	P25	P50	P75	P90	P95
AM 1.0	M1C_LM3	821	4.34 (1.90)	<3	4	5	6	6	7
AM 2.0	M1C_LM3*	821	4.19 (1.90)	<3	4	4	5	7	7
AM 2.0	M2_LM	835	4.28 (1.88)	3	3	4	6	7	7

The results suggest that in order to compare the scores from the Applied Mathematics and Applied Math assessments and to understand the score relationships between the two assessments, the scale scores on the Applied Mathematics assessment need to first be transformed to the Applied Math scale based on the concordance table. Test users need to be aware that the concordance scale scores do not always represent the test scores that a test taker would achieve if he or she were to take the Applied Math assessment. Similarly, comparing group performance averages or analyzing year-to-year performance trends using concordance scores from a test that has not been taken need to be made with a good deal of caution.

Chapter 10

Reliability and Measurement Error

10.1 Overview

This chapter reports the reliability evidence of the WorkKeys[®] Applied Math assessment. Reliability and measurement error are fundamental for evaluating the psychometric qualities of an assessment in order for the assessment claims defined in Chapter 1 to be substantiated. As the *Standards for Educational and Psychological Testing* (referred to as *the Standards* below) states, “for each total score, subscore, or combination of scores that is to be interpreted, estimates of relevant indices of reliability/precision should be reported” (AERA et al., 2014, p. 43).

According to *the Standards*, reliability is the degree to which test scores for a group of test takers are consistent over repeated applications of a measurement procedure and hence are inferred to be dependable and consistent for an individual test taker; the degree to which scores are free of random errors of measurement for a given group (AERA et al., 2014). As a quantitative measure of the consistency of an assessment, reliability is closely related to Standard Error of Measurement (SEM). SEM is the standard deviation of an individual’s observed scores from repeated administrations of a test (or parallel forms of a test) under identical conditions (AERA et al., 2014). The SEM summarizes the amount of error or inconsistency in test scores.

Because any WorkKeys foundational skill assessment, including Applied Math assessment, classifies examinees into skill-level groups, classification consistency is important to support level score uses. Classification consistency is defined as the extent to which the classification of examinees into groups is identical when obtained from two independent administrations of a single form or two parallel forms of a test. Because assessments are usually administered only on one occasion to the same examinee, classification consistency is estimated from a single test administration with strong assumptions made about distributions of measurement errors and true scores.

The following sections provide results related to (a) reliability coefficients and SEM estimates of raw scores and scale scores based on Classical Test Theory, (b) reliability coefficients of level scores based on Generalizability Theory, and (c) classification consistency of level scores.

10.2 Reliability Coefficients and Standard Error of Measurement (SEM)

Reliability coefficients quantify the consistency level of test scores. They typically range from zero to one, with values near one indicating high consistency and those near zero indicating little or no consistency. Based on a single test administration, internal consistency reliability, usually measured by Coefficient Alpha (Cronbach, 1951), is one of the most widely used indices of test score reliability. Coefficient Alpha is computed as a reliability estimate for raw scores using the following formula:

$$\hat{\alpha} = \left(\frac{k}{k-1} \right) \left(1 - \frac{\sum_{i=1}^k s_i^2}{s_x^2} \right),$$

where k is the number of test items used for scoring, s_i^2 is the sample variance of the i^{th} item, and s_x^2 is the sample variance of the observed raw score.

For scale scores of test t , the reliability estimate (r_t) can be obtained using the following formula:

$$r_t = 1 - \frac{SEM_t^2}{s_t^2},$$

where SEM_t is the average of estimated scale score CSEMs and s_t^2 is the sample variance of the observed scale score. Scale score SEMs were estimated using a four-parameter beta compound binomial model (Kolen, Hanson, & Brennan, 1992). If the distribution of measurement error is approximated by a normal distribution, true scale scores for about two-thirds of the test-taker group are within plus or minus one SEM of their scale score.

Table 10.1 presents the Coefficient Alphas and the SEMs for the Applied Math assessment for both raw scores and scale scores. The reliability and SEM estimates are based on the sample utilized for the Scaling Study described in Chapter 8. The sample included 1,185 examinees following data cleaning. For score use, a minimum value of 0.80 is required for reliable test score interpretations. The reliability estimates for both the raw and scale scores exceed the threshold of 0.80. (Corresponding plots of Conditional Standard Error of Measurement (CSEM) on raw scores and scale scores are presented in Chapter 8.)

Table 10.1: Coefficient Alphas and SEMs for Applied Math Form M2C_S1

Form	N	Raw Score		Scale Score	
		Coefficient Alpha	SEM	Coefficient Alpha	SEM
Form M2C_S1	1,185	0.88	2.16	0.89	1.61

10.3 Generalizability Theory

Reliability based on Generalizability Theory was also investigated. Generalizability Theory provides a broad conceptual and statistical framework for evaluating measurement precision (Cronbach, Gleser, Nanda, & Rajaratnam, 1972). Generalizability Theory not only produces reliability-like coefficients known as generalizability and dependability coefficients but also disentangles and estimates multiple sources of error. Multivariate generalizability theory (Brennan, 2001) can address issues involved in analyzing data for a stratified test under a table of specifications. In Applied Math forms, items are nested (stratified) within specific levels of difficulty, that is, Levels 3 to 7. A mixed model of *persons* \times (*items:strata*) or $p \times (i:h)$ from a multivariate perspective was used, and the results are presented in Table 10.2 with the following highlights:

- The estimated universe score variance which is analogous to the true score variance, $\hat{\sigma}^2(p)$, is relatively larger at the middle levels of items, suggesting that the average performances can be differentiated more on the moderately difficult items than the easy or difficult items;
- Variability of item difficulty, $\hat{\sigma}^2(i)$, is small, suggesting that difficulty is similar among items within each level;
- Interactions of person-by-item, $\hat{\sigma}^2(pi)$, are greater for the items at Levels 5 to 7 than those at Levels 3 and 4, indicating that performance is less consistent across the items at Levels 5 to 7 than at Levels 3 or 4;
- The estimates of error variances, $\hat{\sigma}^2(\delta)$ for norm-reference decisions and $\hat{\sigma}^2(\Delta)$ for criterion-reference decisions, are similar due to the small $\hat{\sigma}^2(i)$;
- The reliability-like coefficients, $E\hat{\rho}^2$ for norm-reference decisions and $\hat{\Phi}$ for criterion-reference decisions, are 0.52 or higher at each level with Level 7 having the lowest value;
- The estimated effective weights which indicate relative contributions of each level of items to the total variance are higher for the middle levels (Levels 4 through 6) than for Levels 3 and 7. The results suggest that moderately difficult items are more heavily weighted in forming the total scores than the other items in the test;
- For total scores, the reliability-like coefficients for both rank-ordering test takers and judging performance levels of test takers are 0.89 and 0.88, respectively.

Table 10.2 Estimated Variance Components, Error Variances, and Generalizability Coefficients at Each Level for Applied Math Form M2C_S1

Level	I	$\sigma^2(p)$	$\hat{\sigma}^2(i)$	$\hat{\sigma}^2(pi)$	$\hat{\sigma}^2(\delta)$	$\hat{\sigma}^2(\Delta)$	$E\hat{\rho}^2$	$\hat{\Phi}$	Effective Weight
3	6	0.027	0.000	0.010	0.010	0.010	0.73	0.73	0.12
4	6	0.061	0.001	0.022	0.022	0.023	0.73	0.73	0.24
5	7	0.059	0.002	0.025	0.025	0.027	0.70	0.68	0.28
6	6	0.058	0.001	0.031	0.031	0.032	0.65	0.64	0.23
7	6	0.028	0.001	0.025	0.025	0.026	0.52	0.52	0.13

10.4 Classification Consistency of Level Scores

The Standards (AERA et al., 2014, p. 46 as Standard 2.16) recommends that test publishers provide information about the percentage of test takers who would be classified in the same way for classification tests if they were to take a test twice using alternate forms. Classification consistency ranges from 0 to 100 percent, with values near 100 indicating higher consistency and those near zero indicating little or no consistency.

According to Subkoviak (1984), two important classification consistency indices are:

- agreement index p , which is the proportion of consistent classification based on two parallel forms, and
- coefficient κ , which is the proportion of consistent classification adjusted for chance agreement.

The classification consistency indices computed using the IRT methodology (Schulz, Kolen, & Nicewander, 1997, 1999) for Applied Math Form M2C_S1 data are presented in Table 10.3. The second row of the table, labeled “Exact,” shows the percentages of test takers who would receive the same level score from two parallel forms. For example, if a test taker were to take two parallel forms of the test and score at Level 3 on both forms, this would be a case of exact agreement. For Applied Math Form M2C_S1, the estimated exact agreement is 57 percent. The remaining rows show the consistency of aggregated classifications (i.e., at-or-above) at each level. Aggregated classification consistency for a level score is the summary of test-taker percentages of two groups: Both scores are either below the level score, or at-or-above it. For example, a test taker who scores at Level 4 and Level 5 on two testing occasions would not be consistently classified as Level 5, but would be consistently classified as Level 4 or above. In this study, aggregated classification consistency of level scores is estimated to be 87 percent or higher. As expected, the values of coefficient κ are lower than those of agreement index p .

Estimates of classification consistency are sensitive to the distribution of skill levels in the test taker sample. For example, the mean of the test taker sample is between the Level 4 and Level 5 theta cutoff, suggesting that the true skill of a relatively large proportion of these test takers was close to the two θ cutoffs. Generally, test takers are more likely to be misclassified because of measurement error when their true skill is closer to the cutoff.

Table 10.3: Estimated Classification Consistency Indices for Level Scores for Form M2C_S1

Level	p	κ
Exact	57%	45%
3	94%	53%
4	87%	69%
5	87%	72%
6	91%	68%
7	96%	65%

In summary, the reliability and classification consistency findings above are deemed acceptable based on the available field study data presented in Chapter 8. As the Applied Math assessment is administered to large numbers of examinees, ACT will continue to update the findings related to test score reliability and classification consistency.

Chapter 11

Validity

11.1 Validation of Test Score Uses and Interpretations

The *Standards for Educational and Psychological Testing* (AERA et al., 2014) define validity as “the degree to which evidence and theory support the interpretations of test scores for proposed uses” (p. 11). In adhering to this understanding of validity, the ACT[®] WorkKeys[®] Assessments incorporated an approach of gathering evidence as a means to enable users to evaluate the appropriateness and reasonableness of test score interpretations and uses.

To validate test score interpretations and/or uses is to review and evaluate the plausibility of the claims made regarding the test and its scores. Kane (2013) maintained that an argument-based approach to validation requires that the score-based claims be clearly articulated along with their associated inferences and assumptions. Validation henceforth becomes a scientific process designed to evaluate the degree to which the analytic and empirical evidence supports the assessment claims.

Validation, as a scientific process, entails the careful articulation of test claims along with the inferences and assumptions required to build the connections from examinee task performance to score-based interpretations and uses. The assessment claims are explicit statements regarding the purpose of the assessment and how test scores are to be interpreted and used. As such, the claims provide the framework for validation. When clearly specified, an evidentiary chain is built between the claims and associated evidence. If the claims are rational, and their associated inferences and assumptions are plausible based on evidence, then the defined test score uses should also be considered plausible or valid (Kane, 2013; Messick, 1989).

Validation of test score interpretations and uses through the evaluation of evidence does not lead to a Yes/No validity determination. Validation is a matter of degree, requiring interpretation and insight into the underlying theory supporting the meaning of the test scores and the potential uses and consequences of score-based decisions. As several theorists have argued, a test may be interpreted as appropriate and

valid for one usage, but altogether inappropriate and problematic for a second usage. As a result, it is the usage and decisions stemming from test scores that are validated and not the test itself (Cronbach, 1988; Kane, 2006; Messick, 1989).

In collecting and evaluating evidence regarding Applied Math test score interpretations and usage, WorkKeys Assessments subscribed to the concept of validity as a claims-based argument (Cronbach, 1988; Kane 2006, 2013; Mislavy, 2006). In adhering to a claims-based validation approach, WorkKeys Assessments also utilized the principles of Design Science (Johannesson & Perjons, 2014; Van Aken & Romme, 2012) as a means of clearly defining the assessment problem, developing proposed solutions, gathering feedback and test data, and documenting evidence and decision making.

The Applied Math Design Team implemented a process that began by articulating the purpose of the assessment and its associated claims; it culminated with the collection of data from various sources to evaluate the validity use argument. The purpose of the validity chapter is to present the Applied Math assessment claims and assumptions, then provide evidence to evaluate the appropriateness of the proposed interpretations and uses.

11.2 Purpose of the Applied Math Assessment

The Applied Math assessment provides information to examinees, employers, workforce development officials, and educators. For examinees, the assessment provides them with insights in regards to their foundational applied mathematics skills and their career readiness. In some cases, scores on the assessment may assist examinees in finding employment. For employers, the assessment provides information that may be used, with other information, for employment decisions. For workforce development officials, the assessment provides information regarding the work-ready status of individuals requesting services and also assists them in guiding individuals toward jobs. For secondary educators, the assessment provides information related to foundational skills and career readiness that may be used as an accountability measure. For postsecondary educators, the assessment provides information related to program readiness or program evaluation. For the assessment to be used appropriately for each of these purposes, ACT needs to collect evidence and evaluate it. Additionally, ACT needs to provide guidance in regards to the proper use of the assessment for each purpose.

An additional purpose of the Applied Math assessment relates to the issuance of the ACT WorkKeys National Career Readiness Certificate (NCRC®). The assessment constitutes one of three assessments that are used to determine an examinee's achievement of a WorkKeys NCRC. The WorkKeys NCRC is an evidence-based career readiness credential, which assists both examinees and employers in various ways. For the examinee, the WorkKeys NCRC provides them with a better understanding of their level of foundational skills. The WorkKeys NCRC level and assessment scores provide both examinees and counselors with insights in regard to their skill levels and how these relate to various occupations.

WorkKeys developed the Applied Math assessment as an updated version of the WorkKeys Applied Mathematics assessment. Both the original Applied Mathematics assessment and the updated assessment measure examinees' ability to apply mathematical skills to work-related situations in order to solve a problem (ACT, 2008). The updated Applied Math assessment measures these same work-related skills, but updates the contexts and, at higher levels, includes a few additional skills. As such, scores on Applied Math cannot be used interchangeably with scores from the previous assessment of Applied Mathematics.

Using data and knowledge gained through over 20 years of administering the Applied Mathematics assessment, ACT was able to more fully develop the updated assessment's construct and content. At the lower levels, the assessment requires examinees to apply mathematical skills to work-related scenarios in a similar manner as Applied Mathematics. As the examinee works through the assessment, however, new types of skills are assessed. The updated assessment measures the examinee's ability to identify where errors occurred, identify correct equations for spreadsheets, and interpret results. These are work-related mathematical skills that go beyond computation.

The WorkKeys assessment program was conceived to mitigate the “skills gap” problem. The skills gap is a term used to describe the challenge that employers and hiring managers face. The skills gap occurs because many well-paying jobs exist; but, due to the shortage of qualified workers, employers are unable to find workers to fill them. Goldin and Katz (2008) provide evidence demonstrating that, since 1970, United States educational achievement has increased only marginally while technological advances and requirements in business and industry have increased greatly. Many of the problems associated with businesses being unable to find quality workers is the result of average worker skill levels being little better than the skill levels of 40 years ago. As a result, a discrepancy exists between employer needs and the skill sets many workers bring to the job (Autor, 2015; Goldin & Katz, 2008). (For more detailed information on the skills gaps, see Chapter 1.)

Because of the discrepancy between educational achievement and job requirements, WorkKeys provided a means of addressing the skills gap for both employers and workers (ACT, 2011). Through the use of WorkKeys assessments and the WorkKeys NCRC, workers can demonstrate the foundational skills needed in today's economy. For the employer, WorkKeys assessment scores allow them to use skills-based hiring practices as a means of identifying the right person for the job.

11.3 Applied Math Assessment Claims

Drawing on its understanding of the skills gap and skills-based hiring practices, the Design Team developed three primary claims for the Applied Math assessment.

Claim #1: U.S. examinees of high school or workforce age who demonstrate scores that reach at least a given level on the Applied Math assessment are more likely to successfully perform in more and higher levels of U.S. jobs (in the ACT job taxonomy) than examinees whose scores do not reach that level.

Claim #1 Assumptions:

1. Applied Math is a component of foundational workplace skills, and it is required for success in a large number of jobs (based on ACT's job profile database).
2. ACT has developed a professionally valid and appropriate definition of the applied mathematics construct.
3. ACT's Applied Math assessment provides reliable and interpretable scores that reflect the construct. ACT's Applied Math assessment elicits observable evidence of the construct.
4. ACT has defined workplace appropriate Applied Math performance level descriptors (PLDs), and ACT has established standards (e.g., cut points) aligned to the PLDs.
5. Cut scores used to delineate each performance level have sufficient classification accuracy.

6. Businesses and employers are able to validly measure employee performance.
7. Scores on the Applied Math assessment are positively related to measures of employee performance, including productivity and turnover rates.
8. Examinees who score well on Applied Math are more likely to receive higher performance ratings and are more likely to have greater job success (defined as job retention and performance evaluations) than lower scoring examinees.

Claim #2: U.S. companies who hire U.S. examinees of high school or workforce age who demonstrate scores that reach at least a given level on the Applied Math assessment are more likely to achieve greater gains in productivity (for example, measured as increased output per day) from new employees than if the company had hired examinees whose scores do not reach that level.

Claim #2 Assumptions:

1. Claim #1 Assumptions 1–7
2. Employees who possess higher foundational workplace skills (as defined by ACT) are more likely to be productive and effective workers (as defined by supervisor evaluations) than employees who possess lower foundational workplace skills.
3. Having more productive workers leads to a business that is more effective and productive.

Claim #3: U.S. companies who hire U.S. examinees of high school or work force age who demonstrate Applied Math scores that reach at least a given level are more likely to reduce turnover (retain those examinees for at least 6 months) than if the companies had hired examinees whose scores do not reach that level.

Claim #3 Assumptions:

1. Claim #1 Assumptions 1–7
2. Employees with higher foundational skill levels are less likely to be terminated in the first 6 months of employment than employees with lower foundational skill levels.
3. Employees with higher foundational skill levels are less likely to quit in the first 6 months of employment than employees with lower foundational skill levels.
4. Businesses that utilize scores from the Applied Math assessment as part of their hiring process will tend to experience less turnover than businesses who do not use the Applied Math assessment as part of their hiring process.

The three Applied Math claims addressed questions around examinee job success, improving worker productivity, and reducing employee turnover rates. Based on the claims, the critical stakeholders and intended test users are employers and hiring managers, state or regional workforce development officials, schools that prepare students to take jobs in the state or region, and examinees who are, or will be, seeking employment and career advancement.

The *Standards* (AERA et al., 2014) identify five sources of validity evidence: (a) evidence based on test content, (b) evidence based on internal structure, (c) evidence based on relationships to other variables, (d) evidence based on response processes, and (e) evidence based on consequences of testing. The remainder of the chapter applies a validity use argument (Kane, 2013) to provide evidence first related to the assumptions associated with the claims and then for the claims themselves.

11.4 Applied Math—A Measure of Foundational Workforce Skills

All three primary claims are dependent on the validity of initial assumptions:

1. applied mathematics is a foundational workplace skill and is required for success in a large number of jobs;
2. ACT has developed a valid and appropriate construct definition of applied mathematics;
3. ACT's Applied Math assessment provides reliable and interpretable scores that reflect the construct. ACT's Applied Math assessment elicits observable evidence of the construct;
4. ACT has defined appropriate Applied Math PLDs and has established standards aligned to the PLDs; and
5. cut scores used to delineate each performance level have sufficient classification accuracy.

For the primary claims to be plausible, evidence supporting each of the five assumptions needs to be evaluated.

The next subsections present data and analysis related to the five assumptions. The analysis draws on the professional literature from the fields of educational measurement and industrial-organization psychology, as well as data that ACT collected from over 20 years of job profiling, from three separate field test studies, and from a series of standard setting meetings.

11.4.1 Foundational Workplace Skills

Foundational workplace skills are the skills that are essential for conveying and receiving information that is vital to work-related training and success (ACT, 2014). Job skills are different from foundational skills. Job skills are the skills required to perform a specific job. For example, licensed electricians require skills in working with electrical circuits and wiring to perform their jobs. Foundational skills are more general than job skills; they are the skills that enable a person to learn specialized job skills.

Foundational skills are often referred to as basic or academic skills that are taught through formal schooling, but they may be learned from other sources. The foundational skills are frequently defined in terms of academic subjects including reading, writing, mathematics, and science. These skills enable individuals to acquire job-specific skills, communicate information with fellow workers, and engage in lifelong learning.

Foundational skills are fundamental in that they serve as the basis for supporting additional learning. They are “portable” in that, rather than being job specific, they can be applied at some level across a wide variety of jobs and occupations (Symonds, 2011). In the 21st century, multiple studies and surveys have identified the need for employees to be engaged in lifelong or fluid learning (Infosys, 2016; NNIA, 2014; Organization of Economic Cooperation and Development [OECD], 2016; Society for Human Resource Management [SHRM], 2010). As the economy has become more technical and global, the pace of change has increased greatly. The concept of a job for life has become outdated. Successful workers will have a flexible mind set and the basic skills needed to continually learn and re-train themselves to remain relevant and successful in a dynamic and shifting economy (Infosys, 2016).

11.4.2 Applied Math—A Foundational Workplace Skill

In the assumptions supporting the assessment claims, ACT identified Applied Math as one facet of foundational workplace skills. ACT based its argument that applied mathematics is a foundational workplace skill on three sources of evidence: (1) job analysis data that has consistently indicated that applied mathematics skills are needed to achieve job success, (2) professional literature and job competency models that identify applied mathematics as a critical 21st century skill, and (3) descriptions of the Programme for the International Assessment of Adult Competencies (PIAAC) assessments in which the ability to understand and solve mathematical problems is a critical element of adult numeracy.

Since initiating its job profiling services in 1993, ACT has conducted over 21,000 job profiles representing a wide cross-section of U.S. jobs. Job profiles have been conducted on jobs in manufacturing, health care, construction, financial services, public administration, leisure and hospitality, agriculture, and other sectors. ACT has profiled 193 (just under 50%) of the 387 Bright Outlook Occupations identified by O*NET using Bureau of Labor Statistics projection data (U.S. Bureau of Labor Statistics, 2013). Analysis of the job profile database indicates that skills people associated with using applied mathematics to solve problems were included in 12,516 profiles or slightly less than 59% of all ACT profiles. When ACT assigned each completed profile to an O*NET job code, applied mathematics appeared as a required skill for 653 distinct O*NET job codes or 60% of all O*NET job codes.

In recent years, several business and industry associations have built 21st century workplace competency models that provide support for the inclusion of applied mathematics as a foundational workplace skill (Association for Career and Technical Education [ACTE], 2010; Infosys, 2016; NNBIA, 2014).

The competency model developed by the Business Roundtable (NNBIA, 2014) defined common employability skills, classifying skills into four categories: personal skills, people skills, applied knowledge, and workplace skills. The third skill identified under applied knowledge was mathematics. They maintained that employees needed proficiency in the following math-related skills:

- Add, subtract, multiply, and divide whole numbers, fractions, decimals, and percentages
- Convert decimals to fractions; convert fractions to decimals
- Calculate averages, ratios, proportions, and rates
- Take measurement units of time, temperature, distance, length, width, height, and weight; convert one measure to another
- Translate practical problems into useful mathematical expressions (p. 3)

ACTE (2010) argues that students must be able to apply academic knowledge to authentic situations that they might find in their careers. The report emphasizes that students need strong knowledge and skill in the core academic studies, particularly in English language arts and math. It maintains that because most students will be engaged in more than one career over their working lifetime, that the core academic skills are critical in helping them to develop new skills and adjust to new situations.

PIAAC evaluates the status of adult workplace competency through three different assessments: Literacy, Numeracy, and Problem Solving in Technology-Rich Environments (OECD, 2016). In the

Numeracy assessment, they present examinees with items that require the examinee to first understand the problem, then organize the problem, then solve the problem. They expect their examinees to be able to apply mathematical skills to problems containing quantitative data to solve problems.

Based on the understandings gained from studying ACT's job profiling data, the workforce competency models, and the construct definitions developed for the PIAAC assessments, applied mathematics is a necessary foundational workplace skill that contributes to employee success and lifelong learning.

Of course, solving applied mathematics problems is not universally required across all jobs. As stated above, ACT has found that solving applied mathematics problems is used in 653 distinct O*NET job codes or approximately 60% of all O*NET job codes. When the Applied Math assessment is used as a part of the hiring process, ACT recommends that the employer gathers evidence to support the relevancy of the assessment and level score requirements. ACT provides its job profiling service as a valid method for gathering the required evidence to demonstrate both assessment relevancy and score level requirements.

11.4.3 Applied Math—Construct Defined

A detailed description of the Applied Math construct is provided in Chapter 2. Summarizing Chapter 2, Applied Math is designed to assess the extent to which individuals can apply mathematical reasoning and skills to work-related situations to solve problems. The ability to think problems through to find and evaluate solutions is critical for workplace success (Australian Association of Mathematics Teachers Inc., 2014; Smith, 1999).

To be more specific, the Design Team defined the construct as six general applied mathematical skills that workers use to solve quantitative work-related problems. They are:

- Basic Operations Including Decimals
- Fractions
- Percentages/Ratios/Proportions
- Unit Conversions
- Geometric Measurement
- Applied Math Reasoning

11.4.4 Applied Math—Field Test Sampling

Applied Math was theoretically defined and supported through analyses of professional literature on the use of mathematics in the workplace, data collected by ACT through the job profiling services, and through input provided by a panel of Subject Matter Experts (SMEs).

ACT engaged in a series of three field test studies to evaluate the psychometric properties of initial Applied Math forms. For each of the field test studies, ACT attempted to recruit samples that were representative of the WorkKeys test population. In recruiting for the field test studies, ACT was cognizant

of recruiting a sufficient number of adult test takers due to the workforce orientation of the assessment. Table 11.1 provides a comparison of the percentages of test takers from the WorkKeys test population (2013–2014) to the three field test samples.

Table 11.1: Comparison of WorkKeys Test Population and Field Test Samples by Student/Adult, Gender, and Ethnicity

Group	WorkKeys Test Population	Field Test #1 Sample	Field Test #2 Sample	Field Test #3 Sample
Age Groups				
High School Age	40.6%*	67.1%	60.5%	47.1%
Adults	59.4%	32.9%	39.5%	52.9%
Gender Groups				
Women	46.0%	49.0%	52.6%	56.0%
Men	54.0%	48.0%	47.4%	44.0%
Ethnic Groups				
White Examinees	58.0%	71.8%	60.7%	63.4%
African-American Examinees	21.2%	16.4%	17.4%	16.4%
Hispanic Examinees	8.2%	3.7%	6.7%	7.9%

Note. The WorkKeys test population percentages are based on examinees self-identifying with a specific group during the testing period from July 1, 2013 and June 30, 2014.

*Based on test-takers who reported their age as 20 and below.

The field testing was designed to (a) determine an acceptable time allotment for testing, (b) develop a standardized score scale that was interpretable and could be applied for developing subsequent Applied Math forms, (c) evaluate model-data fit for the three-parameter logistic (3-PL) IRT (Hambleton & Swaminathan, 1985), and (d) evaluate the mode effect on test scores (paper vs. online administration).

11.4.5 Measuring Applied Math

Testing Time. ACT conducted two separate studies to assess the appropriate amount of time examinees should be allowed to complete the Applied Math assessment. In the first study, examinees were assigned to take either the online or the paper version of the assessment. They were also assigned to have either 55 or 60 minutes to test. Based on the study, ACT wanted to determine (a) whether the test mode (online vs. paper) required the same or different time allotments, and (b) the appropriate amount of time to provide examinees in testing.

ACT defined the assessment as a power test, which is a test that provides examinees sufficient time to answer all items or tasks, and the speed by which an examinee solves the items or tasks should not affect test scores. In a speeded test, examinees' ability to work quickly through the items or tasks is considered a relevant facet of the construct. For Applied Math, whether examinees work through the

items quickly or slowly, their speed should not affect their scores. Any effect that speed might have on test scores is interpreted as construct irrelevant variance.

ACT evaluated test speededness by analyzing the percentage of examinees who were able to answer the last item on the assessment and the omit rate of items across the complete assessment. Over 500 examinees participated in the first field study.

From the first field study, ACT found that examinees took approximately the same amount of time to complete the assessment regardless of mode (online vs paper). They also found that the completion rates for the assessment were only slightly different for the 55-minute time limit compared to the 60-minute time limit. For online testing, where ACT was able to track the amount of time examinees spent on each item, examinees in the 60-minute condition used an average of a little more than one additional minute for testing than examinees in the 55-minute condition. Ninety-five percent of the examinees in both conditions completed the assessment in 51 minutes or less. The omit rate for the final test item in both conditions was less than 2 percent. For examinees in the 55-minute condition, 93% either strongly agreed or agreed with the statement that they had sufficient time to test. For examinees in the 60-minute condition, 97% either strongly agreed or agreed with the statement that they had sufficient time to test.

Based on these results, ACT concluded that for both online and paper administration, the allotted testing time should be 55 minutes. In the second field study, ACT continued to evaluate testing time. The findings from the second study confirmed the conclusion of the first study; 55 minutes was a sufficient amount of time to allow examinees. With a 55-minute time allowance, speededness should not affect examinees' Applied Math scores.

Scale Scores. Results from the field study related to the establishment of the scoring scale are presented in Chapter 8.

Score Reliability and Generalizability. Score reliability or generalizability is essential for interpreting and using scores derived from any measure (Kane, 2013). For test scores to be interpretable, they must be consistent across various testing occasions and across different forms of an assessment. Chapter 10 summarizes analyses of field test data to provide estimates of score reliability and measurement error. Based on the analysis, Applied Math scores are reliable and generalizable (i.e., measurement error is minimal) for use in estimating examinee skill levels.

Mode Effects. ACT develops Applied Math items to be used for both paper and online delivery. ACT conducted a field study to determine if scores achieved when taking the Applied Math assessment online were comparable to scores achieved when taking the assessment on paper. ACT evaluated the mode effects at the item level, by comparing the similarity of item p-values, point biserial correlations, IRT item parameter estimates (a , b , and c parameters), and omit rates. The evaluation of the different item statistics indicated that examinees responded to the items similarly across modes. Differential Item Functioning (DIF) analyses were conducted to determine if examinees of similar ability had similar probabilities of answering an item correctly in different modes. ACT also evaluated the mode effect by analyzing raw scores across the two modes. Examinee raw scores across the two modes were nearly identical, as was the raw score variance. ACT further analyzed the mode effect by analyzing the factor structure of the assessment delivered in two different formats. Overall, ACT concluded that the mode effect was negligible. (For greater detail regarding the mode analyses, see Chapter 9.)

11.4.6 Applied Math—Evidence Based on Internal Structure

ACT analyzes WorkKeys assessment item data using a unidimensional Item Response Theory model (Hambleton & Swaminathan, 1985; Lord, 1980). WorkKeys has traditionally applied unidimensional IRT models to make inferences about examinee proficiency based on observed item scores. This requires the assumption that observed score variance be attributable to a single underlying factor.

Applied Math Dimensionality. ACT applied exploratory factor analysis (EFA) to assess dimensionality for the Applied Math assessment. EFA uses an inter-item correlation matrix to identify factors underlying observed item variance. In the analysis, ACT applied four criteria to assess dimensionality. A scree plot of eigenvalues is one of the most commonly used tools for determining test dimensionality. When there is only one eigenvalue above the “elbow” in the scree plot, this indicates a unidimensional test. Hatcher (1994) suggested that a factor should be retained if it accounted for at least 10% of total variance. Reckase (1979) suggested that, if the first factor explains 20% of the variance of a set of items, the item set should be considered unidimensional. Hattie (1985) maintained that the first factor is relatively strong if the factor difference ratio index (FDRI) (Johnson, Yamashiro, & Yu, 2003) is greater than 3. FDRI is the ratio of the difference between the eigenvalue of the first factor and the second factor to the difference between the eigenvalue of the second and the third factor.

The EFA was conducted using data from the second field study. Over 2,100 examinees participated in the second field study. The participants were representative of the WorkKeys testing population in that approximately 60% of the examinees were high schoolers and 40% were adults; approximately 53% of test takers were women and 47% were men.

Figure 11.1 is the scree plot derived from the correlation matrix of item scores on the Applied Math assessment. Table 11.2 summarizes the eigenvalues and FDRI for both test forms. Figure 11.1 reveals that the “elbow” appears immediately after the first eigenvalue. Table 11.1 indicates that the percentage of variances accounted for by the first factor is nearly 40% and, for the second factor, it is 8.7%. Additionally, Table 11.2 indicates that the FDRI is 6.75 or significantly greater than 3. These findings consistently indicate that a single factor underlies item scores on the Applied Math assessment.

Eigenvalue: AM

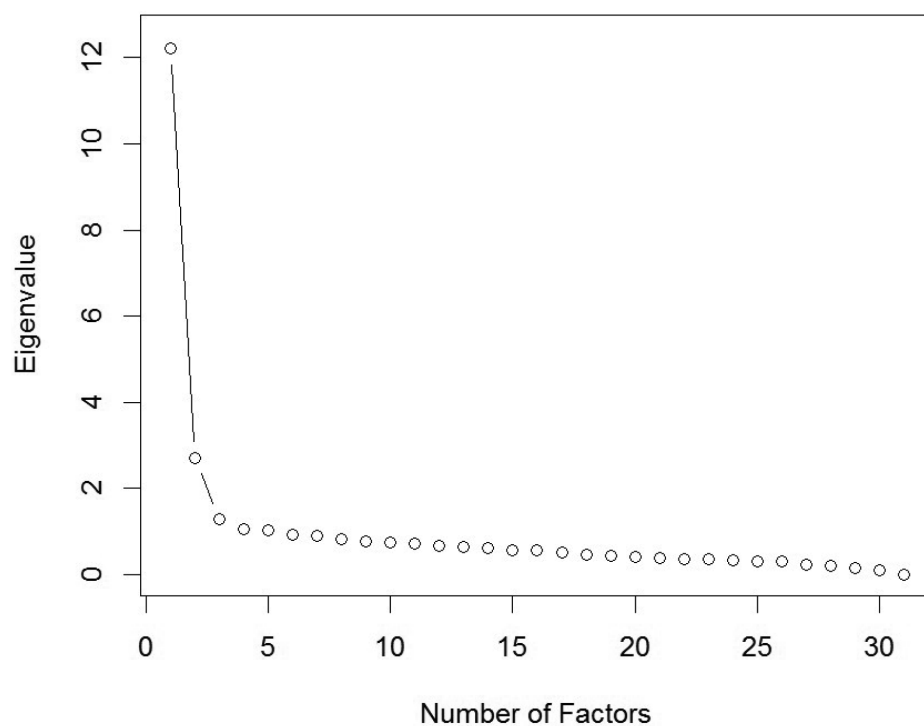


Figure 11.1: Applied Math—Eigenvalue Scree Plot

Table 11.2: Summary of Eigenvalues and Factor Difference Ratio Index (FDRI)

Factor	Eigenvalue	Difference between Eigenvalues	FDRI
1	12.21 (39.4%)		
2	2.70 (8.7%)	9.51	
3	1.30 (4.2%)	1.41	6.75

Note: the percentage in the parenthesis is the percentage of total variance accounted for by that factor.

IRT Modeling—Local Item Independence. The 3PL IRT model assumes that items are locally independent, which means that examinees’ scores on different items in an assessment are statistically independent of each other after controlling for the examinee’s ability. For the assumption to be met, examinees’ responses to one item cannot be affected or prompted by other items. When local independence is achieved, the probability of any pattern of item responses for an individual is the product of the probability of the correct response for each individual item based solely on examinee ability (Hambleton & Swaminathan, 1985).

Items on the Applied Math assessment are discrete items, meaning that each item is a single element on the assessment designed to assess a single skill in isolation. Discrete items do not share common stimulus materials (e.g., graphics or reading passages) with other items on the assessment. After an Applied Math assessment form is assembled, content and research specialists review the form to ensure that no item on the form clues or provides information that may prompt or assist an examinee in answering a different item on the form. ACT form development quality assurance specifies that developers review each other's work to ensure that no item clues another item on the form. Subsequently, items on the Applied Math assessment are locally independent because of its design properties and its quality assurance specifications.

11.4.7 Standard Setting

The goal of the standard setting process is to translate the Applied Math PLDs into a set of cut scores. Essentially, the process is designed to identify a point on the score scale where examinees who score at or above the point have demonstrated that they can perform certain skills, and examinees who score below the point have not demonstrated that they can perform those skills. To provide data and input for setting the cut scores, ACT recruited an external panel of SMEs consisting of educators and business people, some of whom have used WorkKeys products.

ACT implemented the Mapmark standard setting procedure (Schulz & Mitzel, 2005) with Whole Booklet Feedback to establish the standards or cut points for each of the five Applied Math score levels. The Mapmark procedure, which was first implemented by ACT for the Grade 12 mathematics National Assessment of Educational Progress (NAEP) achievement level setting project, builds on the widely used Bookmark method (Lewis, Mitzel, & Green, 1996). The Bookmark method was introduced in 1996 and has gained wide acceptance in state educational assessment programs and in professional certification and licensing programs. Mapmark supplements the Bookmark method by including spatially-representative item maps (Masters, Adams, & Lokan, 1994).

To establish the cut points for each of the five score levels, ACT led the SMEs through three rounds of ratings and reviews. In Round 1, the SMEs applied the Mapmark procedure to establish the initial cut points. The initial cut points were refined in Round 2 by providing the SMEs with whole booklet feedback in the form of examinee test answer sheets. In Round 3, ACT provided the SMEs the estimated level score distribution based on data from the second field study to assist them in finalizing the cut points. Chapter 8—Scores and Score Scales—provides a complete description of the Standard Setting process.

11.4.8 Applied Math Measurement—Summary

Based on the data analysis presented in Section 11.4, ACT has provided support for the interpretation and use of Applied Math scores. This support was accomplished by starting with the information and data that ACT had gathered over 20 years of conducting job analyses and profiling various jobs requiring applied mathematics. The information and data was then supplemented by a thorough review of the professional literature around the use of mathematics both in education and the workforce. The external SMEs further assisted ACT in refining the construct definition of applied mathematics and the development of exemplary items.

With the development of the initial forms of the assessment, ACT then conducted field tests to learn more about applied mathematics and the assessment. The preponderance of the research and data analyses indicated that the Applied Math assessment provided a reliable measure of a unidimensional construct built around the concept of examinees working through problems requiring different levels of applied mathematics. The analysis gathered by having external SMEs evaluate the construct and exemplary items indicated that ACT had appropriately defined applied mathematics. The analysis of field test responses assisted ACT in identifying the appropriate amount of time for testing. Field testing also allowed ACT to conclude that the assessment was a measure of a unidimensional construct and that construct irrelevant variance was minimal. Analysis of field test data further demonstrated that scores achieved taking the assessment by paper administration were comparable to scores achieved by online administration. Lastly, the analysis found that scale scores and level scores earned on the assessment were reliable.

11.5 Applied Math—Primary Claims and Relevant Findings

The purpose of the WorkKeys system is to help build a high-performance workforce by connecting job skills, training, and testing in a manner that benefits both employers and employees. WorkKeys also assists educators in identifying skill gaps between student skills and employment needs, so that they may better address the gaps and thereby improve students' employment prospects.

The three primary claims articulate how scores from the Applied Math assessment may provide actionable information to examinees, employers, educators, and workforce development officials to make these connections. The three claims differ in who is the focus of the claim and how score information may be used to accomplish the intended result.

The focus of Claim #1 is the examinee or person seeking employment. Scores on the Applied Math assessment are related to workplace success. In other words, an examinee who scores at a prescribed level (as defined through data from a Job Profile) will have a greater probability of achieving success in a corresponding job (based on levels established through a Job Profile) than an examinee who did not score at the prescribed level. Additionally, examinees who score at higher levels on the Applied Math assessment will have a higher probability of obtaining jobs with greater responsibilities and wages. Claim #1 provides the structure for evaluating how high scores on Applied Math may help an individual in the labor market.

The focus of the second and third claims is the employer or business. Scores on the Applied Math assessment are related to workplace success in ways that will result in improved business productivity and efficiency. Claim #2 states that, if a business determined the Applied Math assessment scores required for specific jobs through a job analysis or Job Profile, and if the business then hired people who achieved those scores, the productivity gains provided by the new employees would be greater than if a business had not used the assessment scores to help select employees. Claim #3 states that, if a business follows the hiring process outlined for Claim #2, the business would experience less employee turnover (i.e., more new hires retained) than if the business had not used the assessment to help select employees.

Claims #1 and #2 can be supported by the development of the content-related and construct evidence provided in Section 11.4. Additionally, they can be supported through the analysis of outcome data. Claim #3 requires the analysis of employee turnover rates to be plausible. ACT has embarked on a series of outcome studies collecting data from employers and educators to assess the extent that the claims are plausible. With Applied Math being an updated assessment, ACT is in the process of teaming up with businesses and states to collect the necessary data. Following the collection and analysis of the data, ACT will publish the findings and update the technical manual. In the meantime, this section of the technical manual presents information and data derived from the initial Applied Mathematics assessment, the WorkKeys NCRC, and from meta-analyses relating cognitive assessments to workplace performance.

11.5.1 Applied Mathematics—Evidence Based on Test Content

Evidence based on content comprises one source of evidence to establish the validity of test score interpretations and uses (AERA et al., 2014). Content evidence often comprises the first line of evidence to support employment selection practices. The *Uniform Guidelines on Employee Selection Procedures* (Equal Employment Opportunity Commission [EEOC], Civil Service Commission, Department of Labor, & Department of Justice, 2000), the *Standards* (AERA et al., 2014), and the *Principles for the Validation and Use of Personnel Selection Procedures* (Society for Industrial Organizational Psychology [SIOP], 2003) all describe the need to demonstrate that knowledge and skills in employment measures should be demonstrably linked to work behaviors and job tasks. Both the *Standards* (2014) and the *Principles* (2003) suggest that expert judgment can be used to determine the importance and criticality of job tasks and to relate such tasks to the content domain of a measure. This process is commonly conducted through a job analysis that identifies the tasks required for performance on a job and subsequently for the development of the content blueprint and item development to ensure content validity (Cascio, 1982; Dunnette & Hough, 1990). The Applied Math assessment was designed to assess foundational skills and skill levels associated with many jobs. As such, the content-related validity evidence for the assessment was originally established by the SMEs across numerous jobs that aligned the Applied Math skills and PLDs to specific tasks and job behaviors for a particular job.

ACT applies a job profiling procedure that focuses on the skills and behaviors present across the ACT WorkKeys assessments. It is a multi-step process that includes the creation of one or more groups of SMEs who are typically job incumbents or supervisors. An ACT-trained and authorized job profiler conducts the profiling procedure. Each profile that is conducted represents a content validation study at the organizational level.

The job profiling process involves several steps to establish a link between the PLDs and the requirements of a particular job. Ideally, the SMEs participating in the job analysis comprise a representative sample across a variety of demographic variables (e.g., race, ethnicity, gender, geographic region).

The process begins with a task analysis where the group of SMEs generates a task list that accurately represents the job at an organization and to rate each task in terms of its importance. Figure 11.2 details the steps in the job profiling procedure where tasks and skills are identified leading to the completion of the job profile.

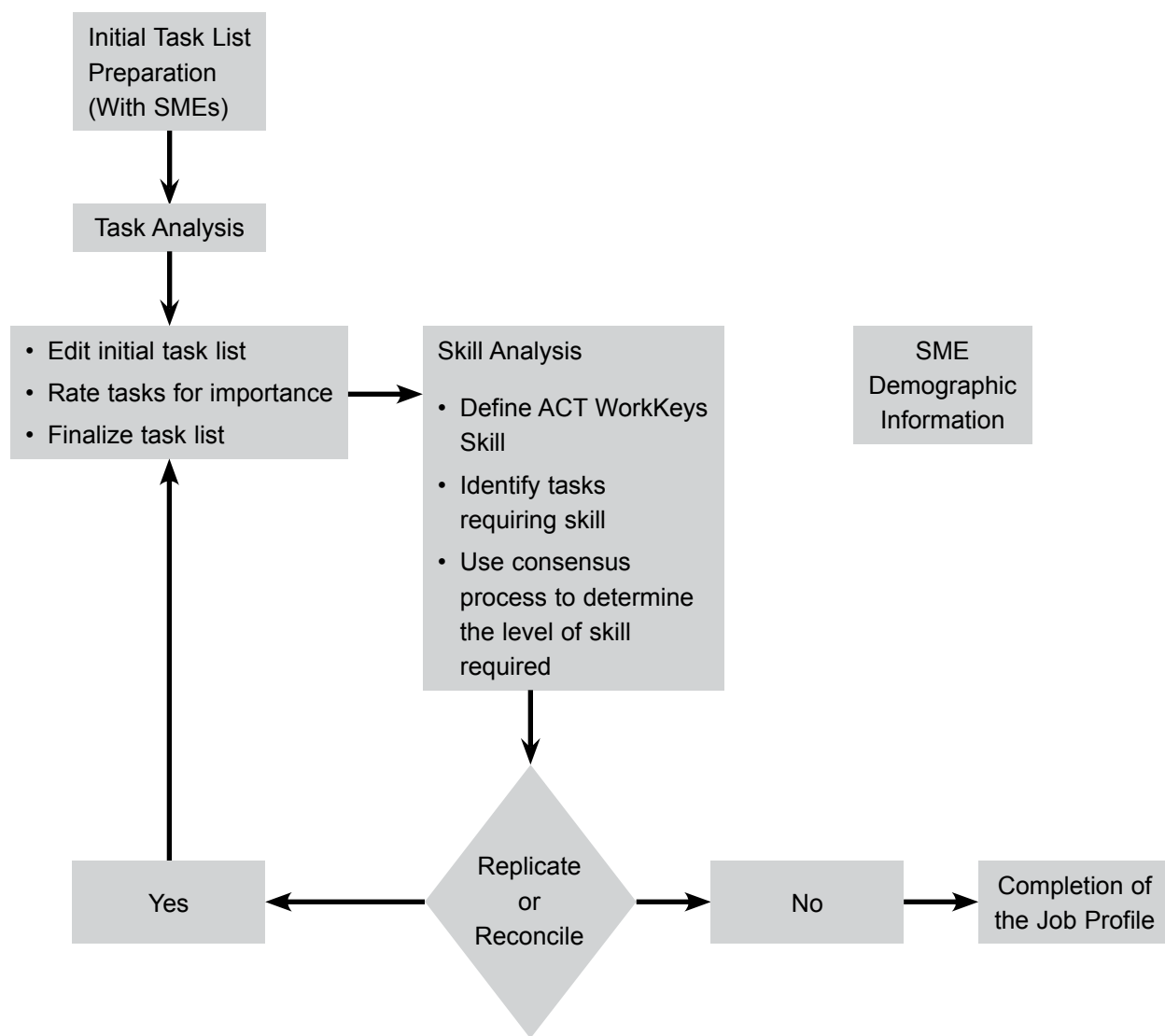


Figure 11.2: Job Profile Process Designed to Align Job Tasks to Skill Levels

Equally important is the skill analysis where the SMEs review each skill measured by the Applied Math assessment. Once the SMEs understand the definition of the skill and have determined its relevancy to the job, they independently identify the important tasks on the Final Task List that require the skill. They also identify the ways in which a task uses an identified skill. After discussing the relationship of

the skills to the tasks, only those tasks identified as important by a majority of the SMEs are included in subsequent discussions, and only those tasks are used to determine the level of skill required for the job through a consensus process.

As part of the skill analysis segment, the SMEs use successive approximation to determine the skill level required for the final set of tasks. Each skill level denotes a level of difficulty, with the lowest level representing the simplest of tasks related to the skill construct and the highest level representing the most complex. The SMEs typically begin with the lowest skill level. They then determine whether the job requires skills at, above, or below the level described. If the SMEs determine that the skills required for the job are higher than skills described in a level, they proceed to the next higher level; if they determine the required skills are lower, they review the next lower level. If they determine that the skills are about the same as the level they are reviewing, they are still shown the next higher level before confirming agreement between skills and a designated level to confirm their judgment.

No decision is reached until the SMEs have considered a range of skill levels: those skills they have identified at the required level, at least one level above it, and at least one level below it (unless they have chosen the highest or lowest level available).

The process described in this section is documented by the job profiler in a content validity report that is provided to the client. Currently, ACT WorkKeys clients have completed over 21,000 job profiles.

11.5.2 Applied Mathematics—Evidence Based on Relationships to Work-related Variables

LeFebvre (2016) summarized 15 workplace outcomes studies for the WorkKeys suite of assessments, including the Applied Mathematics assessment. These studies examined the relationship between scores on the Applied Mathematics assessment and outcome measures with sample sizes ranging from 13 to 2,162 participants. The studies included health care service providers, manufacturing workers, motor coach drivers, and students in career technical education. She concluded that individuals who achieve higher Applied Mathematics scores tended to receive higher job performance ratings and achieved higher grades in postsecondary and career-technical studies. Table 11.3 presents a summary of the validity coefficients, which are the correlations between scores on the Applied Mathematics and different outcomes. Table 11.3 also presents the relationship of composite scores from Applied Mathematics, Reading for Information, and Locating Information with different outcome measures (LeFebvre, 2016).

Table 11.3: Correlations between Scores on the WorkKeys Applied Mathematics Assessment and Different Outcomes

WorkKeys Assessment	No. of Studies	Sample Size or Range	Validity Coefficient*	Outcome Variable
Applied Mathematics	1	2,162	.21	Career Tech Course Grades
Applied Mathematics	1	1,246	.28	Postsecondary GPA
Applied Mathematics	13	13–165	.12	Overall Job Performance—Supervisor Ratings
Composite of AM, RFI, and LI	3	68–951	.29	Overall Job Performance—Supervisor Ratings
Composite of AM, RFI, and LI	1	951	.25	Career Tech Course Grades

*When multiple studies are included, the table presents the median validity coefficient for the set of studies.

Hendrick and Raspiller (2011) analyzed data from 12 different companies that used the WorkKeys NCRC to determine its effect on worker retention. They found that businesses using the WorkKeys NCRC as part of the hiring process saw their retention rates increase from 84% to 93%. Further, they found that the higher the WorkKeys scores, the more positive the effect on retention. In follow-up interviews with hiring managers, Hendrick and Raspiller (2011) learned that using the WorkKeys NCRC as part of the hiring process also resulted in new employers requiring less training time and less of a need to be closely supervised.

Greene (2008) analyzed the use of the WorkKeys cognitive assessments in business and industry in North Carolina. She surveyed employers of small and large companies focusing primarily on the use of the WorkKeys NCRC. She found that employers viewed the WorkKeys NCRC as a useful tool to assist in hiring. In using the WorkKeys NCRC to assist in hiring decisions, 60% of hiring managers agreed that training time was reduced, 52% agreed that worker turnover rates were reduced, 40% agreed that company teamwork increased, and 36% agreed that re-work was reduced. In follow-up interviews, the hiring managers stated that the WorkKeys NCRC provided a pre-employment screening device that allowed them to select workers who learned job tasks more quickly, reached production targets more quickly, and produced better overall quality work.

These studies specifically analyzed scores on the Applied Mathematics assessment or levels achieved on the WorkKeys NCRC to outcome measures, including job performance ratings and grades in career and technical education programs. Other researchers have analyzed measures of cognitive ability and their usefulness in the employment sector. The most reputable of these studies have combined data from many studies and incorporated meta-analysis techniques to draw conclusions.

Prior to the use of meta-analysis and today's understanding of measurement problems associated with outcome variables, researchers believed that validity coefficients varied a great deal from one job to the next. For the first 70 years of the 20th century, researchers evaluated employment selection methods by correlating scores on selection tests to measures of job performance. They found that using the same tests for nearly identical jobs often resulted in quite different validity coefficients. They concluded that the differences in validity coefficients stemmed from subtle differences in job requirements resulting in situational-specific validity (Ghiselli, 1966).

Many of the differences reported across different validity studies have been shown to be the result of statistical and measurement artifacts (Schmidt & Hunter, 1977; Schmidt, Hunter, Pearlman, & Shane, 1979). Subsequently, meta-analytic methods were developed to account for sampling error, selection bias, low reliability of criterion measures, and other artifacts. When statistical and measurement artifacts were accounted for, the findings indicated that the variability of validity coefficients was reduced to near zero (Hunter, 1980). The finding that validity coefficients could be generalized across selection methods and jobs made it possible to compare and analyze different personnel selection methods.

In a comprehensive review, Schmidt and Hunter (1998) examined 85 years of research on personnel selection and concluded that the best predictor of job performance and the ability to benefit from job-related training was general cognitive ability. As an update to the 1998 paper, Schmidt, Oh, and Schaffer (2016) evaluated 31 different methods of personnel selection from cognitive ability testing to job interview rating systems to the analysis of handwriting. They concluded that general cognitive ability was the “gold standard” of selection methods, and they then assessed how much additional predictive power was gained by combining other methods with cognitive ability testing.

Schmidt and Sharf (2010) evaluated the three assessments constituting the WorkKeys NCRC. They concluded that “measures of general cognitive ability such as WorkKeys are the most job related (i.e., most valid) predictors of job performance in both the military and civilian workforces” (p. 12). They defined the Applied Mathematics assessment as a measure of quantitative reasoning skills that was highly relevant to job performance and learning.

Combining Schmidt and Sharf’s (2010) results with LeFebvre’s summary reveals a median correlation of 0.29, which appears similar to correlations of the SAT and ACT to first-year college grades. Taking into account selection effects, range restriction, and low reliability of outcome measures, similar to the validity coefficients of the SAT and ACT in predicting student grades, the correlation of 0.29 is a conservative estimate. The disattenuated correlation is likely much greater (Sackett, Borneman, & Connelly, 2008).¹

11.5.3 Applied Mathematics and Return on Investment

Hunter, Schmidt, and Judiesch (1990) published a ground breaking analysis indicating that the return on investment (ROI) of hiring the best people was potentially large, and for jobs that required complex information processing, it was very large. They utilized meta-analytic methods to evaluate data from several hundred studies involving thousands of employees doing different jobs. They concluded that, for jobs that required low levels of information processing, a person who was in the top 1% of the applicant pool would be 1.52 times more productive than a person who was at the median of the applicant pool. For jobs that required moderate levels of information processing, a person who was in the top 1% of the applicant pool would be 1.85 times more productive than a person who was at the median of the applicant pool. Lastly, for jobs that require high levels of information processing, a person who was in the top 1% of the applicant pool would be 2.27 times more productive than a person who was at the median of the applicant pool. They concluded that differences in individual productivity were large and businesses that hire the best people tend to experience a competitive advantage. This difference would be particularly pronounced for a business where large numbers of employees are engaged in high levels of information processing.

Mayo (2012) analyzed hiring data for New Options New Mexico evaluating the ROI of using the WorkKeys NCRC as part of the hiring process. Preexisting data for each employer was collected and outcomes compared pre- and post-WorkKeys NCRC implementation. She found that by implementing the WorkKeys NCRC, businesses experienced a 25–75% reduction in turnover, a 50–70% reduction in time to hire, a 70% reduction in cost-to-hire, and a 50% reduction in training time. Overall, she concluded that using the WorkKeys NCRC as part of the hiring process resulted in employers making a minimal investment in order to receive a very large return.

11.5.4 Applied Mathematics and Educational Outcomes

LeFebvre (2016) reviewed studies that related Applied Mathematics scores to postsecondary educational outcomes (see Table 11.3). In career and technical education programs, individuals who achieved higher Applied Math scores tended to have higher completion rates and earn higher grades. Also, individuals who achieve higher Applied Math scores tended to have higher grade point averages in their postsecondary studies.

Schultz and Stern (2015) studied changes in examinee perceptions of career readiness following the administration of the NCRC assessments to high school students in Alaska. They surveyed students in their junior year of high school and asked them if taking the assessments and reviewing their scores were helpful. Students reported that the assessments assisted them in evaluating their career readiness, were useful in career planning, and caused them to think more seriously about different career options. Most interestingly, scores from the assessments provided students with information that appeared to contradict the feedback they had received from their high school course grades. Whereas nearly 75% of the students reported receiving class grades of A's and B's, and they regarded their skills as strong, based on their WorkKeys scores, slightly more than 50% of the students did not meet the college or career readiness standards.

11.5.5 Applied Math at the State and Regional Level

LeFebvre (2016) analyzed statewide workforce studies where the WorkKeys NCRC was used to assist individuals in finding employment. Using data from workforce development agencies in Indiana, Iowa, Ohio, and southwest Missouri, she found that individuals who achieved higher levels experienced faster time to hire, earned higher wages, and stayed in their jobs longer.

11.6 Applied Math—Evaluation of Claims

The cited studies analyzed data from the Applied Mathematics assessment, the WorkKeys NCRC, and general measures of cognitive ability. As mentioned earlier, the Applied Math assessment constituted one of three assessments of the WorkKeys NCRC. Applied Math was designed building on the information that ACT had collected over the past 25 years from the original Applied Mathematics assessment. Its content was updated to better reflect current uses of applied mathematics in the workforce.

Psychometrically, the updated Applied Math assessment met or exceeded the psychometric standards that were used to develop forms of the Applied Mathematics assessment. For these reasons, data collected from the Applied Mathematics assessment can tentatively be used to evaluate the claims, even though ACT is currently collecting outcome data related to Applied Math performance.

From the individual examinee perspective, based on the findings, when score information from the Applied Mathematics assessment and the WorkKeys NCRC were used as part of employment selection or for educational evaluation, it appeared that individuals who achieved sufficient scores on Applied Mathematics tended to experience the following:

- Reduction in time to hire (LeFebvre, 2016; Mayo, 2012)
- Higher wages (LeFebvre, 2016; Mayo, 2012)
- Longer job tenures (Mayo, 2012)
- Better job performance evaluations (LeFebvre, 2016)
- Better post-secondary grades and higher career-technical program completion rates (LeFebvre, 2016)
- Information that provides insight useful in evaluating career readiness and career planning (Schultz & Stern, 2015)

The findings from the studies provided evidence supporting Claim #1 that examinees who score at given levels of the Applied Math assessment are more likely to successfully perform in more and higher levels of U.S. jobs than examinees whose scores do not reach that level.

From the employer's perspective, based on the findings, when score information from the Applied Mathematics assessment and the WorkKeys NCRC were used as part of the employment selection process, it appeared that businesses tend to have the following outcomes:

- Higher levels of productivity (LeFebvre, 2016; Greene, 2008; Hunter, Schmidt, & Judiesch, 1990)
- Lower rates of re-work (Greene, 2008)
- Lower turnover rates/higher retention rates (Hendrick & Raspiller, 2011; Mayo, 2012; Greene, 2008)
- Less training time (Hendrick & Raspiller, 2011; Mayo, 2012; Greene, 2008)

The findings provided evidence supporting Claims #2 and #3 that businesses that use the Applied Math assessment as part of the hiring process will experience increases in business productivity and reduced worker turnover rates.

From the state and regional perspective, based on the findings of using test scores from the Applied Math assessment and the WorkKeys NCRC to promote local workforce development, it appeared that states and regions that have a large number of workers who have earned high scores and credentials have the following characteristics:

- workers with higher levels of the WorkKeys NCRC tend to be hired more quickly (LeFebvre, 2016)
- workers with higher levels of the WorkKeys NCRC tend to earn higher wages (LeFebvre, 2016)
- workers with higher levels of the WorkKeys NCRC tend to stay in jobs for longer periods of time (LeFebvre, 2016; Hendrick & Raspiller, 2011; Mayo, 2012; Greene, 2008)

As ACT builds up the Work Ready Communities, it is collecting data on economic and business productivity. It is also collecting data on job growth and wages.

11.7 Applied Math—Evidence Based on the Consequences of Testing

Kane (2013) defined consequential evidence that should be evaluated and weighed in making decisions about test use. Two critical components of consequential evidence that need to be evaluated are intended outcomes and adverse impact. The intended outcomes of the Applied Math assessment are articulated by the three primary assessment claims. Empirical evidence should indicate that an assessment program achieves its intended outcomes and not unintended negative outcomes. Adverse impact refers to possible performance differences between demographic groups and how decisions derived from scores might adversely affect a specific group. The *Uniform Guidelines on Employee Selection Procedures* (EEOC et al., 2000) defined adverse impact in the area of employment selection.

11.7.1 Intended Outcomes

An evaluation of the three primary claims is presented in Section 11.5. Based on analyses of the Applied Mathematics assessment and the WorkKeys NCRC, it appears that scores from the assessment and levels of the credential are assisting individuals in finding suitable employment and assisting businesses in finding qualified workers.

With the updated Applied Math assessment, ACT is collecting outcomes data relating test scores to outcomes such as job performance, successful completion of educational programs, and other evaluative measures.

11.7.2 Adverse Impact

Chapter 12—Fairness—specifically addresses the Applied Math assessment and adverse impact. The chapter defines adverse impact and provides analysis and recommendations to employers regarding fair employment procedures.

When the Applied Math assessment or any WorkKeys assessment is used for pre-employment screening or other employment decisions, employers should conduct a well-documented job analysis that provides appropriate evidence linking the skills required on the job with the skills measured in the assessment. When cutoff scores are used to assist in decision making, they should be established at appropriate levels, and the process for identifying the levels should be clearly documented (AERA, et al., 2014; SIOP, 2003).

11.8 Applied Math—Ongoing Validation

ACT continually collects and analyzes data related to the validation of its products. With the development of the updated Applied Math assessment, ACT has begun the process of collecting data and evidence to determine the plausibility of its claims.

As outcome data is collected and analyzed, ACT will publish the findings through research reports and it will be supplementing the Technical Manual. In collecting and analyzing the data, ACT is cognizant of the two main populations served by the Applied Math assessment: adults in the workforce and students in high school, college, or career and technical programs. It is critical that validity evidence is collected and analyzed from both populations to confirm that it meets the needs of both. While specific details of the analyses are dependent on the available outcome data, ACT will analyze the relationships of scores on the Applied Math assessment to critical outcome variables including job performance, job attendance, job retention, and completion of training programs. With sufficient sample sizes, ACT will additionally analyze assessment scores and relationships by demographic groups such as gender, ethnicity, and job types.

Note

1. Sackett, Borneman, and Connelly (2008), applying meta-analytic methods to address range restriction and low reliability of outcome measures, estimate that the disattenuated correlation of general cognitive ability with job performance is 0.47.

Chapter 12

Assessment Fairness

This chapter contains evidence to address assessment fairness related to the WorkKeys[®] Applied Math assessment. The chapter adheres to the conceptual framework of fairness defined in the *Standards for Educational and Psychological Testing* (AERA et al., 2014). The *Standards* maintain that fairness is a fundamental validity component that requires evaluation throughout the assessment process, from design to test administration to score interpretation and use.

12.1 Test Fairness—Overview

Striving for the fairness of all tests is a professional responsibility and a fundamental component for the validation of test score use. The most recent edition of the *Standards* (AERA, et al., 2014) devotes an entire chapter to fairness. The *Standards* divide fairness into four elements, each requiring evaluation: (1) fairness in treatment during the testing process, (2) fairness in access to the construct(s) measured, (3) fairness as lack of measurement bias, and (4) fairness as validity of individual test score interpretations for the intended uses.

Whenever tests are used as part of the decision making process, whether for educational or workforce purposes, it is critical for the testing program to be developed and carried out in a fair and unbiased manner. ACT subscribes to the *Standards* definition of fairness regarding validation and test score usage.

A test that is fair within the meaning of the *Standards* reflects the same construct(s) for all test takers, and scores from it have the same meaning for all individuals in the intended test population; a fair test does not advantage or disadvantage some individuals because of characteristics irrelevant to the intended construct (AERA, et al., 2014, p. 50).

As a component of validation, evaluations of fairness are ongoing, with evidence being collected and reported throughout the life of a testing program. Evidence regarding the fairness of the Applied Math assessment is not limited to this chapter and is drawn from other chapters in the technical manual.

Further, ACT continually collects and analyzes assessment data. As additional data is collected and analyzed, ACT will continually issue reports related to the fairness of Applied Math score interpretations and use.

12.2 Fairness and Test Administration

Fairness during the testing process refers to examinees being assessed in a way that maximizes their opportunity for showing their standing on the construct (Wollack & Case, 2016). In other words, the entire testing process, from test design to scoring, facilitates test takers being able to perform their best and does not adversely affect the performance of an individual examinee or a group of examinees.

The design, development, and scoring of the Applied Math assessment incorporated principals of Universal Design (CAST, 2011) and Evidence-Centered Design (Mislevy et al., 2004) to assist in ensuring fairness to all test takers. ACT developed and documented standardized procedures for the training of test center staff for test administration. They have articulated room and equipment standards in an effort to support standardized and fair conditions for all test takers. They further have defined protocols for the handling of secure information to safeguard sensitive information and protect the privacy of examinees. When unexpected events occur at a test center, the Test Coordinator is required to file an Irregularity Report detailing the event and allowing ACT to make a determination as to whether the event compromised validity. WorkKeys has implemented these procedures as a means to attain fairness for all examinees in the administration of the Applied Math assessment. (See Chapter 4 of the Technical Manual for a comprehensive review of the test administration procedures.)

The Applied Math assessment is administered to examinees in both paper and online formats. To provide evidence of the fairness of scores across both administrative formats, ACT conducted a mode comparability study. ACT evaluated the mode effects at the item and score level. Through the analysis, ACT concluded that modes effects on examinee responses and scores were negligible. (For greater detail regarding the mode analysis, see Chapter 9.)

Although ACT recognizes that the standardization of procedures for test administration is critically important for ensuring that all examinees have an equal opportunity to demonstrate their standing on the construct, ACT also recognizes that flexibility is required to achieve true fairness. When the standardized administrative procedures hinder a test taker from demonstrating his or her standing on the construct, and the test taker provides proper documentation, accommodations to the standardized procedures are considered fair and appropriate.

12.3 Fairness in Access to the Construct Measured

Accessibility in the context of fairness refers to the extent to which examinees can access the knowledge, skills, and/or abilities intended to be measured by the test without being unduly burdened by aspects of the test or test administration that may affect or limit access (Stone & Cook, 2016). For

example, an examinee with a visual impairment may not be able to appropriately answer questions on the Applied Math assessment because he or she cannot clearly see the test materials. In such cases, the lack of accessibility to the test materials creates construct irrelevant variance. A second example might involve an examinee who has been diagnosed with mild Autism Spectrum Disorder (ASD). This examinee may require a special testing location, free from distractions with additional time to complete the test. ACT provides a variety of accessibility options for examinees designed to provide access to the intended test construct, while not violating the construct or giving the test taker an unfair advantage.

The supports provided on the Applied Math assessment are structured along a continuum of increasingly intensive supports designed to meet the needs of all potential examinees. Three levels of accessibility supports are provided: 1) Embedded Tools, 2) Open Access Tools, and 3) Accommodations. Embedded tools are commonly used by many people, available to all examinees, and do not need to be requested in advance. Open Access Tools are used by fewer people, are also available to anyone, but their use must be identified and planned for in advance. Accommodation supports and tools are the most intensive level of support. Accommodations are available to those who are qualified to use them. Examinees who receive accommodations have a formally documented need and have therefore been identified as qualifying for resources that require expertise, special training, and/or extensive monitoring to select and administer effectively and securely.

All accessibility supports permitted for the Applied Math assessment are designed to remove unnecessary barriers to performance, while not violating or interfering with the measurement of the intended construct. (See Chapter 5 for a comprehensive review of test accessibility features available for paper and online administrations.)

12.4 Fairness as Lack of Measurement Bias

Measurement bias has been characterized as “a source of invalidity that keeps some examinees with the trait or knowledge being measured from demonstrating that ability” (Shepard, Camilli, & Williams, 1985, p. 79). Measurement fairness requires that examinees of equal standing on the construct average equal scores on the assessment, regardless of group membership (Sackett et al., 2008). Consequently, measurement bias occurs when score interpretations are differentially valid for any group of examinees. To investigate the potential for measurement bias, ACT evaluates the internal structure of the Applied Math assessment by evaluating the invariance of the items and the overall assessment.

ACT evaluates measurement bias at the item level by applying a Differential Item Function (DIF) procedure (Holland & Wainer, 1993). DIF refers to a set of statistical methods used to identify items that individuals from one demographic group respond to differentially than individuals from another demographic group. DIF occurs when equally able examinees have different probabilities of answering an item correctly based on their group membership (AERA et al., 2014). Items flagged as demonstrating DIF contain statistical evidence of bias; but, statistical evidence alone is not sufficient to conclude measurement bias. ACT WorkKeys has established a process for conducting DIF analyses followed by external reviews of flagged items to determine measurement bias.

In conducting the DIF analyses, ACT compares item responses for two groups of test takers. The two groups are termed the Focal Group and Reference Group. The Focal Group is the group of primary

interest, and it includes protected classes under federal employment anti-discrimination laws. The Reference Group serves as the basis for comparison.

For WorkKeys DIF studies, for each item, three separate DIF analyses are conducted using three different comparison group pairs. The group pairs are identified in Table 12.1.

Table 12.1: Differential Item Functioning Evaluations—Group Comparisons

	Focal Group	Reference Group
1	Women	Men
2	African American	White non-Hispanic
3	Hispanic	White non-Hispanic

An item is flagged as containing DIF when one group of matched test takers has a higher probability of answering an item correctly than the other group. Because groups may differ on ability, the DIF analysis matches test takers on ability. (For the WorkKeys DIF studies, ACT matches test takers using total test score.)

For Applied Math items, the Mantel-Haenszel Delta DIF statistics (Dorans & Holland, 1993) are computed to classify items into three DIF categories: Group A—negligible DIF, Group B—moderate DIF, and Group C—large DIF. (The rules for classifying items into the three groups are presented in Table 12.2.) Items classified as either Category B or C are interpreted as flagged items requiring further review.

Table 12.2: WorkKeys DIF Classification Rules

Group A	MH delta (MHD) not significantly different from 0 (based on Chi Square test, alpha = .05) or $ MHD < 1.0$
Group B	MHD significantly different from 0 (based on Chi Square test, alpha = .05) and $\{ MHD \geq 1.0 \text{ and } < 1.5\}$; or MHD not significantly different from 0 and $ MHD \geq 1.0$
Group C	MHD significantly different from 0 (based on Chi Square test, alpha = .05 and $ MHD \geq 1.5$)

Note. Classification rules adopted from National Assessment of Educational Progress (NAEP) guidelines (Allen, Carlson, & Zelenak, 1999).

After ACT has analyzed the DIF statistics and classified items into groups A, B, or C, content specialists evaluate all flagged items (Category B and C) for possible bias. Item bias occurs when an aspect of item content places a group at a disadvantage. As a result, to determine if an item contains bias, item content must be thoroughly reviewed by external evaluators. ACT contracts with external evaluators who have training and expertise in cultural anthropology or multicultural education to review the flagged items. The

review includes evaluating the item's vocabulary or use of numbers and symbols, the knowledge needed to correctly answer, how accessible the knowledge is to test takers, the cognitive processes required, and possible test taker misinterpretations that might occur because of differences in life experiences or opportunity to learn. To assist in this review, ACT has identified five questions for use in the item review:

Status: Are the members of a particular group shown in situations that do not involve authority or leadership?

Stereotype: Are the members of a particular group portrayed as uniformly having certain aptitudes, interests, occupations, or personality characteristics?

Familiarity: Is there greater opportunity on the part of one group to be acquainted with the vocabulary? Is there a greater chance that one group will have experienced the situation or have become acquainted with the processes presented by an item?

Offensive Choice of Words: Has a demeaning label been applied or has a male term been used where a neutral term could be substituted?

Other: Are there any other indications of bias?

After the review of each item, the evaluators recommend one of the following actions:

1. Maintain the item as it is currently constructed and continue to use.
2. Send the item back to the content team for revision; reviewer identifies what aspect of the item should be revised.
3. Remove the item from the item pool.

In the case of the decision to maintain the item as it is currently constructed, the evaluator is essentially stating that the item appears to be fair and the DIF flag was a statistical anomaly. In this case, when the item is used on the next occasion, DIF statistics are again generated. If on the second testing occasion, it is not flagged for DIF, it is assumed to be a fair item and is maintained for use on future forms. If on the second occasion, it is flagged for DIF, it is now assumed to be a biased item, and it is marked in the pool and should not be used.

DIF procedures are an effective method for assessing measurement invariance (Liu & Dorans, 2016). Measurement invariance presumes that an assessment is measuring the same construct for all examinees, regardless of group membership.

12.4.1 DIF Analysis Results from Applied Math Field Testing

During the second step in the field testing process, ACT administered the two forms of the Applied Math assessment to 2,266 field test participants. Forty testing sites in 22 states participated. Of the sites, 13 were high schools and 27 were adult testing centers. Approximately, 61% of the examinees were high school students and 39% were adults. Prior to administration, ACT required the field test participants to answer a series of questions related to their age, educational background, gender, and ethnicity. From the information the participants provided, ACT was able to conduct a series of analyses to better understand the fairness of the forms and items. Table 12.3 presents the demographic characteristics by test form for the Applied Math assessment.

Table 12.3: Applied Math—Number and Percent of Field Test Participants by Demographic Group

Demographic Characteristic	Applied Math					
	Form MS1		Form MS2		Total	
	Number	Percent	Number	Percent	Number	Percent
Total Participants	1,185	49.8%	1,196	50.2%	2,381	100%
Men	549	46.3%	513	42.9%	1,062	44.6%
Women	609	51.4%	648	54.2%	1,257	52.8%
African American	206	17.4%	233	19.5%	439	18.4%
American Indian	27	2.3%	19	1.6%	46	1.9%
Asian American	9	0.8%	6	0.5%	15	0.6%
Hispanic	79	6.7%	82	6.9%	161	6.8%
Native HI/Pacific Islander	1	0.1%	1	0.1%	2	0.1%
Two or more ethnicities	102	8.6%	101	8.4%	203	8.5%
White non-Hispanic	719	60.7%	714	59.7%	1,433	60.9%
Prefer not to respond	42	3.5%	40	3.3%	82	3.4%

DIF analyses were generated for comparisons of Women and Men, and for comparisons of African-American and White, non-Hispanic examinees. (The number of Hispanic-American examinees in the field test sample was too small to conduct a DIF analysis.) For the two forms, consisting of 68 items, seven items were flagged for C-Level DIF. The summary of the DIF analyses for the two forms are presented in Table 12.4.

Table 12.4: Identifications of C-Level DIF items on the two Applied Math Forms

Test	Form	# of Flagged Items	Favored Group
Applied Math	MS1	4	African Americans, Whites
Applied Math	MS2	3	Men, Women

The DIF analysis from the field study needs to be interpreted with caution. First, the sample sizes for African Americans for each form was small ($n = 207$ and $n = 225$). Due to the limited size of the samples, generalizing from the analysis could result in unwarranted interpretations. As a result, ACT will continue generating DIF analyses for test forms and will continue to update the technical manual as new data becomes available through the national and statewide testing programs. Because DIF methods require large sample sizes, for other demographic group comparisons, insufficient test sample sizes preclude ACT from conducting additional DIF analyses.

12.5 Fairness as Validity of Individual Score Interpretations

Fairness of individual score interpretations becomes an important consideration when an assessment score is used as part of a process for making high-stakes decisions. ACT concludes that when a WorkKeys score is used as part of the process to make a decision related to employment, it constitutes high-stakes test use. In these cases, federal rules and procedures should be followed by those using the WorkKeys scores in order for them to have valid, fair, and legal score interpretations.

Federal agencies responsible for enforcing civil rights legislation collectively published the *Uniform Guidelines on Employee Selection Procedures* (EEOC et al., 2000), which regulate how an assessment process may be used to assist in employment selection. If a selection procedure produces adverse impact for a protected group, the procedure should not be used unless the employer is able to demonstrate that the assessment measures skills that are job-related.

Adverse impact occurs when a seemingly neutral employment selection practice has a disproportionately negative effect on members of a protected group (Society for Human Resource Management [SHRM], 2015). Under applicable federal law, adverse impact does not require any intention on the part of the employer to discriminate. The EEOC has defined disproportionately negative effect using two different methods. The first method is frequently referred to as the 80% rule. Adverse impact occurs when the protected group is selected at a rate that is less than 80% of the reference group. The second method is referred to as the statistical significance test. This method attempts to answer the question is the difference in selection rates greater than that which would be expected by chance. It uses Fisher's Exact Test and interprets a difference of two standard deviations as indicating adverse impact.¹

When a selection process that uses assessment scores shows adverse impact, the burden of proof shifts to the employer. The employer must then demonstrate that the assessment measures job-related skills and is justified by business necessity. Business necessity requires that the employer demonstrate a clear relationship between the selection procedure and job requirements.

Differences in scores is not evidence of test bias. There are many reasons why such differences may exist with a cognitive ability test. Ultimately, a differential prediction study may be conducted to examine test bias and whether there are differences in the slope and intercept of regression equations used to predict an outcome (e.g., job performance, turnover) for demographic groups. This type of analysis can be conducted with applicants if they are later employed or by administering a test to incumbents and using extant data on outcomes to examine test bias. ACT is actively recruiting organizations to participate in both validity and fairness studies to examine these issues. Further, organizations using WorkKeys should conduct a job analysis if they intend to use the Applied Math test scores as a part of their employment decision.

When the Applied Math assessment, or any WorkKeys assessment, is used for pre-employment screening or other employment decisions, employers should conduct a well-documented job analysis that provides appropriate evidence linking the skills required on the job with the skills measured in the assessment. When cutoff scores are used to assist in decision making, they should be established at appropriate levels, and the process for identifying the levels should be clearly documented (AERA et al., 2014; SIOP, 2003).

The *Uniform Guidelines* along with the *Standards* recognize the use of job analysis coupled with a content evaluation as a means of validating the selection process. ACT developed its Job Profiling process to meet the validation requirements of the *Uniform Guidelines*. Table 12.5 describes the validation requirements of the *Uniform Guidelines* and how ACT’s Job Profiling process meets the requirements.

Table 12.5: Comparing the Requirements of the *Uniform Guidelines* to the ACT WorkKeys Job Profiling Procedure

<i>Uniform Guidelines</i> Requirement	WorkKeys Job Profiling Procedure
A job analysis that generates descriptions of job behaviors, descriptions of tasks, and measures of their criticality	SMEs (Subject Matter Experts participating in the job profiling procedure) establish a list that describes behaviors and tasks with tasks from O*NET API in SkillPro software and customize using information gained from company materials, interviews, and job shadowing. Then, SMEs rate each task for importance and the SkillPro software averages their ratings in order to yield a list of tasks in order of importance.
Demonstrate that the test is related to the described job behaviors and tasks	ACT job profilers report the percentage of important tasks that require the skill (average SME importance ratings of 2.5 or above on a 0 to 5 scale).
Definition of skills in terms of observable work outcomes	Each WorkKeys skill and skill level is defined with specific criteria and is illustrated with multiple workplace examples. SMEs link these definitions to job behaviors and tasks.
Explanation of how the skills are used to perform the tasks or behaviors	SMEs identify important tasks that require the skill under review. SMEs link specific tasks to a skill level and say how the level is used for the tasks.
No decisions can be made based on knowledge, skills, and abilities that can be learned quickly on the job or in training	SMEs identify the skill level required for job entry. New hires should enter the job with this level, not learn it on the job.
Applicants can be assessed on skills for higher-level jobs only if new hires may advance quickly to the higher-level jobs	SMEs identify the skill level required for performing the job on the first day. In addition, they may set a higher skill level for performing the job effective after training.
The rationale for setting the cutoff score must be provided	SMEs identify cutoff skill levels by describing job tasks and linking skill level descriptions and sample items to cutoff levels.
Cutoff scores are to be consistent with normal expectations of workers	SMEs identify the cutoff skill levels based on the normal requirements of the job; not on unusual situations, desired capabilities, or beliefs regarding their own skill levels.
Scores are interpreted as pass/fail only; they must not be interpreted as rank ordering of test takers	WorkKeys scores show that test takers either have the required skill levels or they do not have them. It is not appropriate to rank order test takers based on their level scores.
Documentation regarding the validation process is maintained	ACT Job Profilers present a full report documenting content-related validity evidence, and retain all related worksheets and computer records.

Anytime an employer wants to use a WorkKeys assessment as part of the selection process, ACT recommends that the employer utilize the Job Profiling process to assist in determining both the requisite skills and levels for the job. In utilizing Job Profiling, the employer is making the most efficient use of the WorkKeys assessment suite. Further, the employer is also providing job applicants a fair method of selection consistent with the *Uniform Guidelines*.

Note

1. In its commitment to fairness in assessment practices, ACT continually monitors examinee scores by group membership. With the recent launch of the updated assessments, ACT currently does not have sufficient volumes of examinee scores to conduct an analysis by group membership. As the updated assessments are administered to more examinees, ACT plans to analyze and publish score distributions for gender and ethnic groups. ACT plans to publish a revision to the technical manual (specifically adding score distributions by groups to Chapter 12) in the next six to twelve months.

Chapter 13

Defining Readiness for Work and Careers

There are many dimensions along which an individual needs to develop to be prepared for success throughout a lifetime. The path to success becomes more complex as individuals leave formal education systems and enter the workforce, where they must apply their knowledge and skills to demonstrate performance. College readiness, which is defined as having the skills and achievement levels needed to succeed in first-year, credit-bearing courses without remediation, is necessary for college success. On the other hand, core academic skills are necessary but not sufficient for college, career, and workplace success (Mattern, Burrus, Camara, O’Conner, Hanson, Grambrell, Casillas, & Bobek, 2014). A more holistic approach is needed to assess readiness across various transition points along the education and career continuum.

Readiness is applicable along a continuum, starting with a general or global standard for the typical level of skills needed for most jobs in the economy, to skill levels needed to be successful in a career pathway or for specific occupations. Career readiness is defined as having the Knowledge, Skills, Abilities, and Other characteristics (KSAOs) needed and the levels of those KSAOs needed to be successful in a typical job in a typical organization. Within the context of career readiness, foundational skills are the fundamental, portable skills that are critical to training and workplace success (Symonds, 2011). These skills are fundamental in that they serve as a basis—the foundation—for supporting more advanced skill development. And they are portable because, rather than being job specific, they can be applied at some level across a wide variety of occupations or within a career pathway. Readiness for a career pathway requires individuals to have the KSAOs and levels of KSAOs to be successful in a typical job within a career pathway.

In contrast to career readiness, a “work ready” individual possesses the KSAOs needed to be minimally qualified for a specific occupation as determined through a job analysis or occupational profile (ACT, 2013a). The skills needed for work readiness (a) are both foundational and occupation specific, (b) vary in both importance and level for different occupations, and (c) depend on the critical tasks identified via a job analysis or an occupational profile. Work readiness skills include foundational cognitive skills such as reading required for the workplace, applied mathematics, graphic literacy, problem solving, and critical thinking.

13.1 Work and Career Readiness Standards and Benchmarks

ACT® Work Readiness Standards and Benchmarks are precise descriptions of the knowledge and combination of skills that individuals need to be minimally qualified for a target occupation. These standards and benchmarks are determined by the level of skills profiled for a national representative sample of jobs in a given occupation (ACT, 2013a). While work readiness standards establish the mix of skills and range of levels reported by employers (i.e., minimum and maximum) for specific occupations, work readiness benchmarks are considered to be a target skill level (i.e., median) that an individual should aim for in order to be considered work ready for that occupation. The standards and benchmarks ensure that current and prospective employees' skills are aligned with employer skill requirements. They also ensure that individuals develop the foundational and job-specific skills necessary to be successful throughout a lifetime. ACT Career Readiness Standards and Benchmarks apply a similar methodology used to determine work readiness by providing individuals with a snapshot of skill requirements for different career pathways (LeFebvre, 2015). Figure 13.1 provides a summary of the work and career readiness definitions and corresponding examples of use cases.

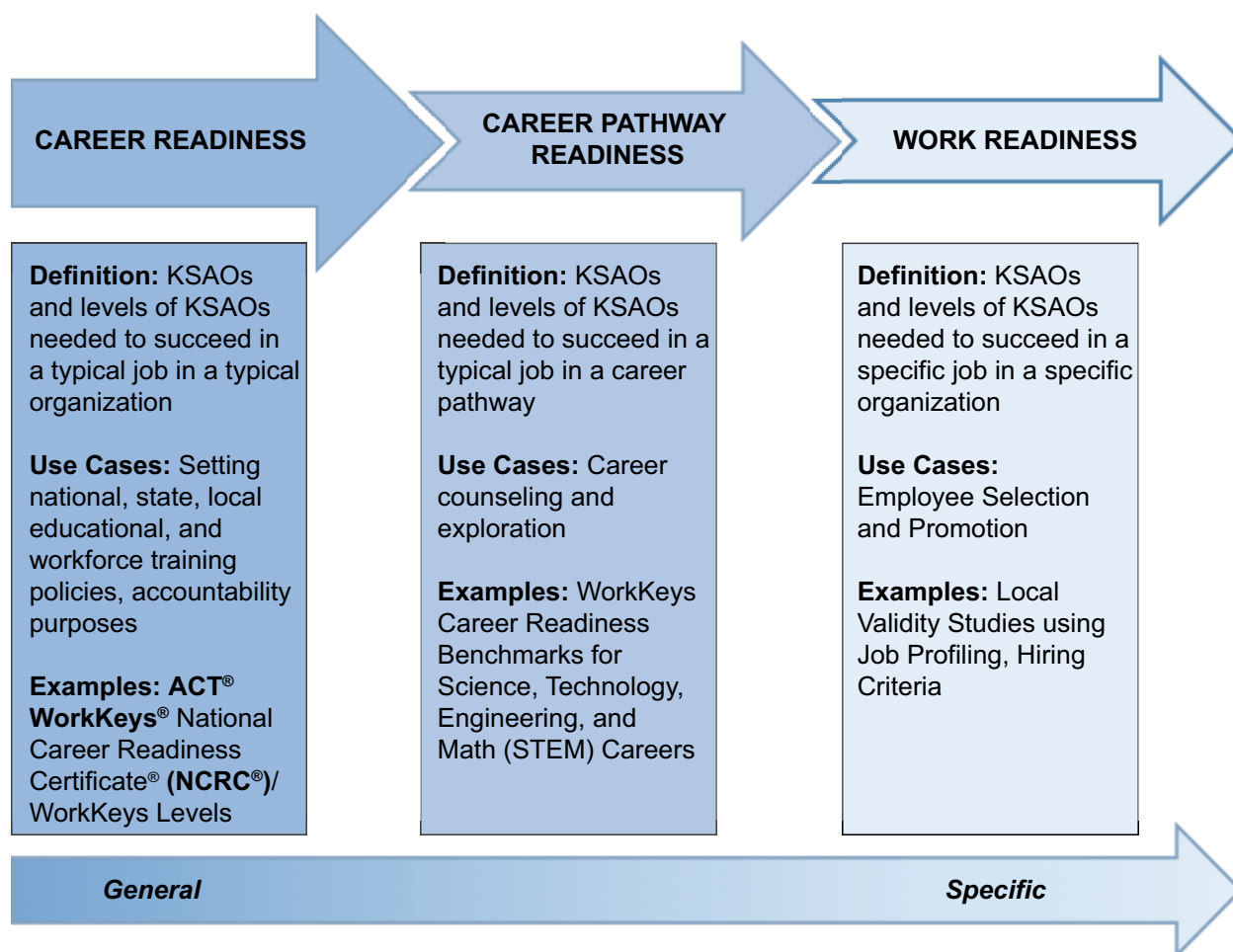


Figure 13.1: Summary of Work and Career Readiness

Source: Hierarchical Education and Workforce Readiness Framework. From *The development of an empirical framework linking college readiness and career readiness* by M. LeFebvre and K. Mattern, in press, Iowa City, IA: ACT, Inc.

13.2 Using WorkKeys Assessments for Career and Work Readiness

The ACT® WorkKeys® Assessments can be used with ACT® WorkKeys® Job Profiling and the WorkKeys NCRC as a comprehensive system to support skill training and development, personnel selection, career planning, workforce and economic development, and accountability. While career and work readiness are closely related, the type of use determines whether specific WorkKeys Assessment scores or the WorkKeys NCRC is an appropriate measure for readiness. The following section provides a summary of the different uses of the WorkKeys Assessments and the WorkKeys NCRC.

13.2.1 Personnel Selection and Development

WorkKeys assessments can be used for (a) pre-employment screening to identify individuals who have achieved levels of proficiency needed for a target job, (b) pre-employment screening to identify less desirable candidates based on behaviors associated with job performance, (c) employee development, and (d) developing the appropriate level of fit with occupations in terms of interests (LeFebvre, 2016).

When WorkKeys Assessments are used for pre-employment screening or other high-stakes employment decisions, employers should demonstrate that the knowledge and skills in the pre-employment measure are linked to work behaviors and job tasks either through job profiling or through research that links the assessment to job performance. When WorkKeys Assessments are used for employee development or the assessment of readiness for individuals or groups, criteria other than job performance may be more relevant (e.g., individual earnings, employment, or training completion). The WorkKeys Assessments should be used in combination with additional measures (e.g., tests, interviews, or other selection procedures) that the employer deems appropriate and relevant for pre-employment selection and other employment decisions.

13.2.2 Workforce and Economic Development

The WorkKeys assessments and the WorkKeys NCRC are widely used in workforce and economic development programs. For example, the WorkKeys assessments and the WorkKeys NCRC can be used by (a) an employer who uses the WorkKeys assessments or the WorkKeys NCRC and other criteria to identify a qualified pool of applicants and requires a specific level of WorkKeys NCRC or WorkKeys scores, (b) an employer who uses the WorkKeys NCRC to make employment decisions and does not require a specific level, (c) states, communities, and schools that use the WorkKeys NCRC to document an individual's level of essential work readiness skills, and (d) states, communities, or schools that use the WorkKeys NCRC to document the aggregate career readiness of a community, region, or state.

ACT® Work Ready Communities (WRC) are an approach for workforce and economic developers to certify that their community has a qualified workforce to support industry demand. This approach uses WorkKeys Assessments and the WorkKeys NCRC to measure foundational workplace skills with goals established for the current, emerging, and transitioning workforce. In order to be certified as a Work Ready Community, states and their counties establish goals based on the Work Ready Communities common criteria. The criteria are evaluated using the WorkKeys NCRC levels obtained across various subpopulations of the workforce (ACT, 2015). Skill gaps across various sectors of the workforce can be identified and addressed by state or local community policies and programs.

13.2.3 Accountability

State accountability systems, such as Career and Technical Education programs, have incorporated WorkKeys Assessments and the WorkKeys NCRC as a measure of employability skills or career readiness (Center on Education Policy, 2013). The WorkKeys NCRC is typically used in conjunction with other technical skills assessments such as industry-based certificates or licensing exams as part of a stackable credentialing system (ACT, 2013b). Some states also report using WorkKeys Assessment results as a requirement for graduation, for receipt of a career/technical diploma, endorsement on a standard diploma, or for scholarship eligibility.

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